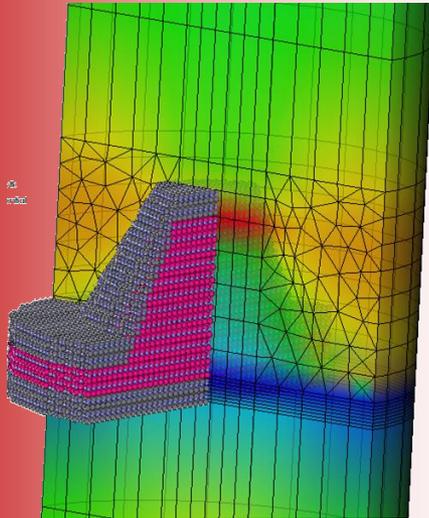


An overview of the TiberCAD capabilities

Alessandro Pecchia



CNR - ISMN *Institute for Nanostructured Materials*

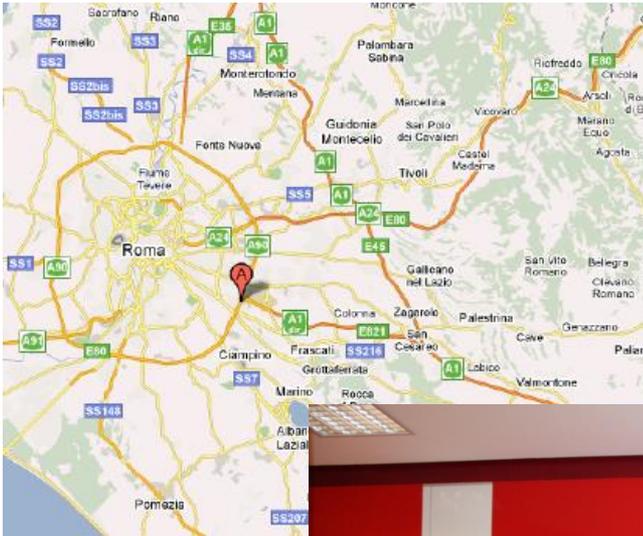


University of Roma "Tor Vergata"

*M. Auf der Maur, G. Penazzi, F. Sacconi, G. Romano
A Gagliardi, F. Santoni, A. Di Carlo*



University of 'Tor Vergata'
is the second University in Rome



OptoLab group



Dr. A. Pecchia



Prof. Aldo Di Carlo



Dr. M. Auf der Maur



Dr. A. Gagliardi



Mr. F. Santoni

tiberCAD

Multiscale Device Simulator

<http://www.tiberlab.com>

Dr. F. Sacconi



Dr. G. Romano



Dr. G. Penazzi



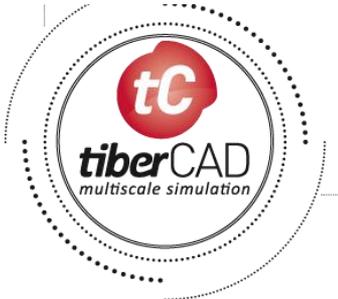
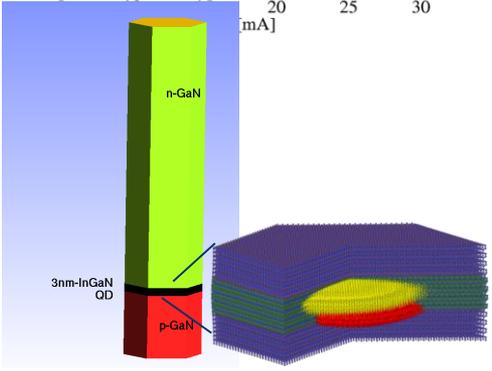
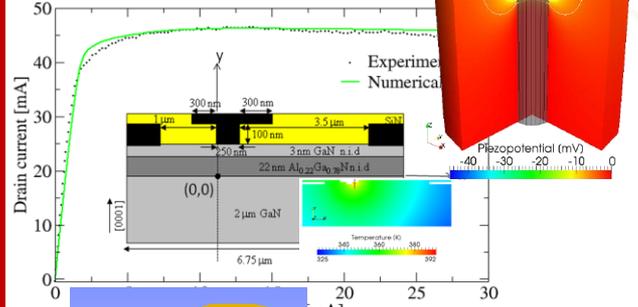
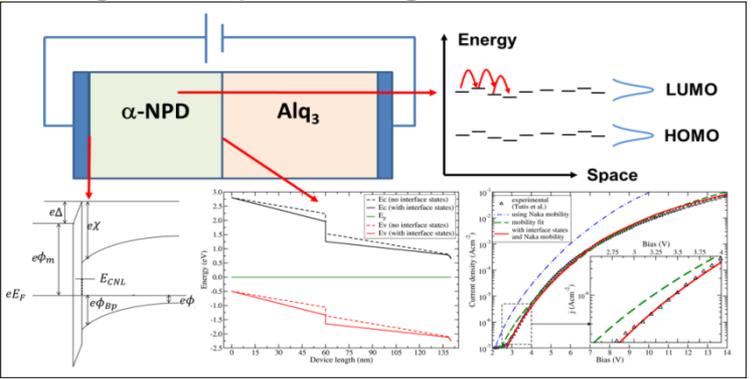
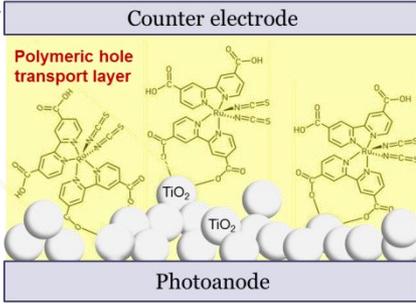
Mr. W. Rodrigues

DSSC/OPV module

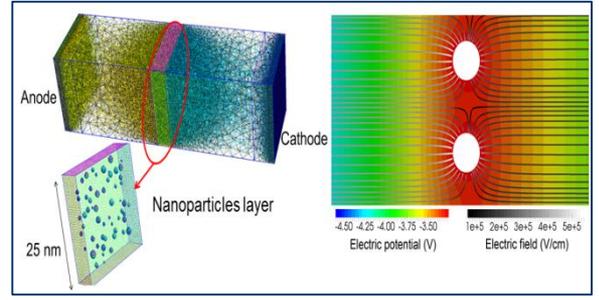
Charge transport in organic semiconductors

Piezoelectricity

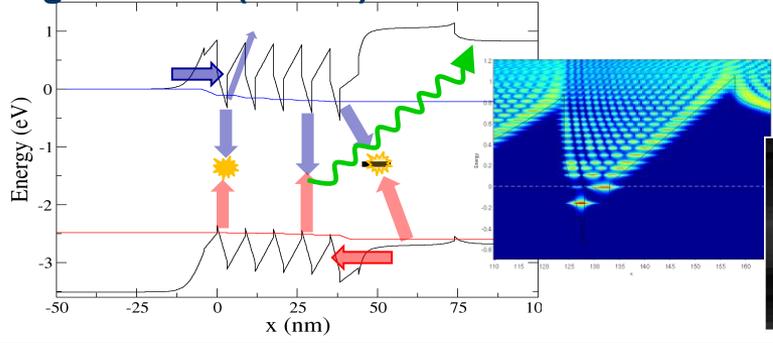
Heat dissipation



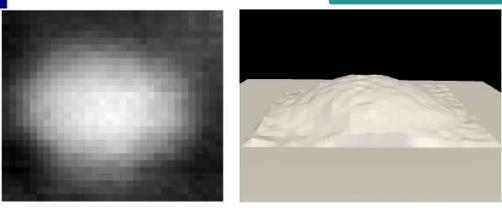
Memristors



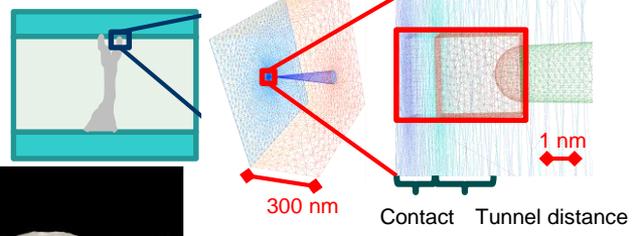
Inorganic LED (InGaN)



Quantum DOTS

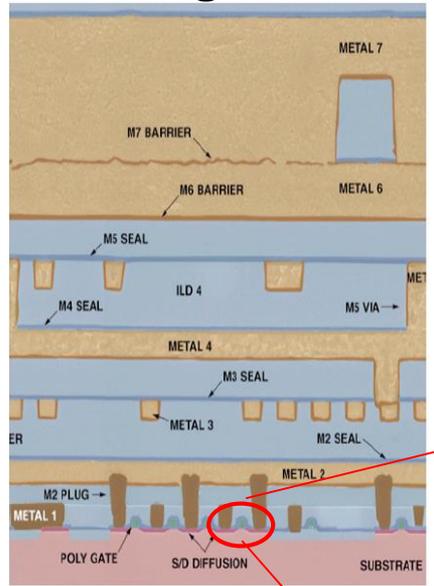


Nanofilaments

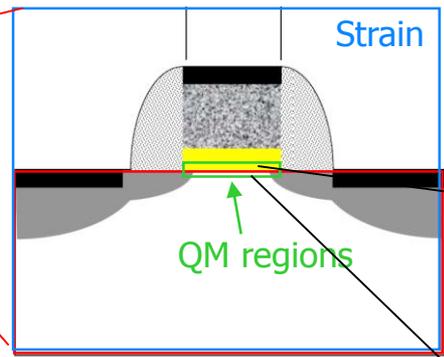


Different physical models on different scales are needed to describe electronic devices

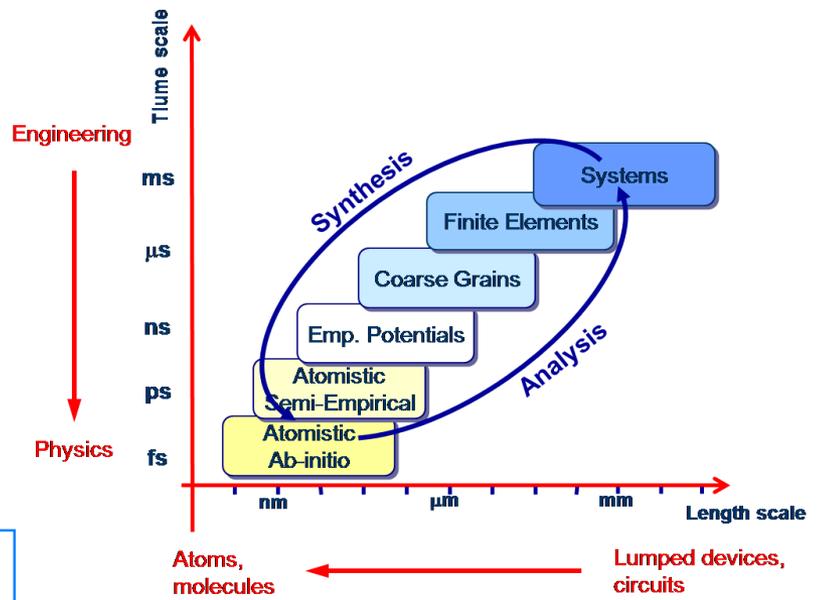
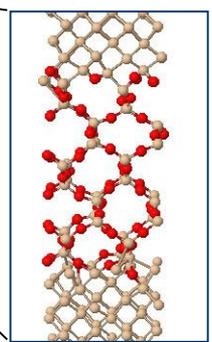
Package Level

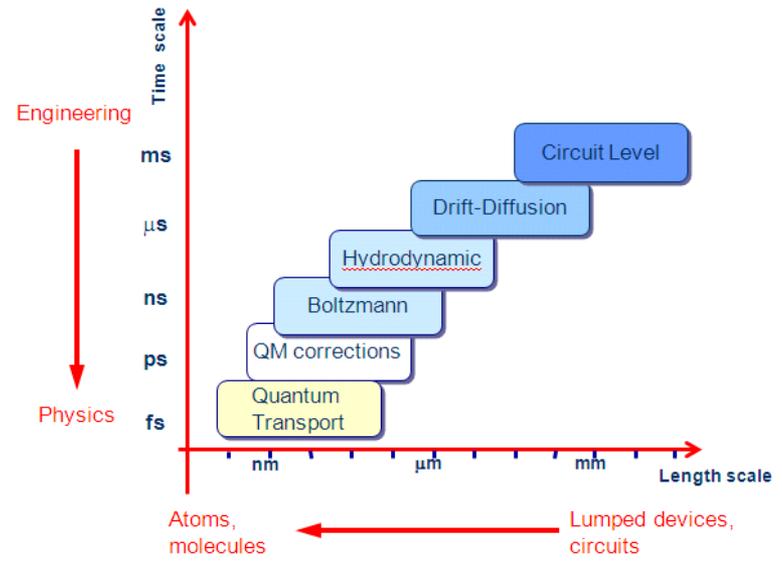
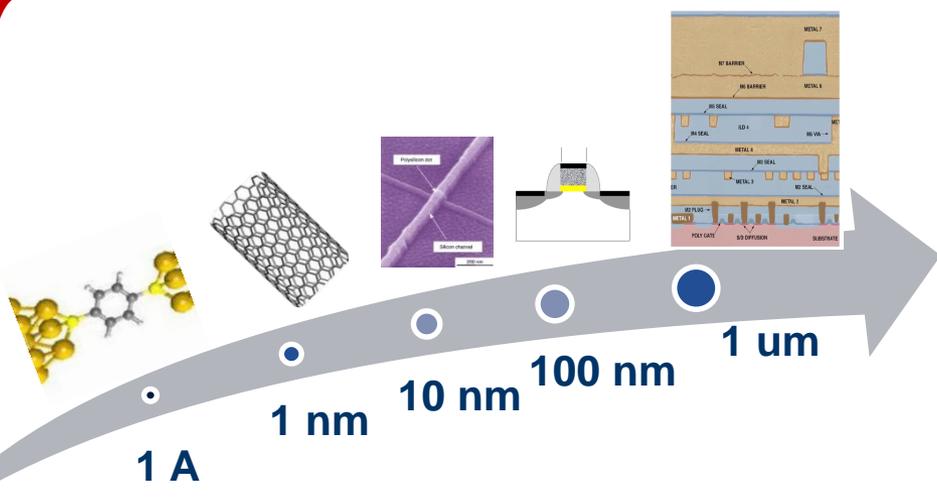


Device Level

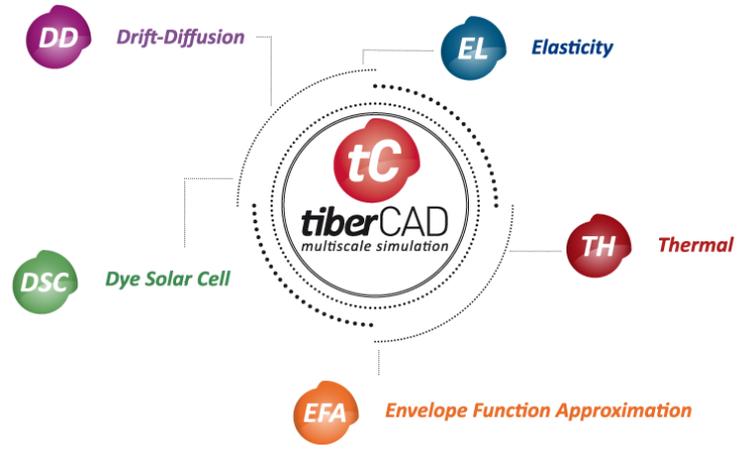


Atomistic Level

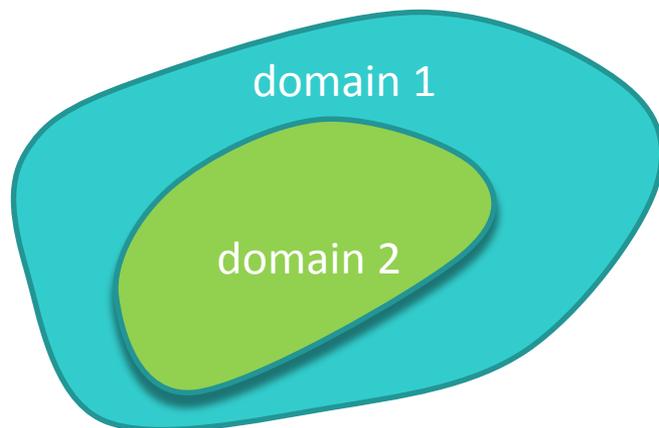




- Features:**
- drift diffusion, strain, thermal, EFA
 - VFF, ETB, DFTB
 - Organics, DSSC modelling.



OVERLAP METHOD



- each model computes physical quantities that act as parameters to the other models.

Schrödinger/Poisson

Transport parameters from DFT

BRIDGE METHOD

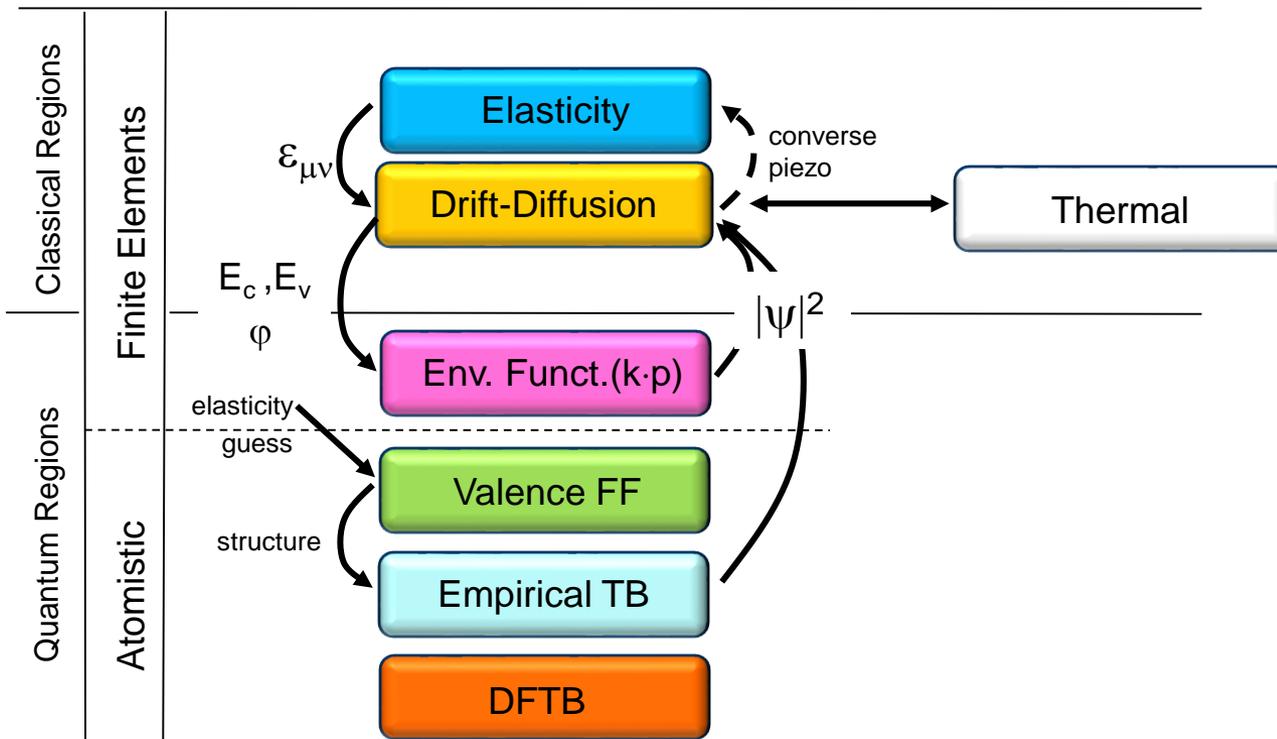


- each domain provides boundary conditions to adjacent domains.

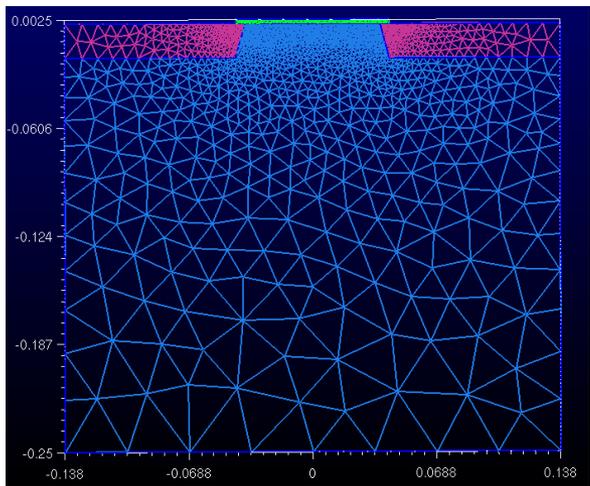
NEGF/drift-diffusion

VFF/continuous elasticity

M. Auf der Maur, G. Penazzi, G. Romano, F. Sacconi, A. Pecchia, A. Di Carlo
IEEE Trans. Electron Devices, 58, 1425 (2011)



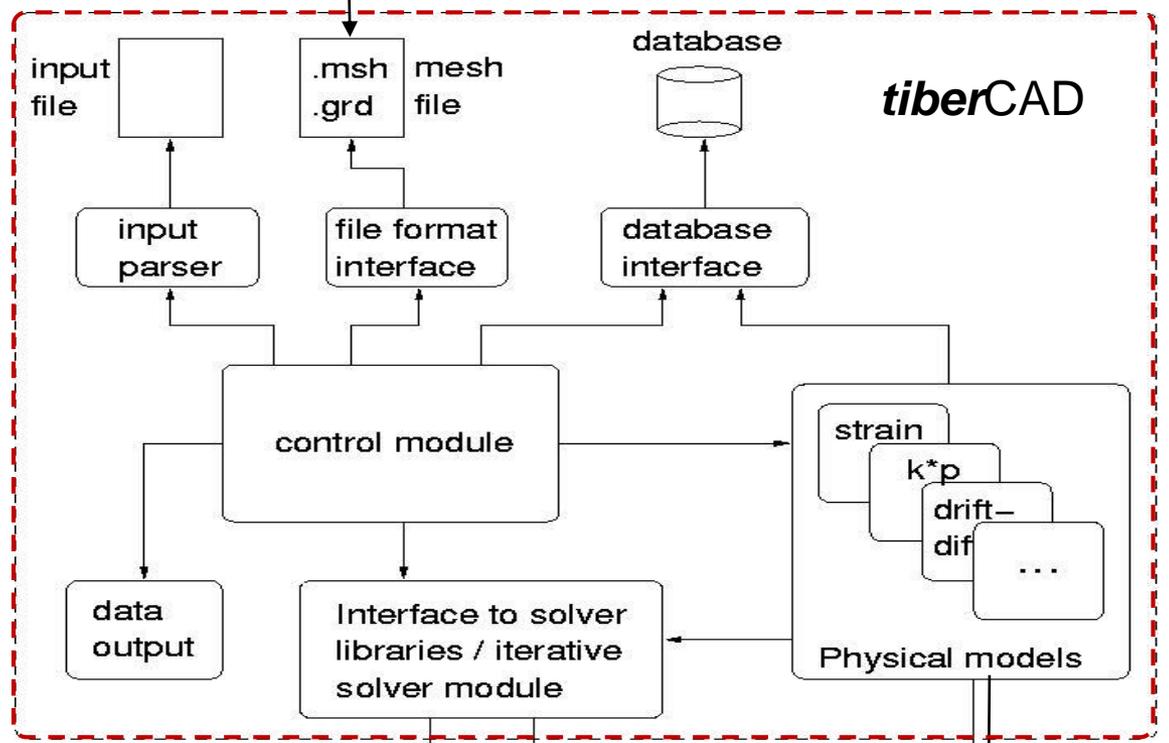
GMSH Device Modelling Mesh Generation



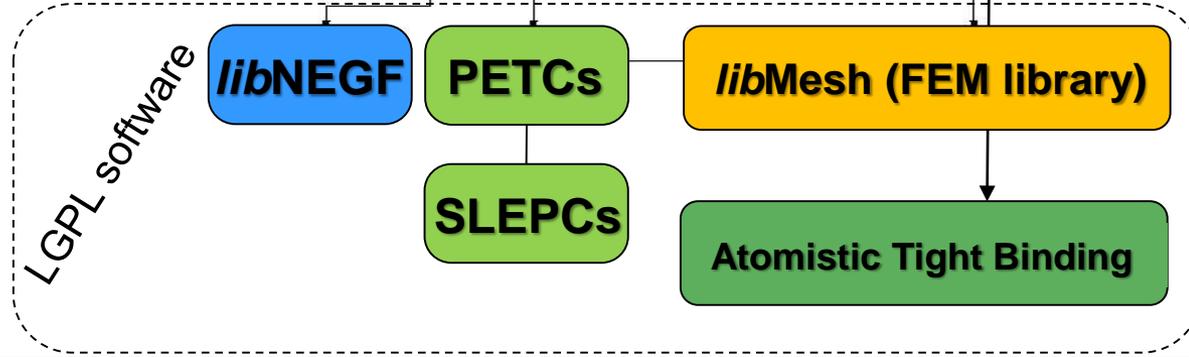
GPL software

Proprietary GUI/CAD/mesher
Under development

Postprocessing
Paraview



tiberCAD



LGPL software

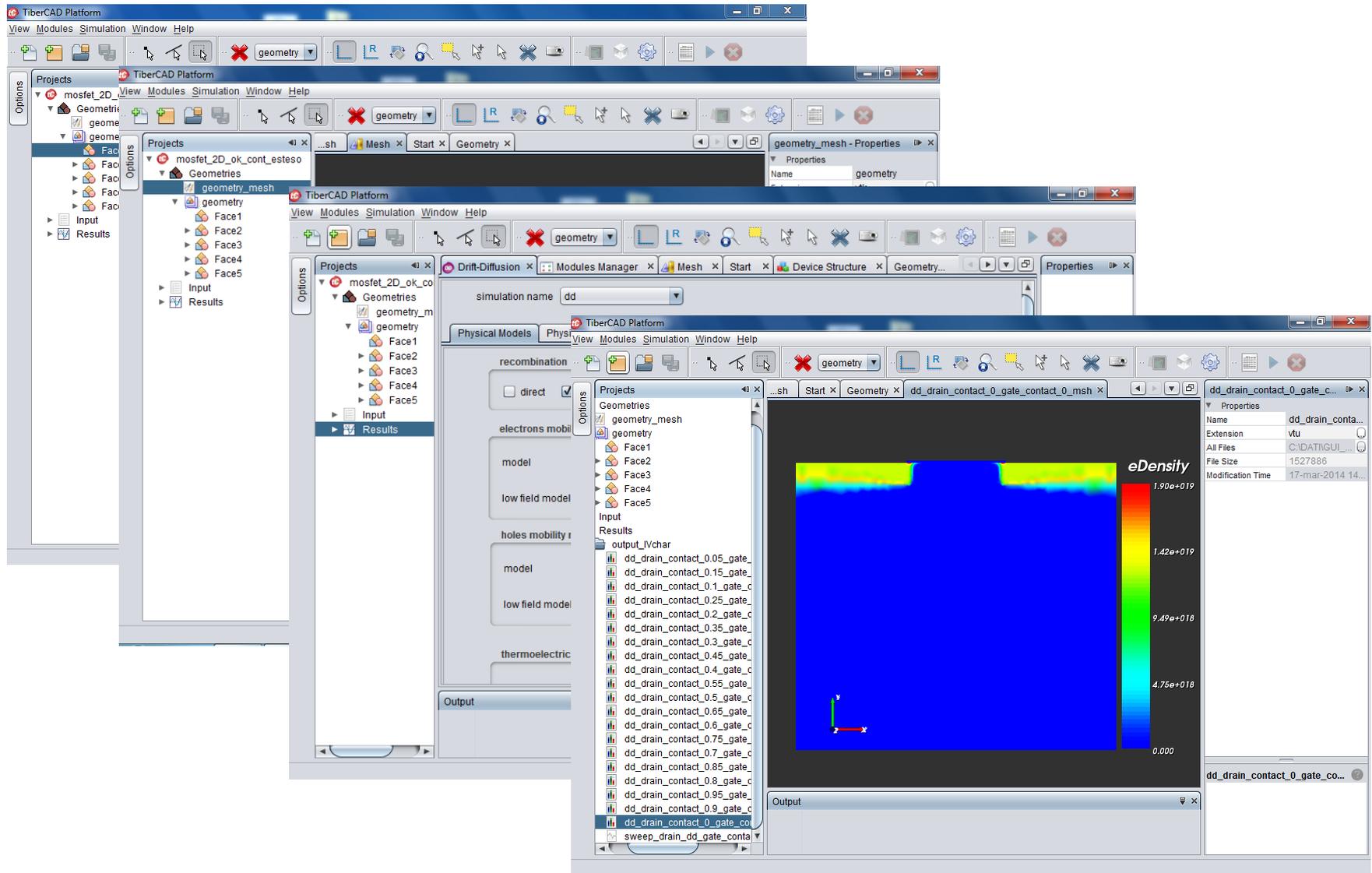
libNEGF

PETCs

libMesh (FEM library)

SLEPCs

Atomistic Tight Binding



Module elasticity

```
{
  name = strain
  regions = all
  plot = (Strain, Stress, Displacement)

  Solver {
    preconditioner = lu
    method = pconly
  }

  Physics {
    body_force lattice_mismatch {
      reference_material = GaN
    }
  }

  Contact substrate { type = clamp }
}
```

Drift-Diffusion

- Consider only $M^{(0)}$ and $M^{(1)}$, assuming carriers in thermal equilibrium ($T_e = T_0$)
- Assume term $(\mathbf{u} \nabla \mathbf{u})$ is negligible
- Define mobility and diffusivity: $\mu = q\tau/m^*$ and $D = k_B T_0 \mu / q$

Current equations

$$\mathbf{J}_n = qn\mu_n \mathbf{F} + qD_n \nabla n$$

$$\mathbf{J}_p = qn\mu_p \mathbf{F} - qD_p \nabla p$$

Continuity equations

$$\frac{\partial n}{\partial t} = \frac{1}{q} \nabla \cdot \mathbf{J}_n + G - R$$

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \nabla \cdot \mathbf{J}_p + G - R$$

+

Poisson equation: $\mathbf{F} = -\nabla V$

$$\nabla \cdot (\epsilon_0 \epsilon_r \nabla V) = -q(p - n + N_D - N_A)$$

key parameter: $\mu = \mu(F, T, N_D, N_A, \dots)$

Low Field

$$\mu(T) = \mu_0 \left(\frac{T}{300} \right)^\alpha$$

High field

Silicon-like

$$\mu(F) = \mu_0 \frac{1}{\left(1 + \left(\frac{\mu_0 F}{v_{sat}} \right)^\beta \right)^{1/\beta}}$$

GaAs-like

$$\mu(E) = \frac{\mu_0 + \frac{v_{sat}}{F} \left(\frac{F}{F_0} \right)^\gamma}{1 + \left(\frac{F}{F_0} \right)^\gamma}$$

Doping Dependent

$$\mu(N_D) = \mu_0 - A \ln \left[\frac{N_D}{n_i} \right]$$

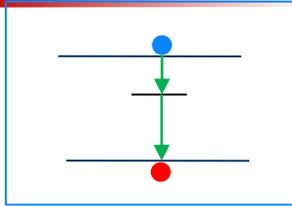
Organic transport

Hopping

$$\mu(F) = \mu_0(T) \exp \left[\sqrt{\frac{F}{F_0}} \right]$$

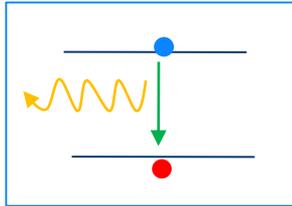
Band-like

$$\mu(F) = \frac{\mu_0(T) \sqrt{2}}{\left[1 + \sqrt{1 + \frac{3\pi}{8} \left(\frac{\mu_0 F}{v_s} \right)^2} \right]^{\frac{1}{2}}}$$



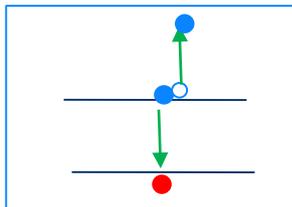
Shockley-Read-Hall (SRH) recombination (non-radiative)

$$R_{SRH} = \frac{pn - n_i^2}{\tau_p \left[n + n_i \exp\left(\frac{E_t - E_i}{kT}\right) \right] + \tau_n \left[p + n_i \exp\left(\frac{E_i - E_t}{kT}\right) \right]}$$



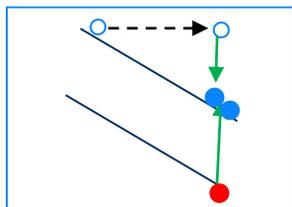
Radiative recombination

$$R_R = C(pn - n_i^2)$$



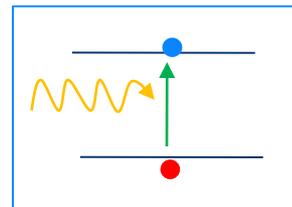
Auger recombination (non-radiative)

$$R_A = D_n(pn^2 - nn_i^2) + D_p(np^2 - pn_i^2)$$



Impact ionization generation (hot-carriers)

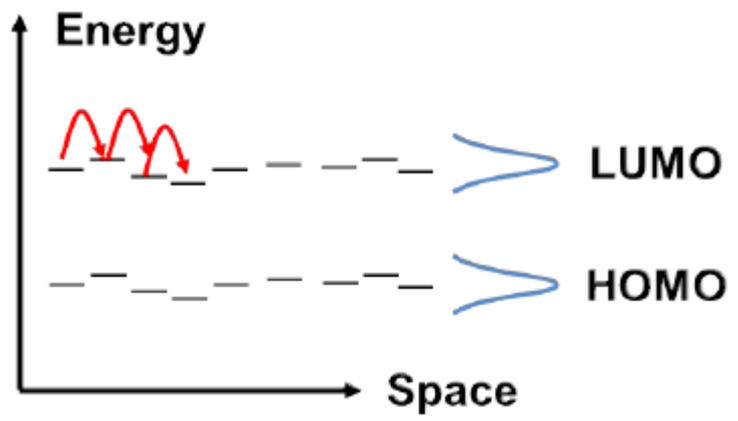
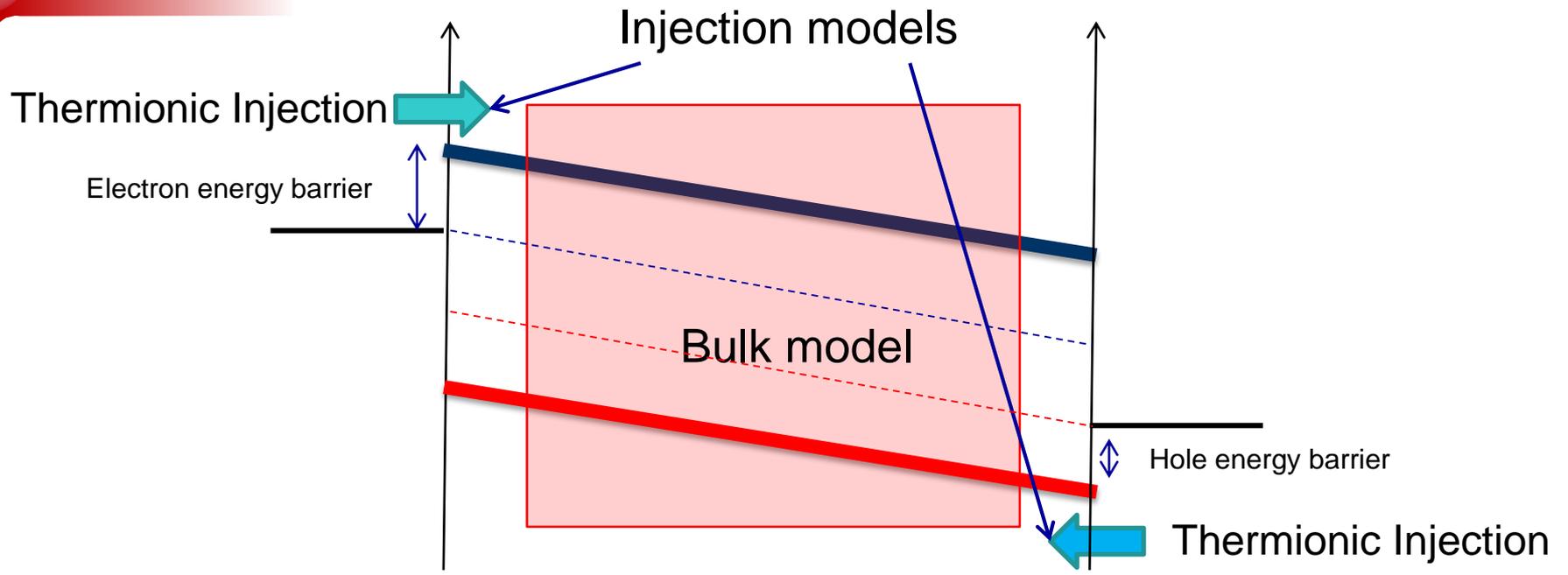
$$G_{II} = \alpha_n \frac{|J_n|}{q} + \alpha_p \frac{|J_p|}{q} \quad \alpha_{n,p}(F) = \alpha_{n,p}^{\infty} \exp\left[-\left(\frac{F_{n,p}^{crit}}{F}\right)^{\beta_{n,p}}\right]$$



Photoabsorption generation

$$G_{ph} = \alpha |E|^2$$

Special case for organics



Drift-Diffusion Model

$$\begin{cases} -\nabla(\epsilon_r \nabla \phi - \mathbf{P}) & = e(p - n - N_d^+ - N_a^-) \\ \nabla(\mu_n n \nabla \phi_n) & = G - R \\ -\nabla(\mu_p p \nabla \phi_p) & = G - R \end{cases}$$

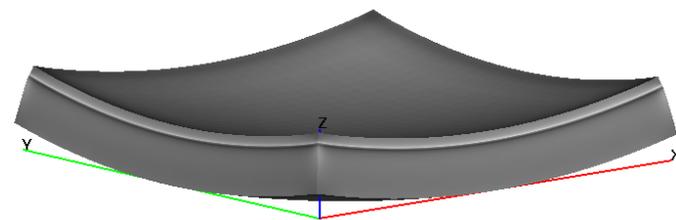
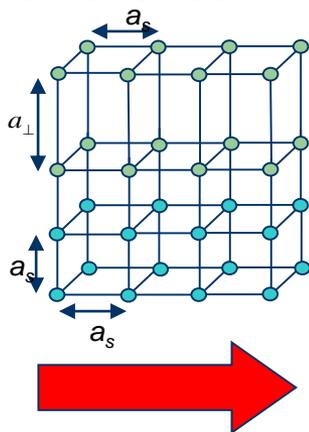
F. Santoni, A. Gagliardi, M. auf der Maur, A. Di Carlo, Organic Electronics 15 (2014) 1557–1570

Elasticity and Strain Module

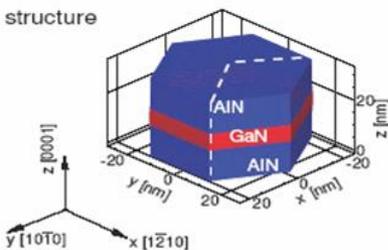
- External mechanical forces can be included as boundary conditions
- We can calculate shape deformation and piezoelectric effect $P_i = e_{i,jk} \varepsilon_{jk}$
- Converse piezoelectric effect can be included $\sigma_{jk} = -e_{i,jk} E_i$
- Thermal stress can be included $\varepsilon_{jk} = -\alpha_{jk} (T - T_0)$
- Several boundary conditions: substrate, plane, free



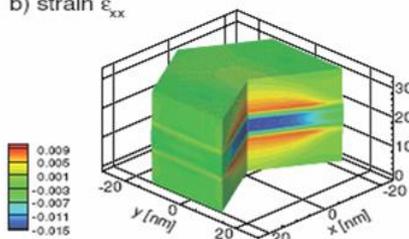
Free-standing AlGaN/GaN



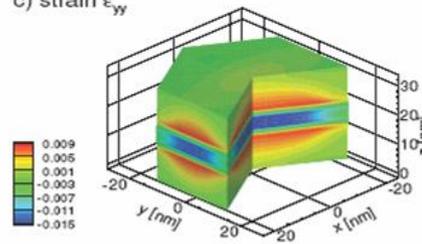
a) structure



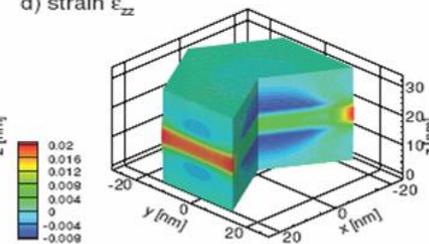
b) strain ε_{xx}



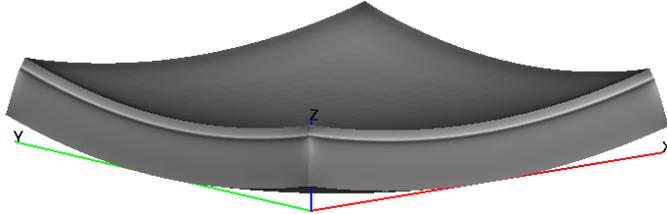
c) strain ε_{yy}



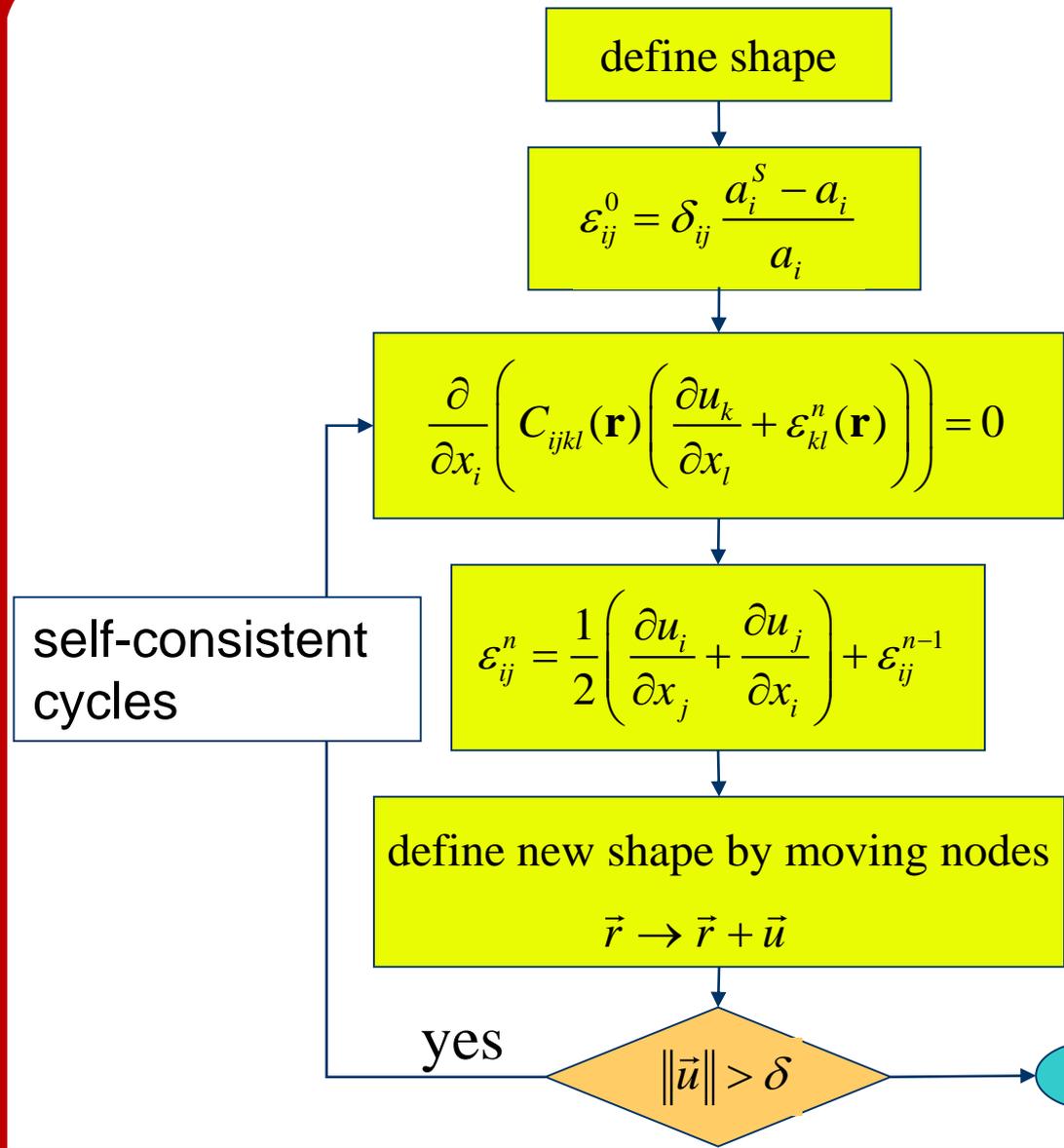
d) strain ε_{zz}



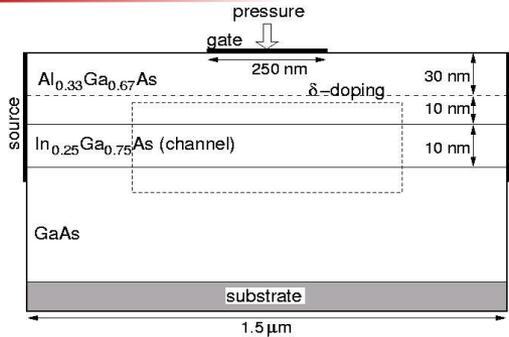
Free-standing AlGaIn/GaN



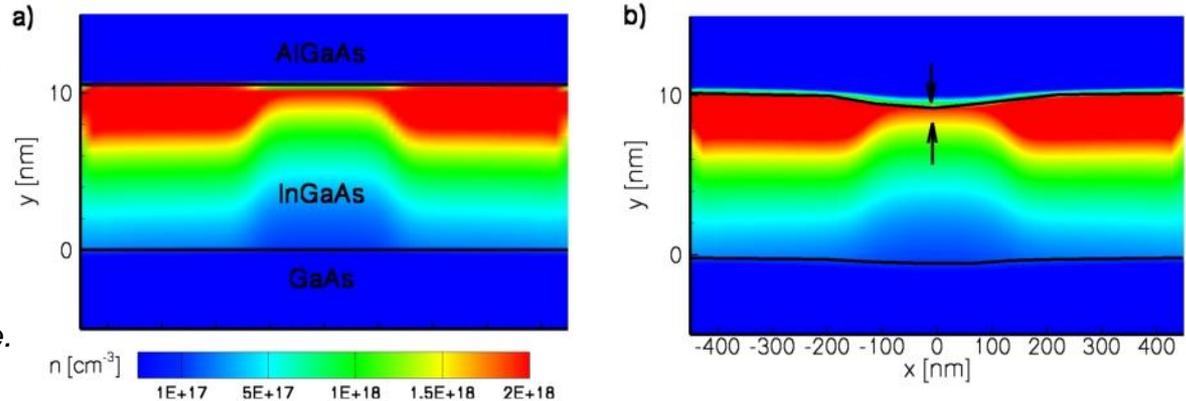
Adaptive grid are used



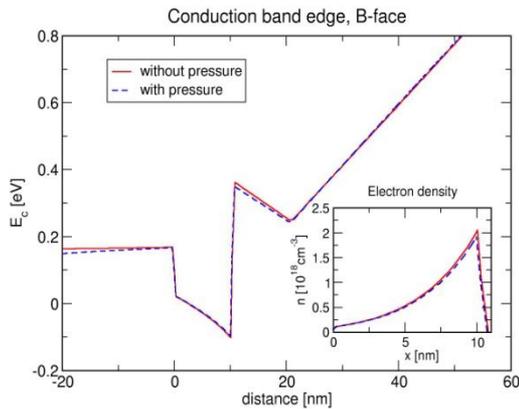
self-consistent cycles



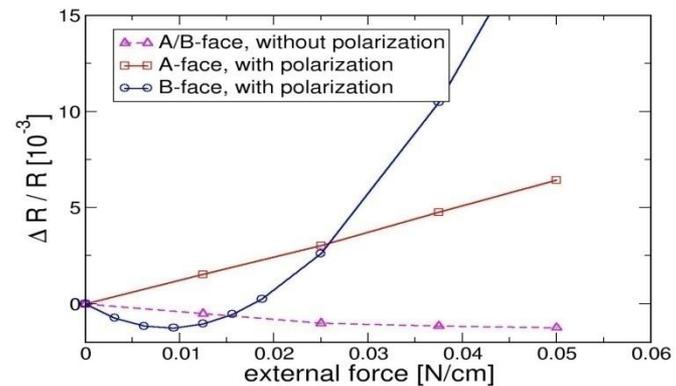
AlGaAs/InGaAs/GaAs HEMT structure. Growth directions [111] (A-face) and [11̄1] (B-face)-are considered.



Electron density in the AlGaAs/InGaAs/GaAs B-face structure without (a) and with (b) pressure ($F = 75\text{mN/cm}$).

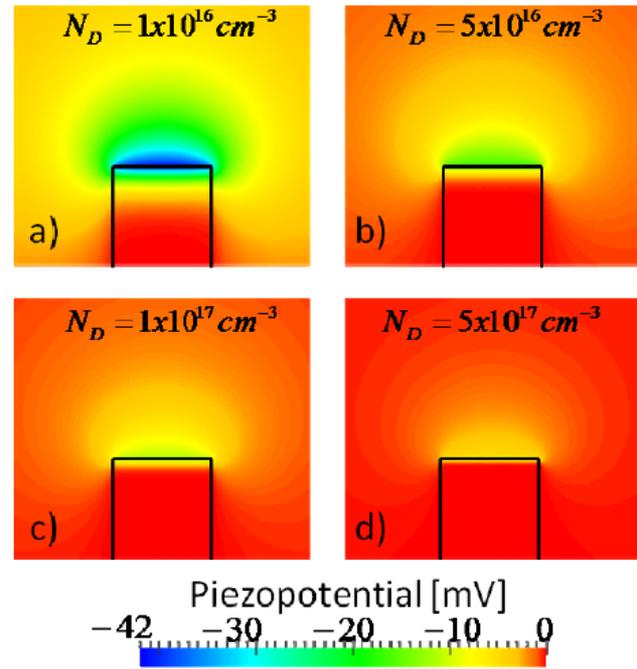
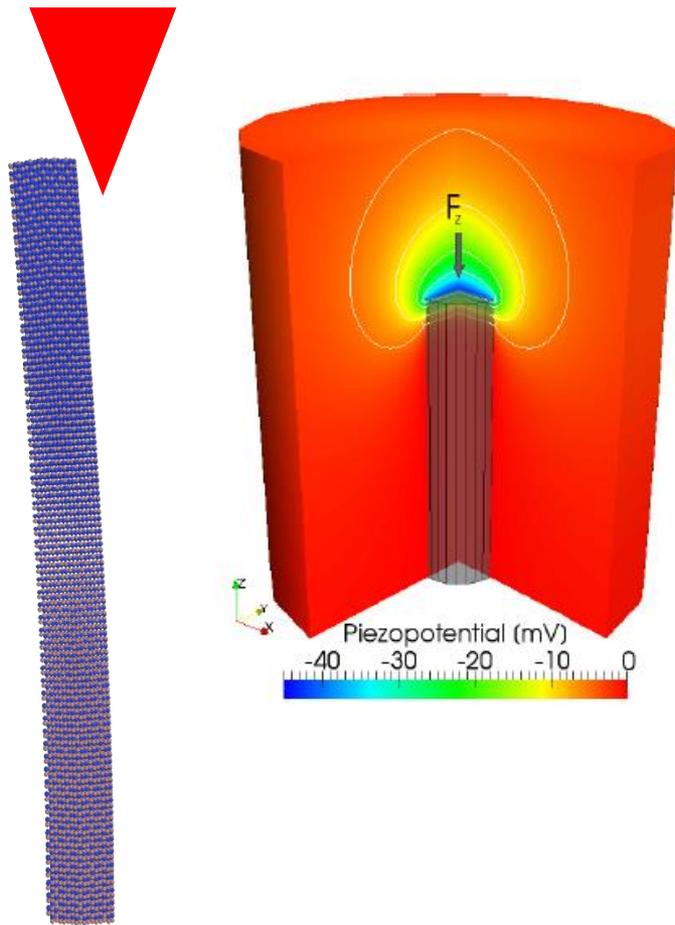


Band profile and classical electron density for the B-face structure with and without pressure.

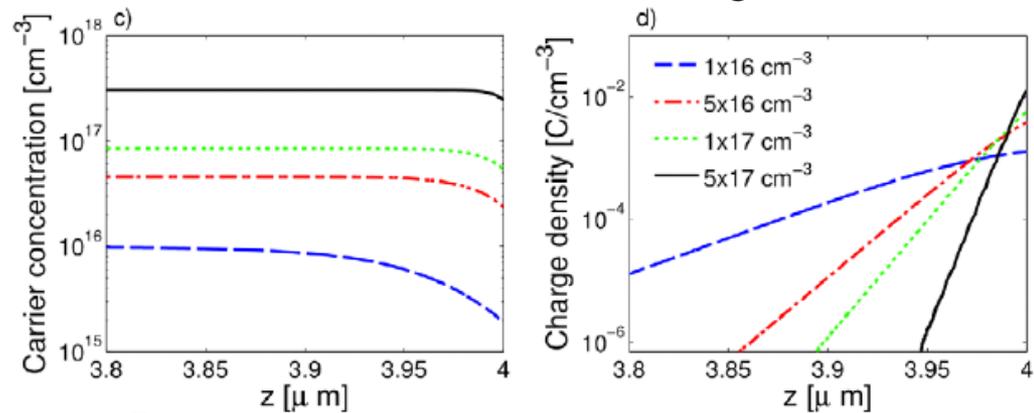


Piezoresistivity for the AlGaAs/InGaAs/GaAs structure. Gate voltage is 0 V.

Deformations and compressive stress



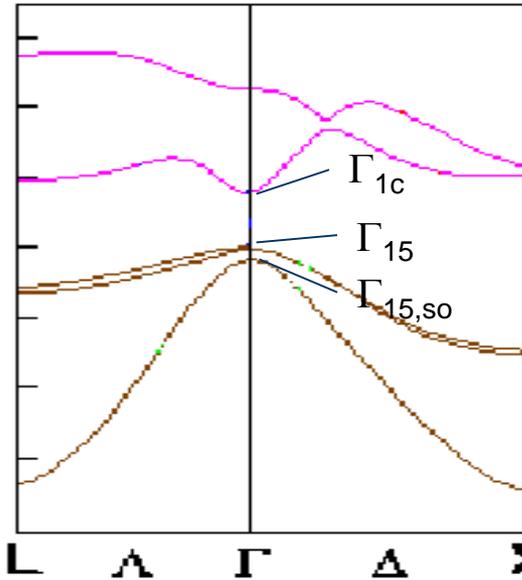
Free-carrier screening effects



G. Romano et al., Nanotechnology 22 (2011) 465401



Quantum States

Band-structure near $k=0$ 

$$H_{rs} = \frac{\hbar^2}{m^2} \sum_{i,j} k_i k_j \sum_{l\alpha\nu} \frac{\langle r | p_i | l\alpha\nu \rangle \langle l\alpha\nu | p_j | s \rangle}{E_{\Gamma_{15}} - E_{l\alpha}}$$

$$H_{3 \times 3} = \begin{bmatrix} Lk_x^2 + M(k_y^2 + k_z^2) & Nk_x k_y & Nk_x k_z \\ Nk_x k_y & Lk_y^2 + M(k_x^2 + k_z^2) & Nk_y k_z \\ Nk_x k_z & Nk_y k_z & Lk_z^2 + M(k_x^2 + k_y^2) \end{bmatrix}$$

$$\left[-\frac{\hbar^2}{2m} \nabla^2 + V_{cr}(r) \right] \psi_{n\mathbf{k}}(r) = E_n(\mathbf{k}) \psi_{n\mathbf{k}}(r)$$

$$\psi_{n\mathbf{k}}(r) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{n\mathbf{k}}(r)$$

$$\left[\hat{H} + \frac{\hbar}{m} \mathbf{k} \cdot \hat{\mathbf{p}} \right] u_{n\mathbf{k}}(r) = \left[E_n(\mathbf{k}) - \frac{\hbar^2 k^2}{2m} \right] u_{n\mathbf{k}}(r)$$

$$E_n(\mathbf{k}) \approx E_{\Gamma_{15}} + \frac{\hbar^2 k^2}{2m^2} + \Lambda_n$$

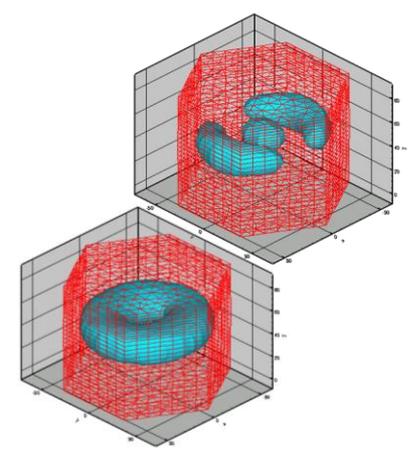
Diagonalize to find
Band n

k·p Hamiltonian generalizes single band dispersions

$$|\psi^i(r)\rangle = \sum_n |u_{n\Gamma}(r)\rangle \phi_n^i(r) \quad \leftarrow \text{Envelope function}$$

$$\sum_n \left[E_{\Gamma} \delta_{mn} + \frac{\hbar^2 k^2}{2m^2} \delta_{mn} + H_{mn}(\mathbf{k}) + V(r) \delta_{mn} \right] \phi_n^i(r) = E^i \phi_m^i(r)$$

k is interpreted as the usual momentum operator: $k_l \mapsto i\partial_l$



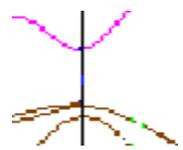
In TiberCAD:



$$H_{2 \times 2}$$

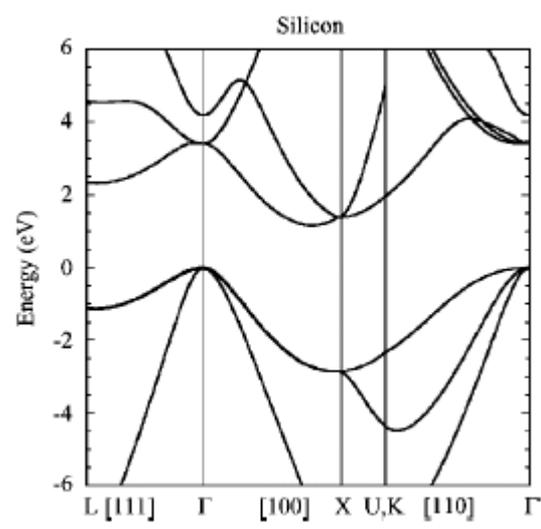


$$H_{6 \times 6} = \begin{bmatrix} H_{3 \times 3} & 0 \\ 0 & H_{3 \times 3} \end{bmatrix} + H_{so}$$



$$H_{8 \times 8} = \begin{bmatrix} H_{4 \times 4} & 0 \\ 0 & H_{4 \times 4} \end{bmatrix} + H_{so}$$

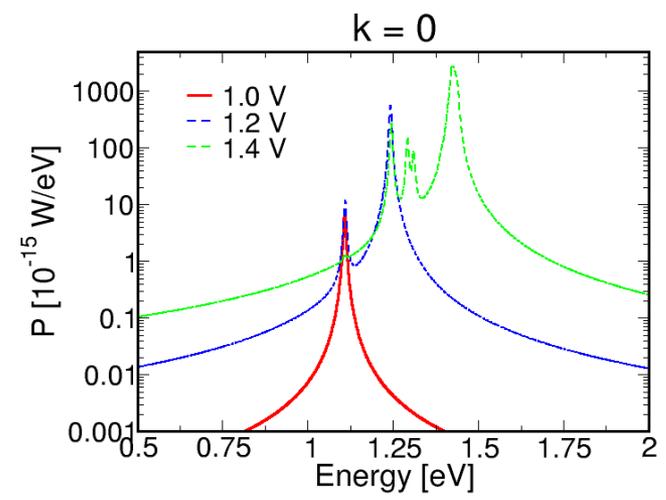
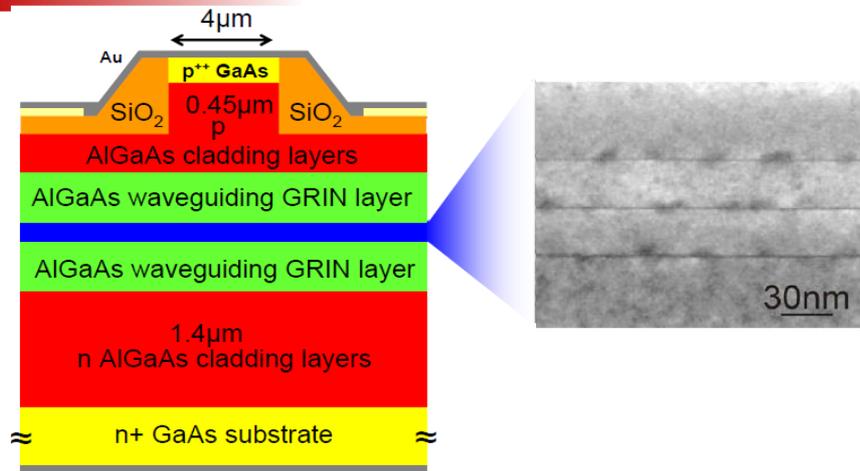
Full Band kp



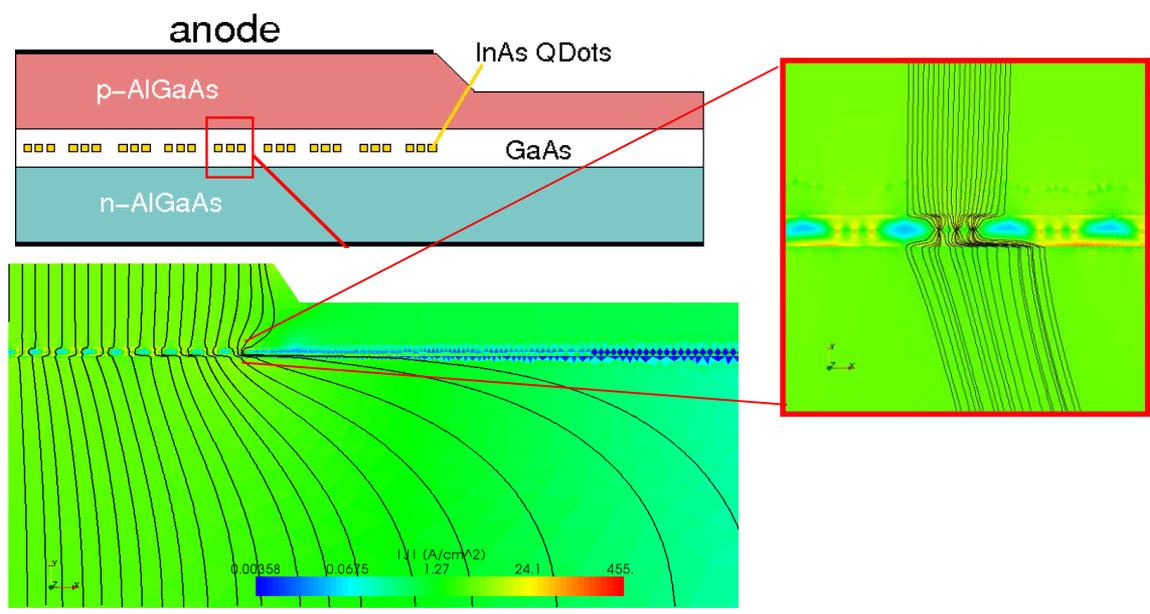
$$H_{30 \times 30} = \begin{bmatrix} H_{15 \times 15} & 0 \\ 0 & H_{15 \times 15} \end{bmatrix} + H_{so}$$

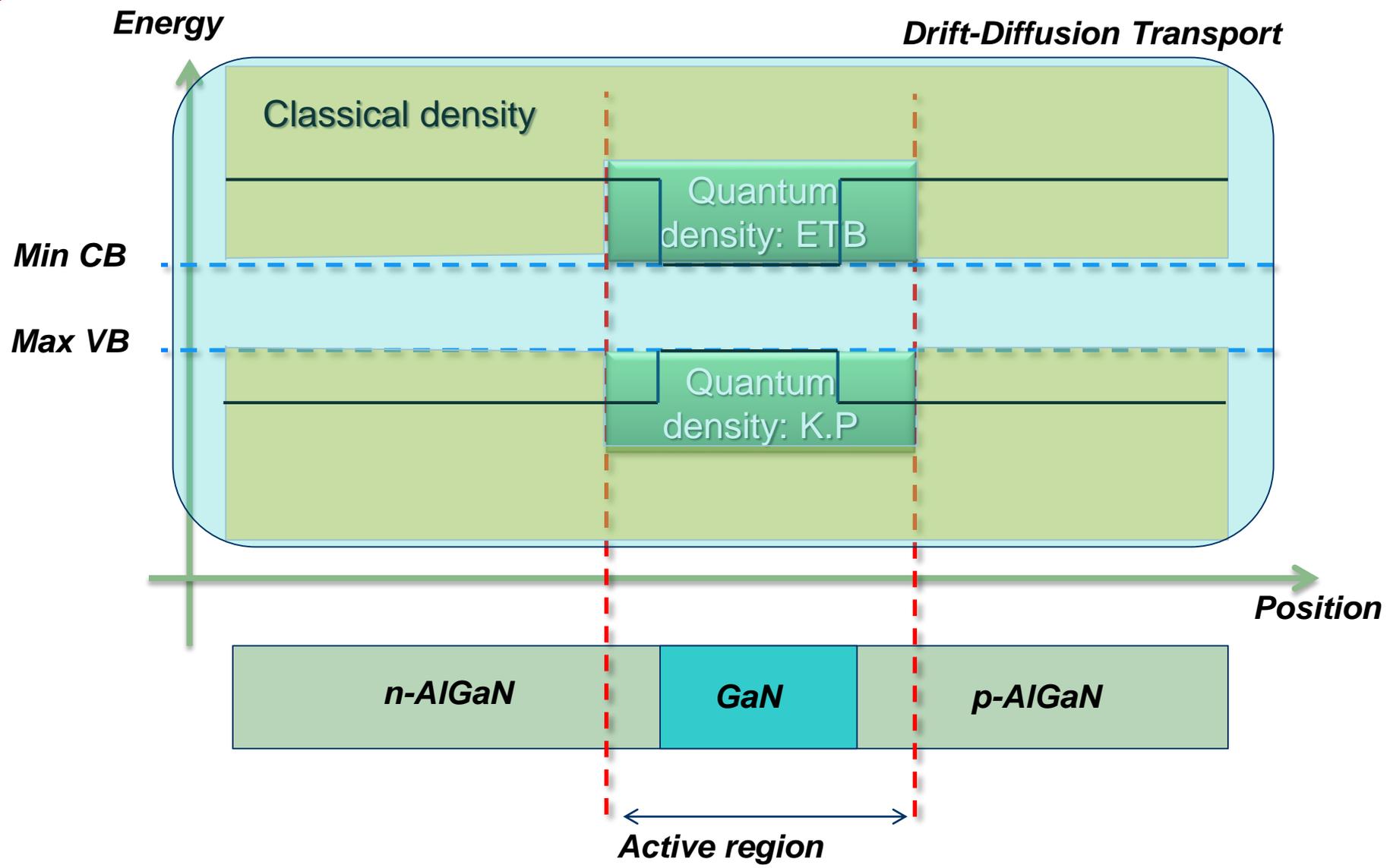
Cardona-Pollak (1966)
G. Fishman (2004)

$$H_{14 \times 14}, H_{20 \times 20}, H_{24 \times 24}$$

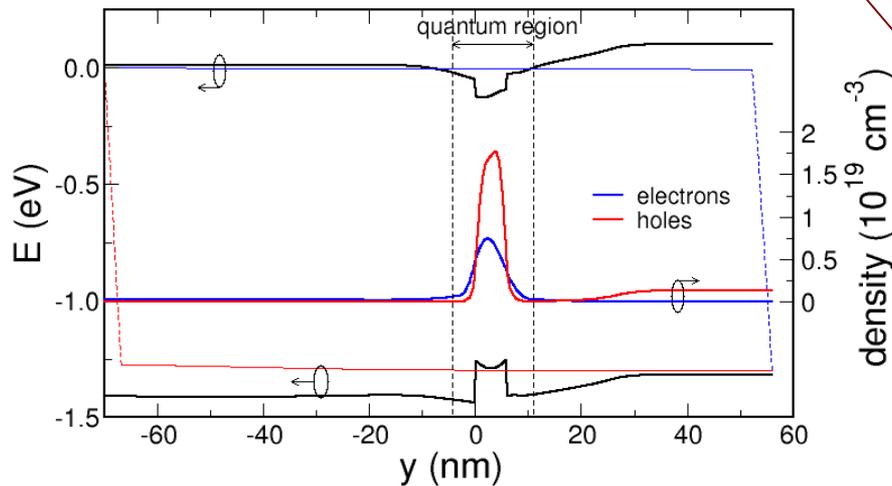
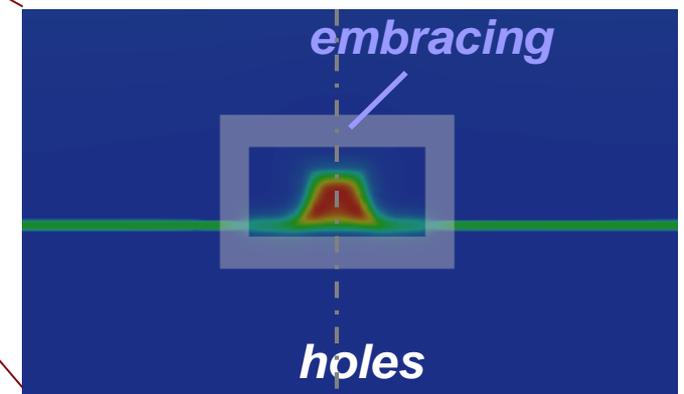
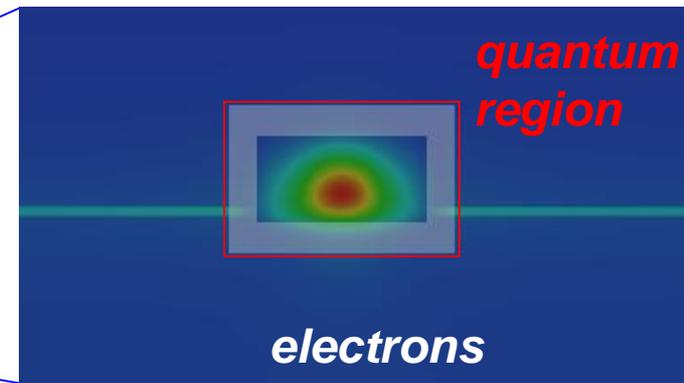
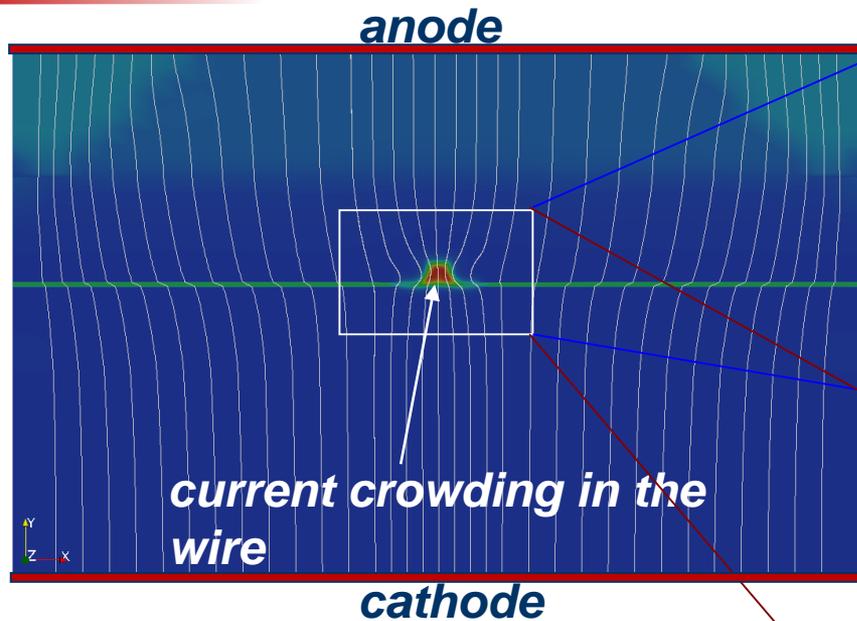


M. Buda et. al., IEEE Journal of Quantum Electronics, 2003





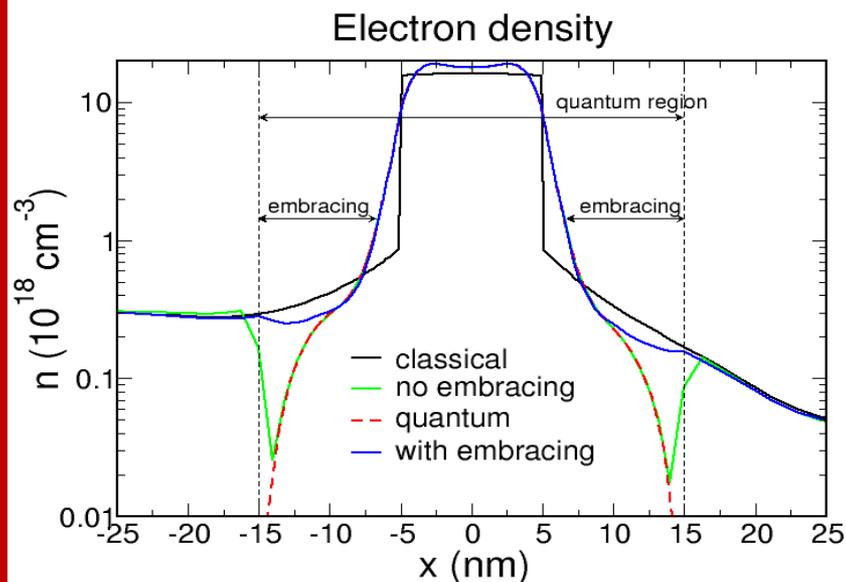
InGaAs Quantum wire: overlap scheme



Self-consistent densities at $V_b = 1.3$ V

K.P quantum model

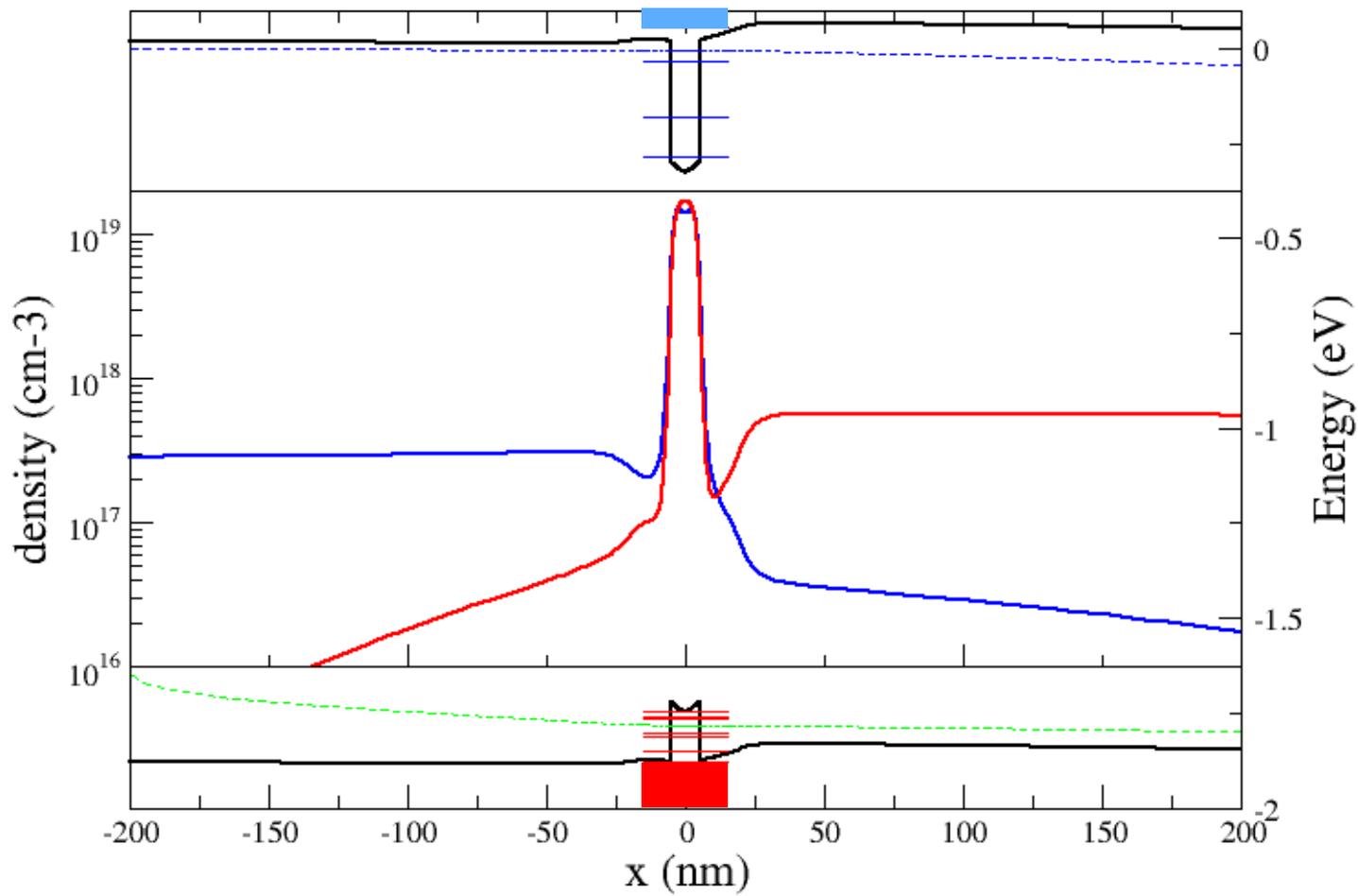
TiberCAD includes a technique for mixing classical and quantum density, acting as a quantum correction to drift-diffusion calculation



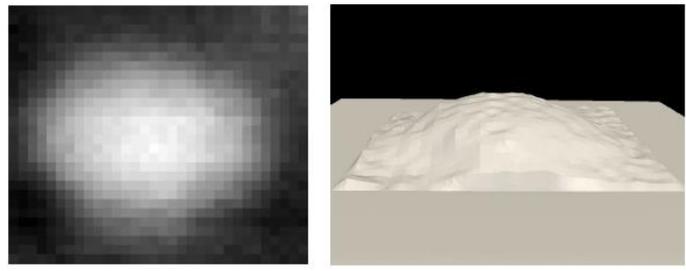
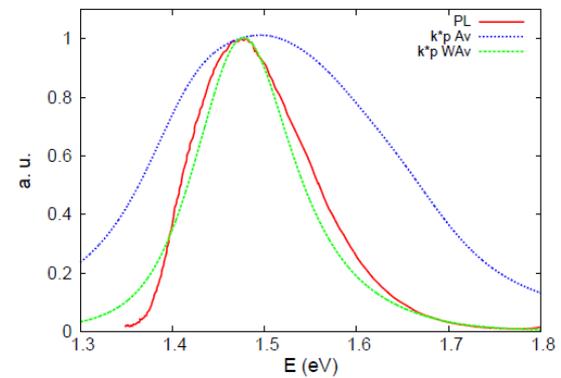
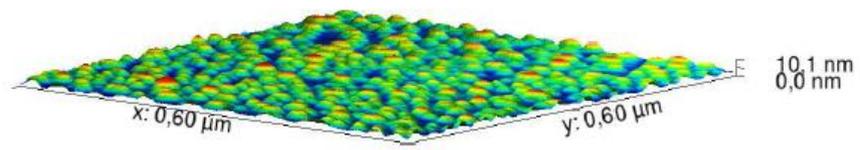
Embracing region where **classical** and **quantum** charge are mixed.



The mixing parameter is solution of a Laplace equation with Dirichlet boundary conditions 0.0 and 1.0

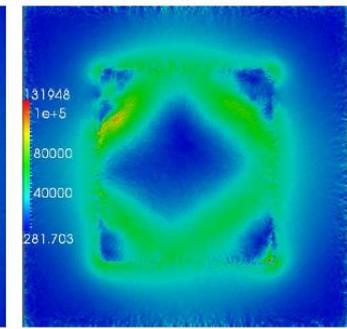
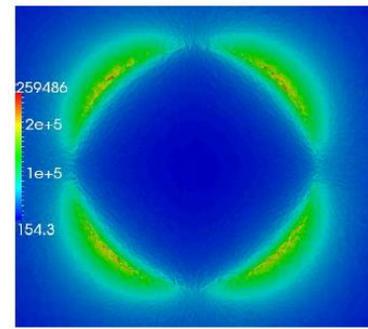


AFM image:

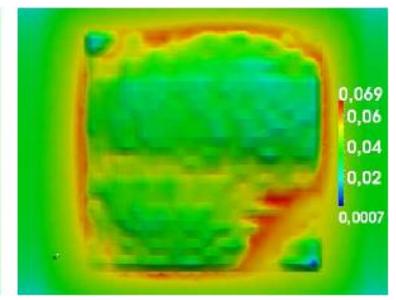
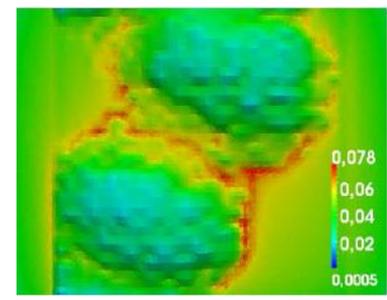
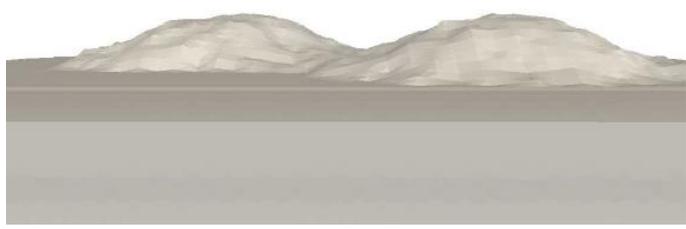


Idealized dot

Realistic dot

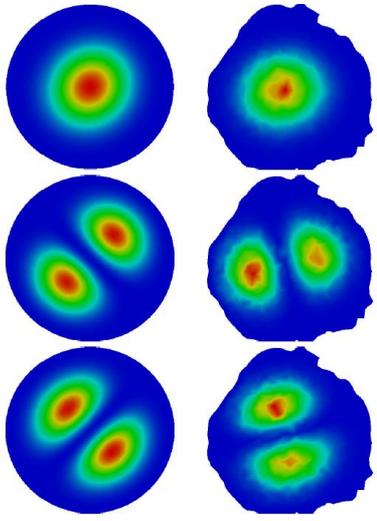


Strain field maps

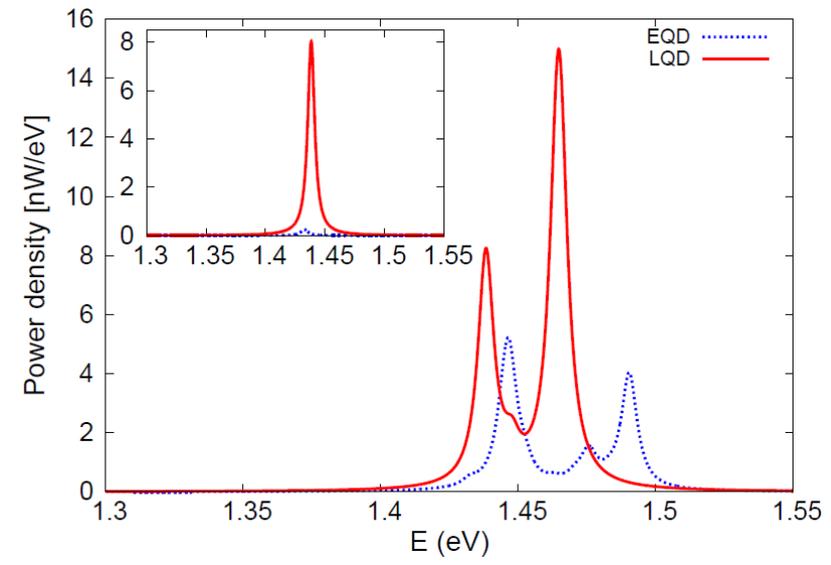
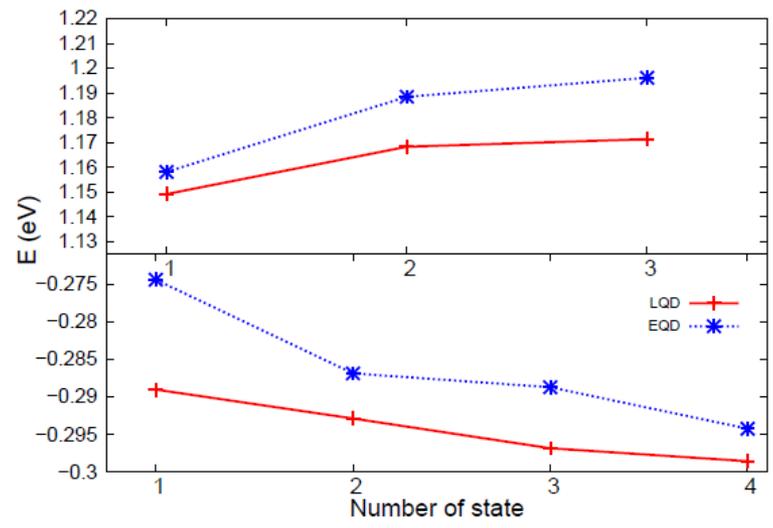
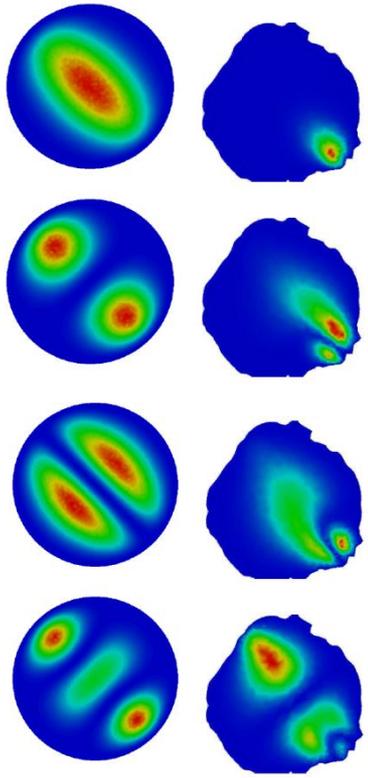


Closely coupled dots

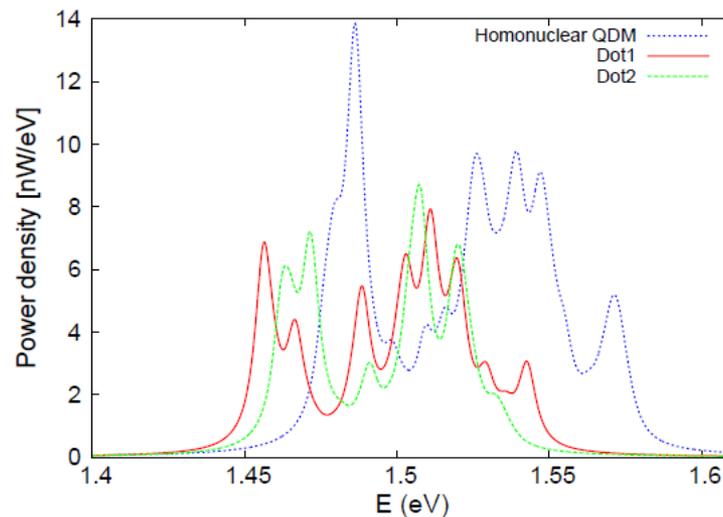
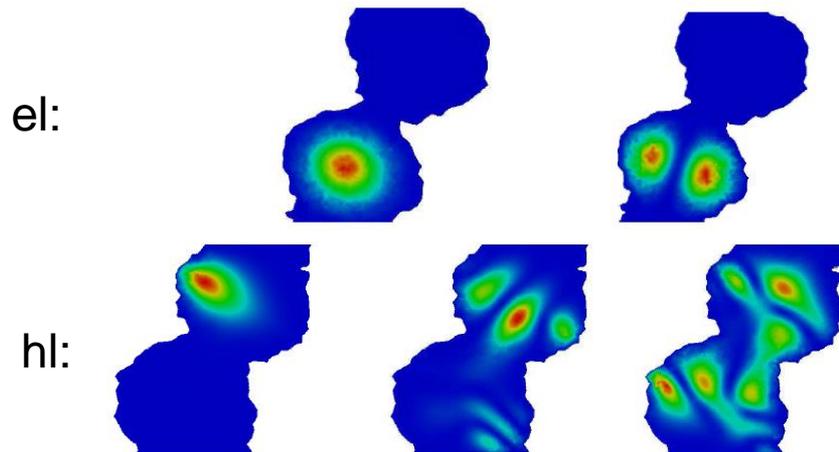
Electron states



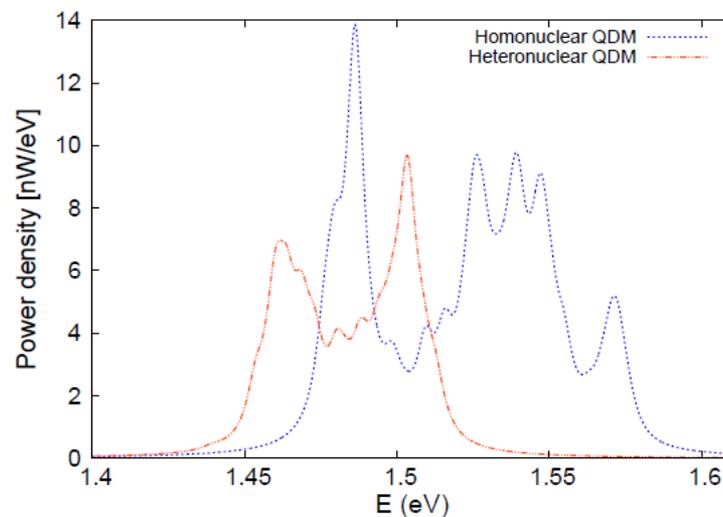
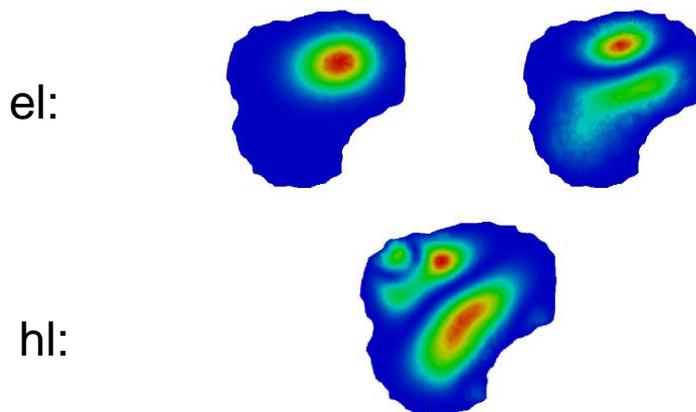
Hole states



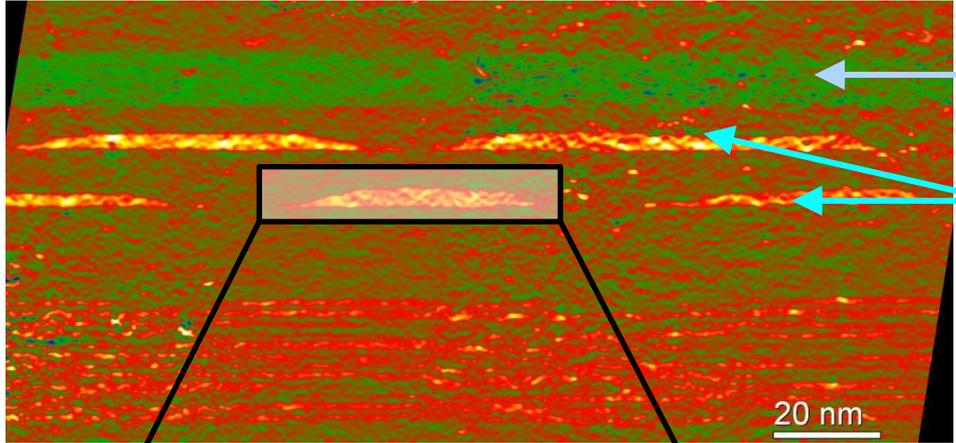
homo-nuclear dots



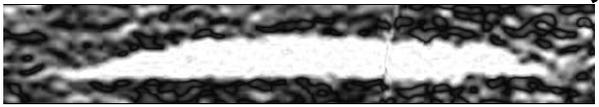
hetero-nuclear dots



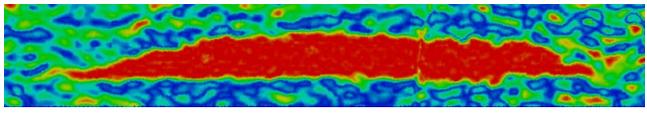
Shape and alloy effects in Qdot system



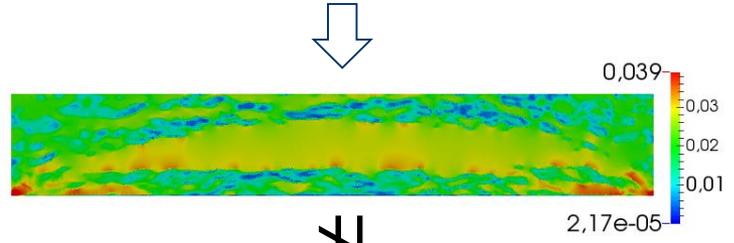
TEM image (In comp.)



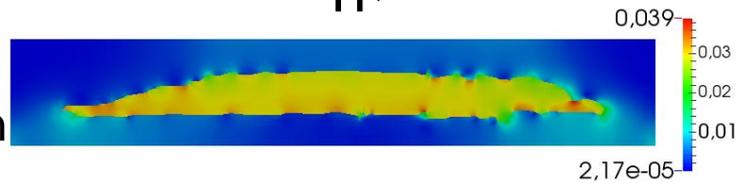
Imported alloy concentration



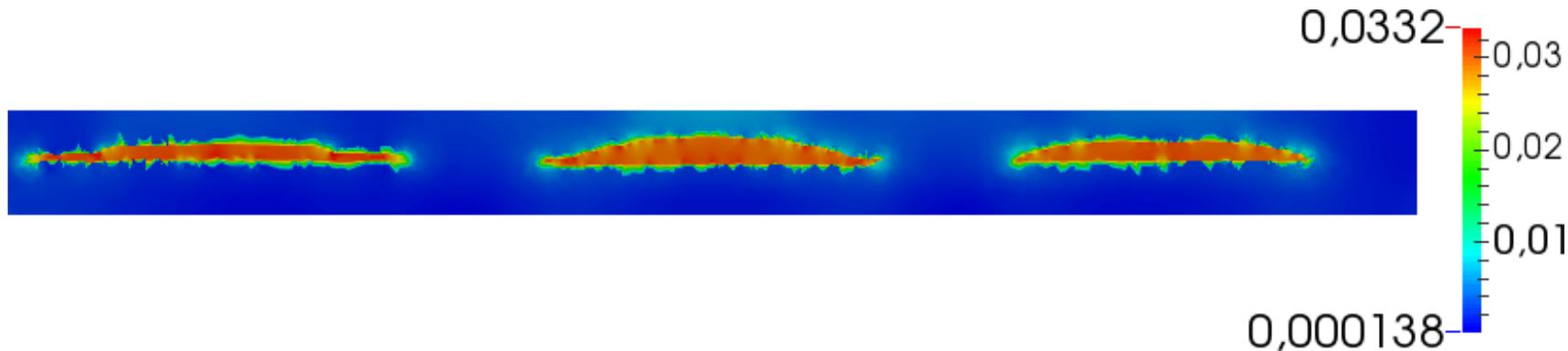
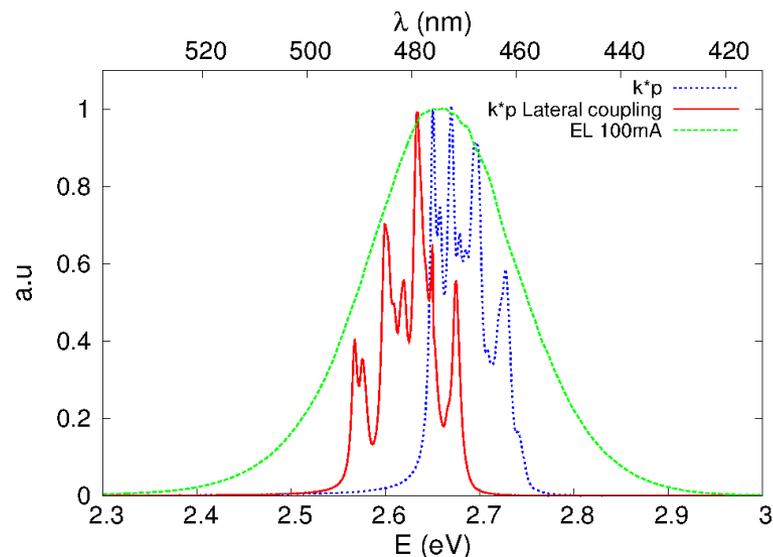
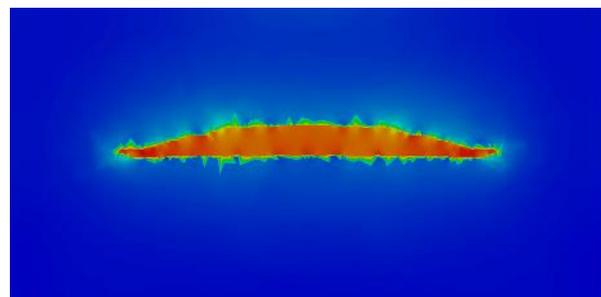
Strain profile



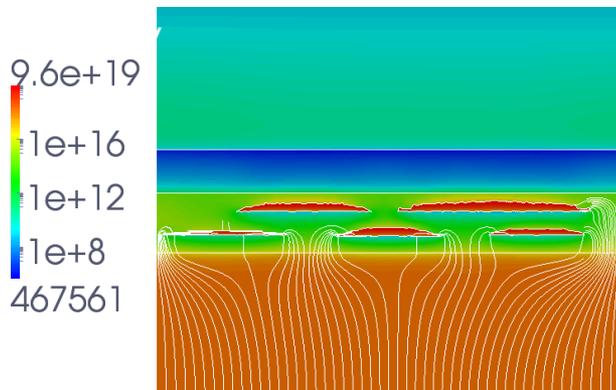
Constant In concentration



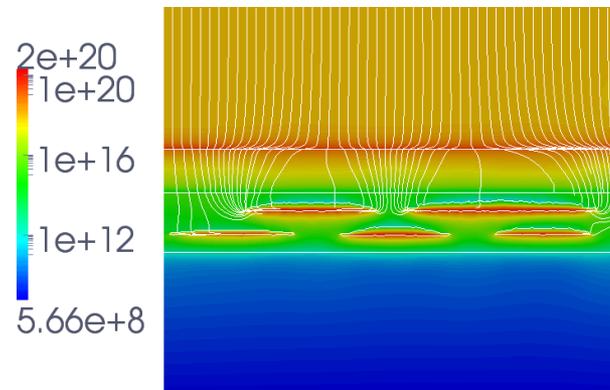
Impact of **lateral** coupling given mainly by strain field (continuum and k^*p 3D model): **shift** of the spectrum of the central dot of about **90meV**



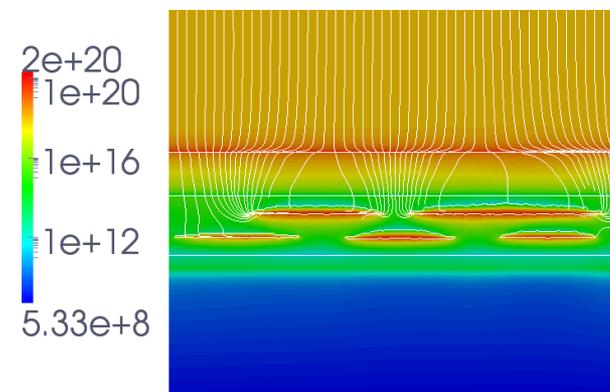
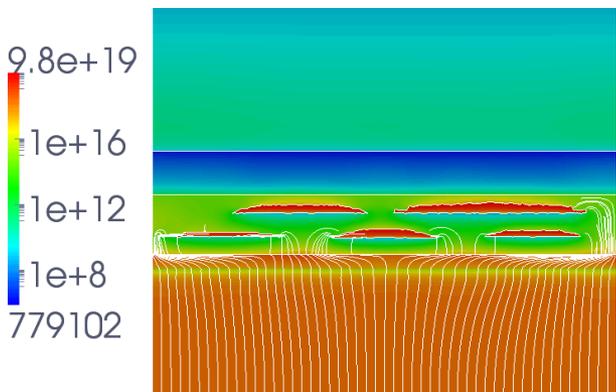
electron current density



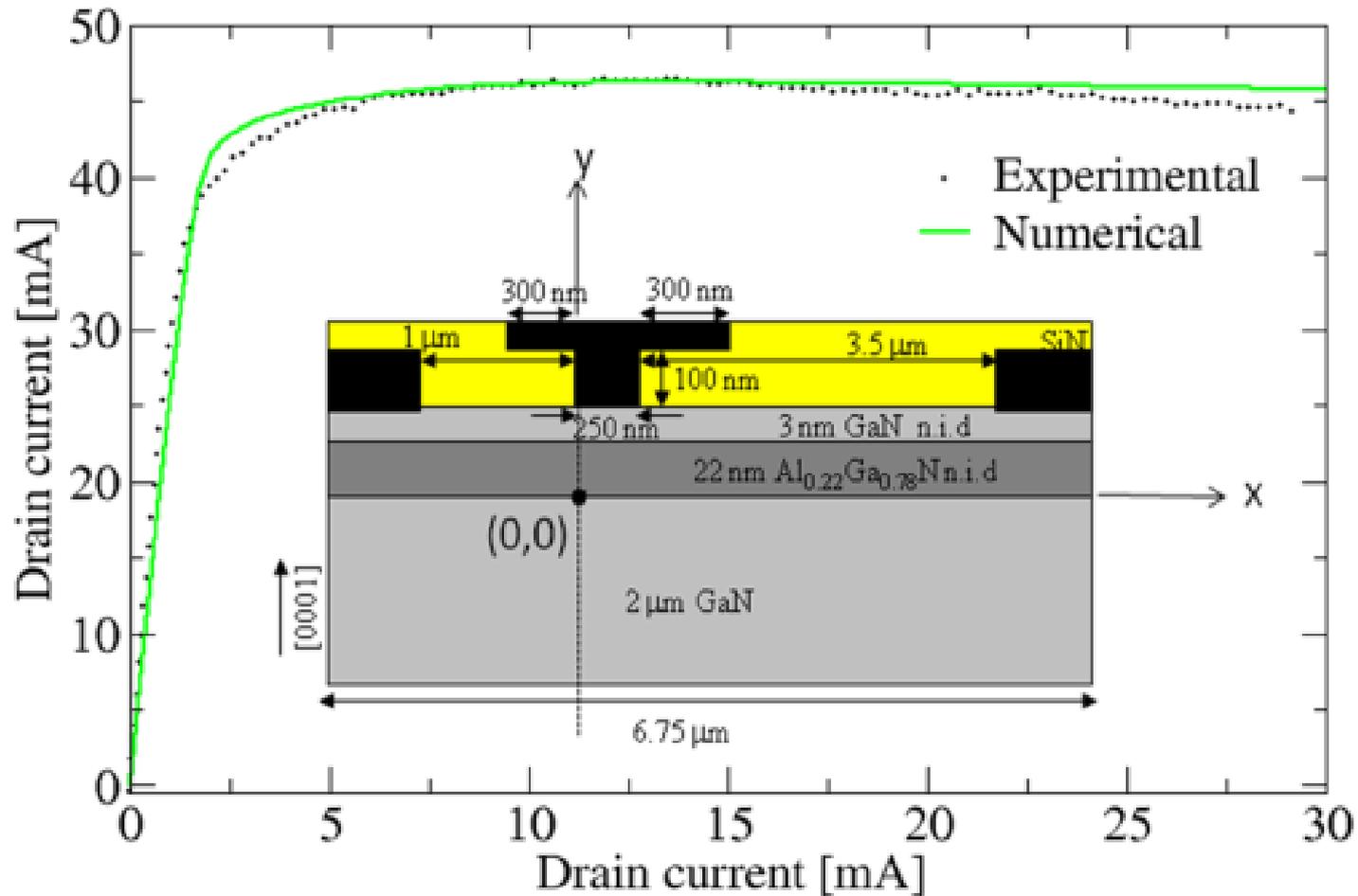
Hole current density



Increasing electron current density with electron-rich layer



Bridge Multiscale



Fourier Heat Diffusion: $-\nabla \cdot (\kappa \nabla T) = H$

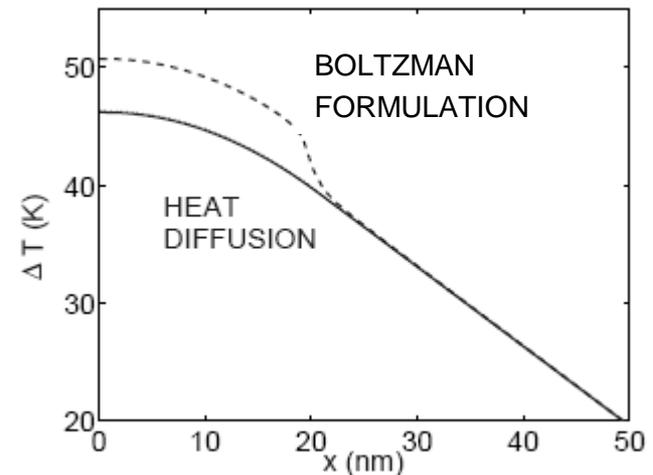
Energy Moment of the Boltzman Transport Equation for phonons

$$\frac{\partial e''}{\partial t} + \mathbf{v} \cdot \nabla e'' = -\frac{e'' - e^0}{\tau}$$

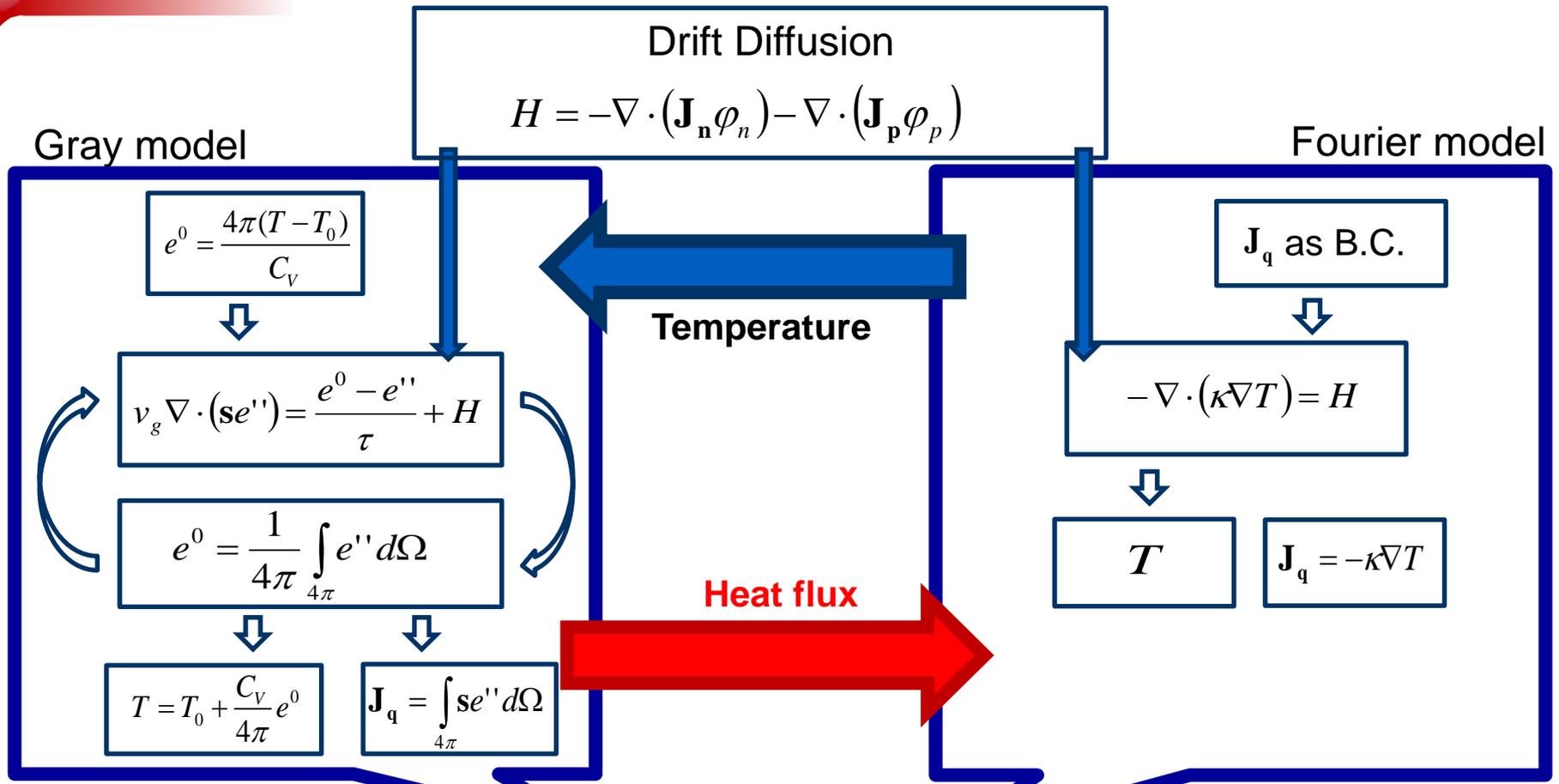
$$e'' = \int \hbar \omega [N - \bar{N}(T_{ref})] g(\omega) d\omega$$

A gray model assume isotropic and constant phonon velocity:

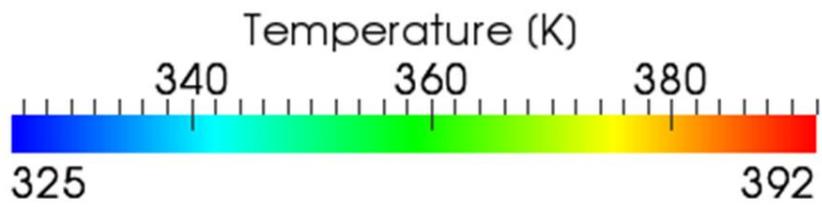
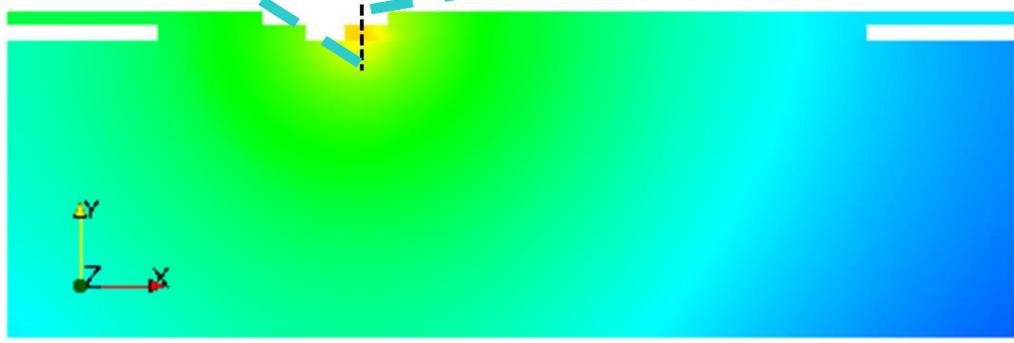
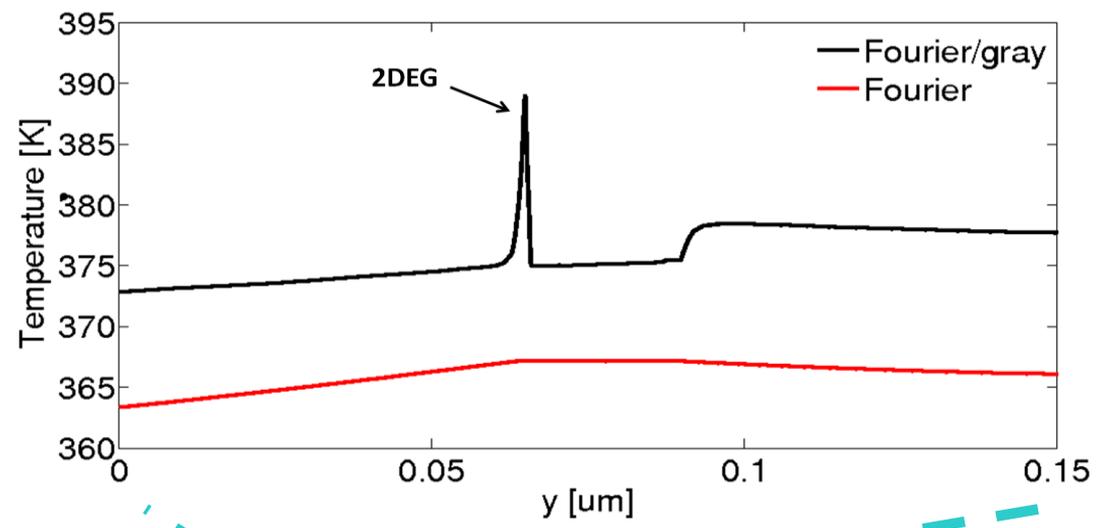
$$\frac{\partial e''}{\partial t} + v_g \nabla \cdot \mathbf{s} e'' = -\frac{e'' - e^0}{\tau}$$



Fourier/Gray bridge method



$$R_T = 0.8 \text{ mWcm}^2/\text{K}$$



Special self-consistence scheme

```
Module selfconsistent
{
  solve = (fourier, gray)

  Multiscale bridge {
    macromodel = fourier
    micromodel = gray
    restrict_variables = (temperature)
  }
  max_iterations = 10
  absolute_tolerance = 1e-3
  relative_tolerance = 1e-9
}
```

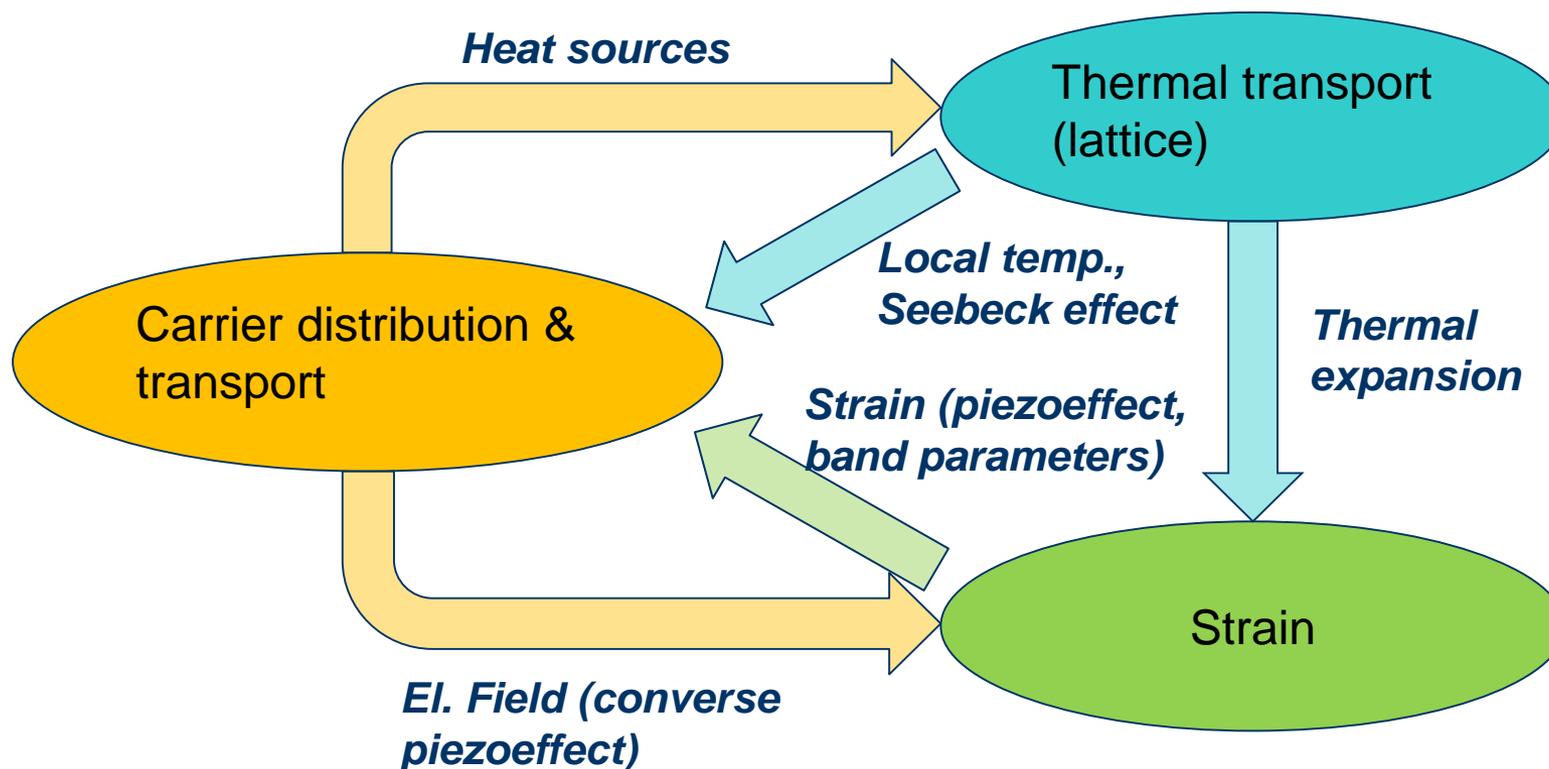
macromodel
is solved everywhere

micromodel is solved

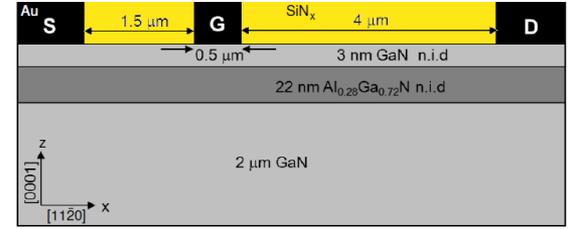
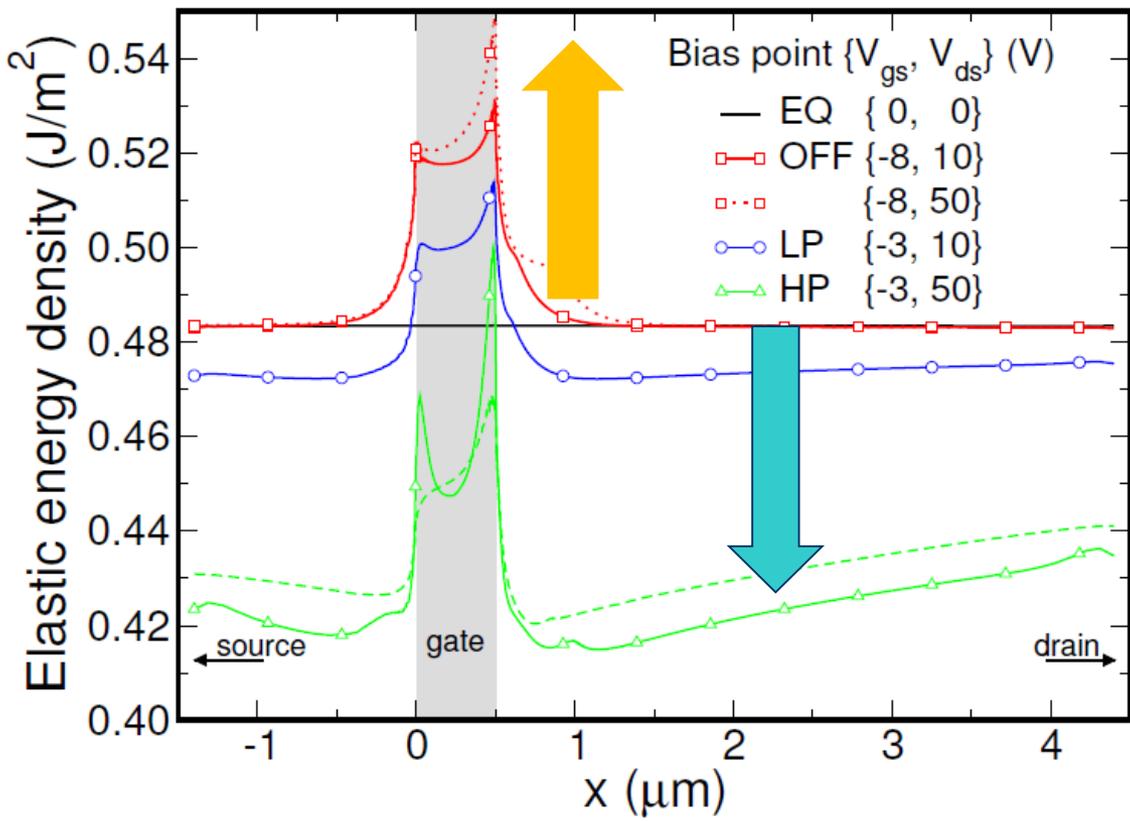
macromodel is solved
temperature is not solved
on $\text{fourier} \cap \text{gray}$

Electro-thermal and Strain

- How does mechanical stress in a HEMT depend on operating conditions?
- Electrical, thermal and mechanical device behavior are interconnected:



Mechanical energy density, integrated along [0001]:



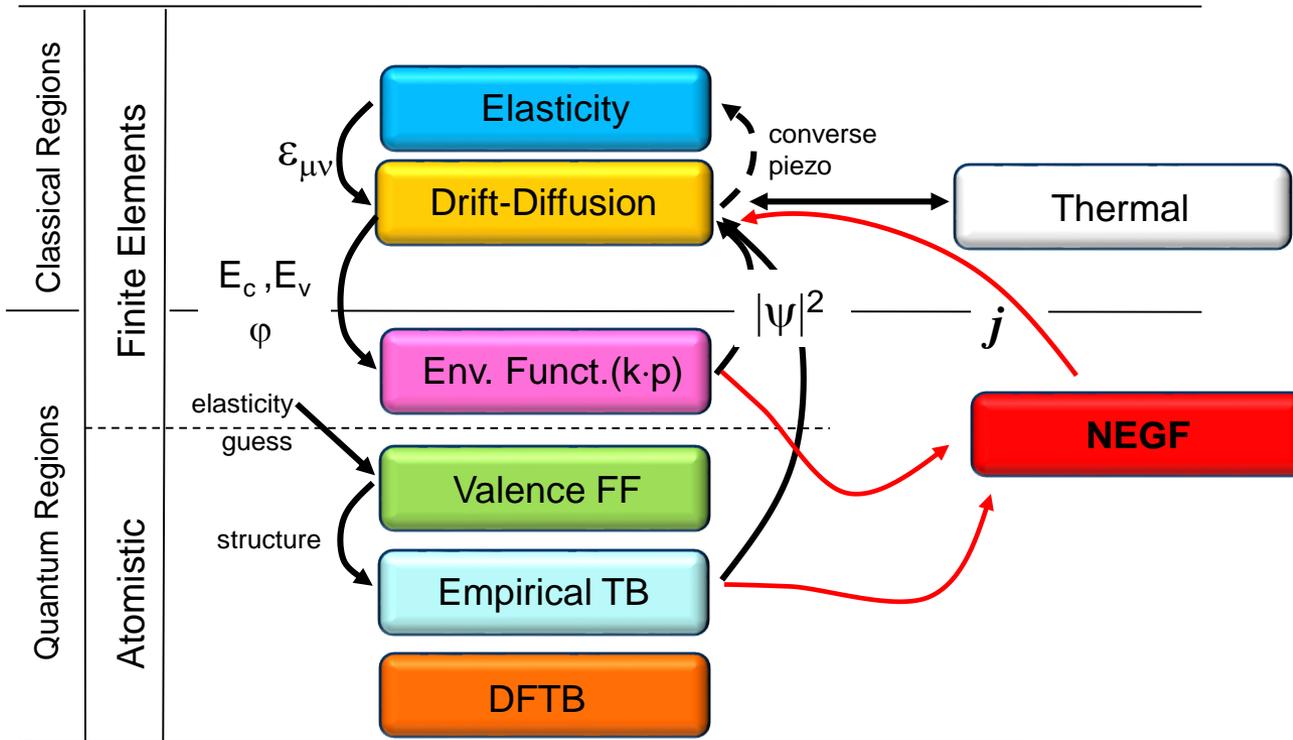
- Converse piezoelectric effect increases locally mechanical stress
- Self-heating decreases overall mechanical stress

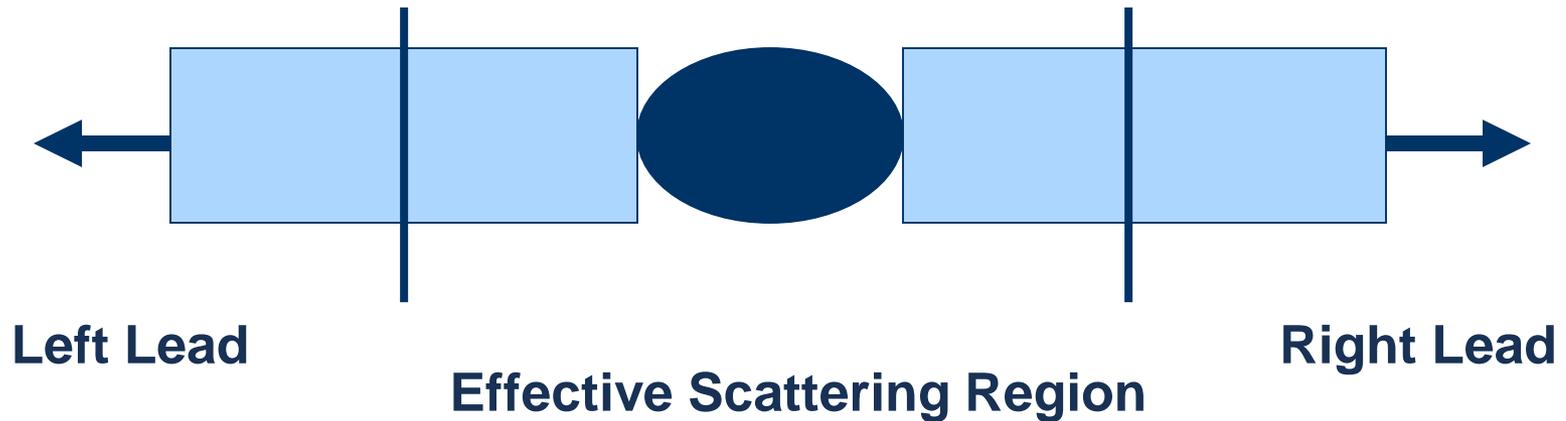
Critical planar energy densities are given in the range of 0.49 ~ 0.7 J/m²

Joh et al. Microelectronics Reliability, 50, 767, 2010

J. Floro et al. J. Appl. Phys., 96, 7087, 2004

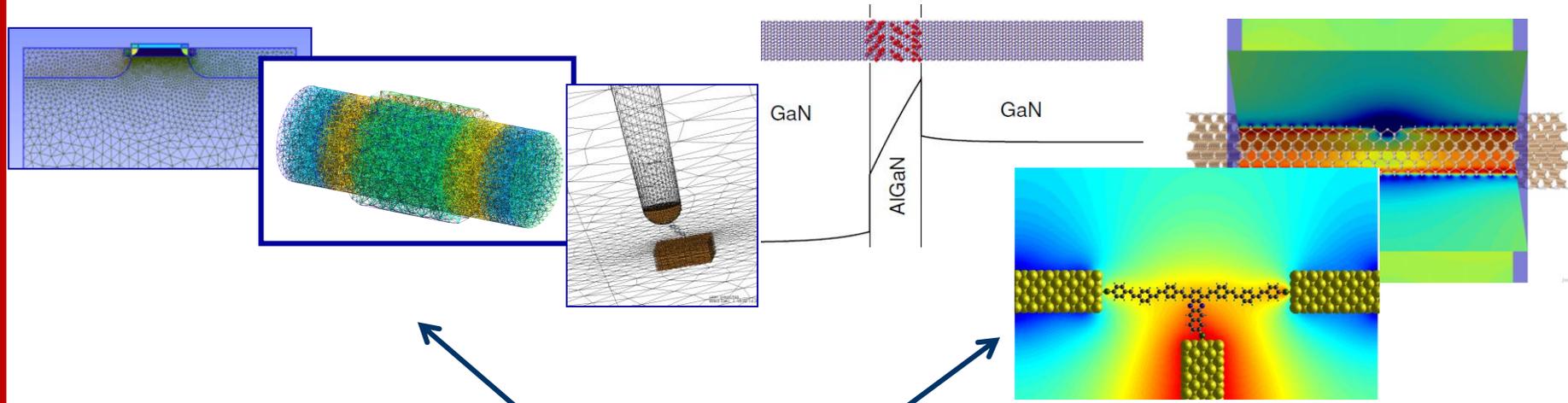
Quantum Transport: NEGF





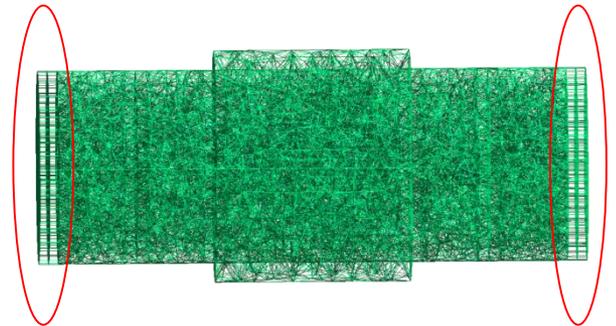
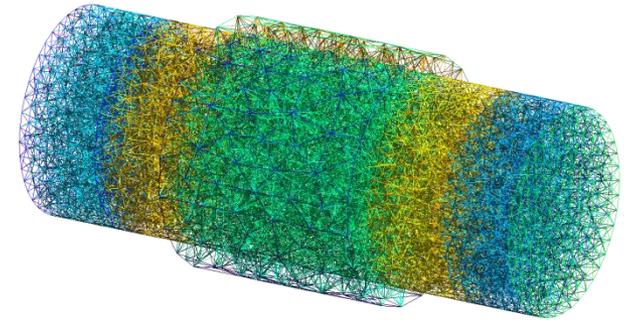
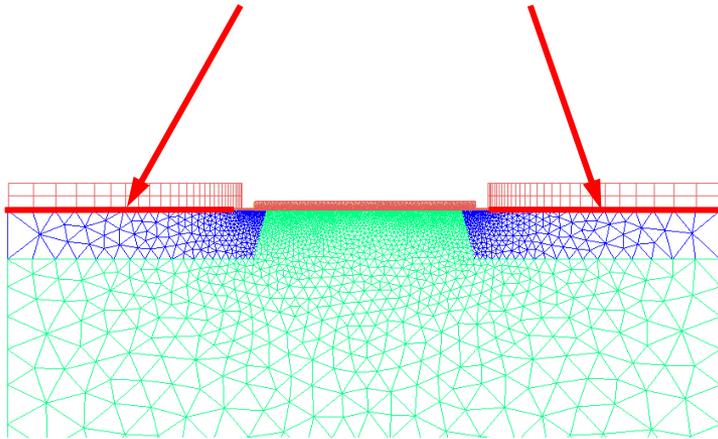
$$[E - H + \Sigma^r(E)]G^r(E) = \mathbf{I}$$

$$D(\mathbf{r}, E) = 2i \operatorname{Im} G^r(\mathbf{r}, \mathbf{r}, E)$$

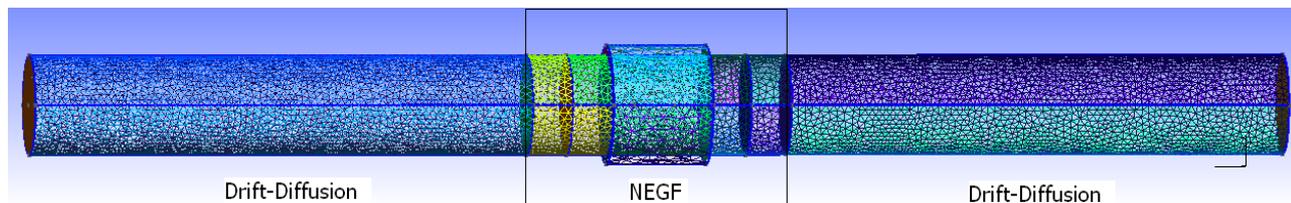


libNEGF

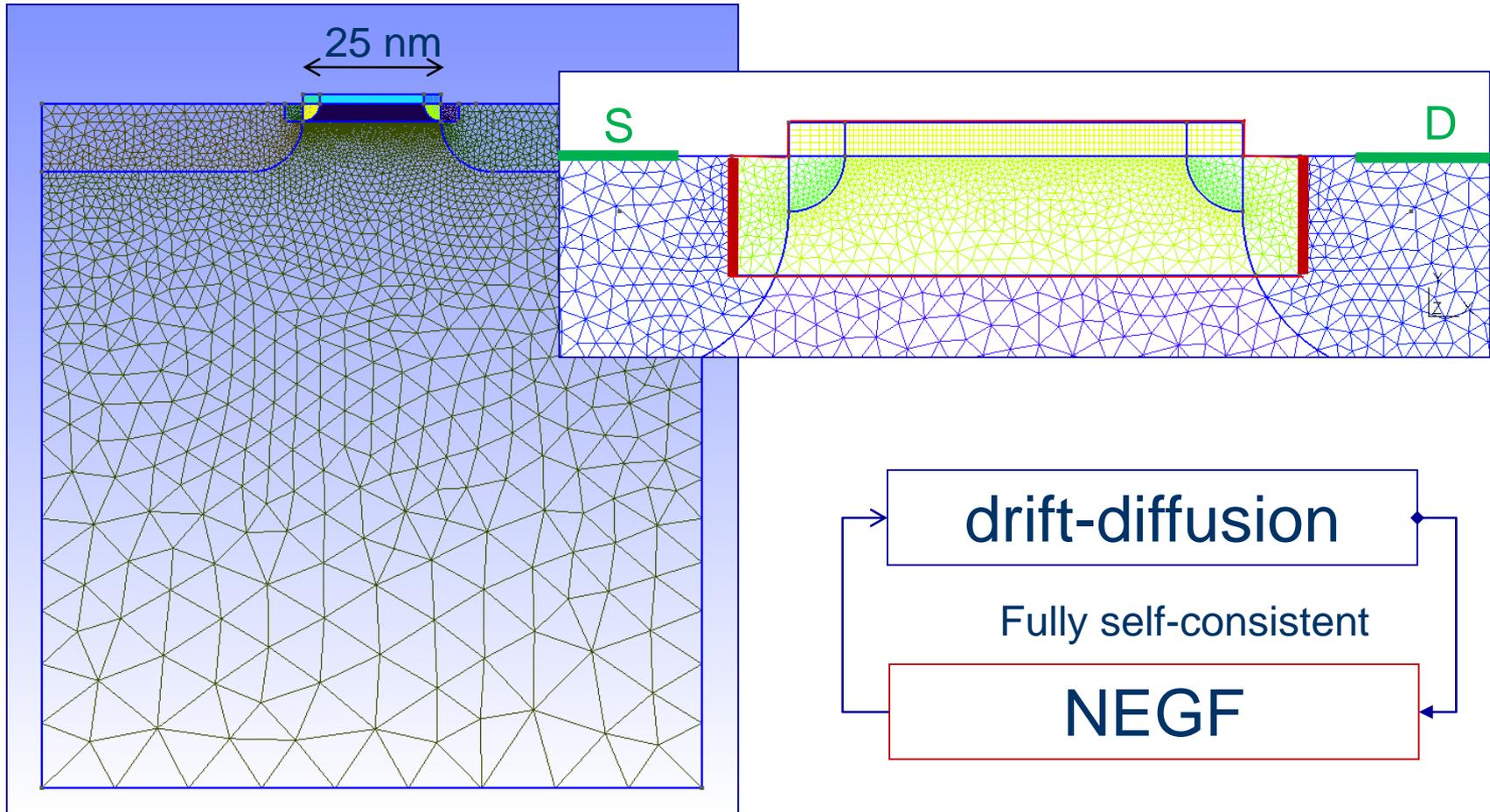
N-1 dimensional Contacts

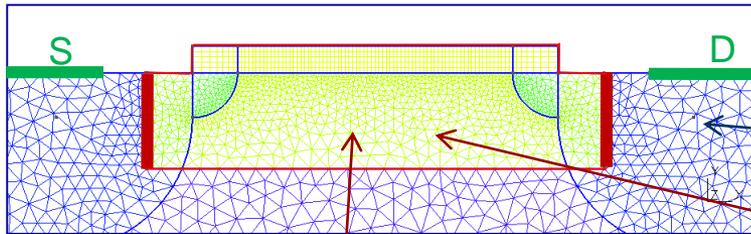


- Automatic mesh creation using *libMESH* classes
- General extrusion of planar contacts in 1,2,3D



Mix between overlap (Schrödinger/Poisson) and bridge (current at NEGF boundary) schemes





$$\begin{cases} \mathbf{J}_n = en\mu_n\mathbf{F} + eD_n\nabla n \\ \nabla \cdot \mathbf{J}_n = e(R - G) \\ \nabla \cdot (\epsilon_0\epsilon_r\nabla V) = e(n - N_D) \end{cases}$$

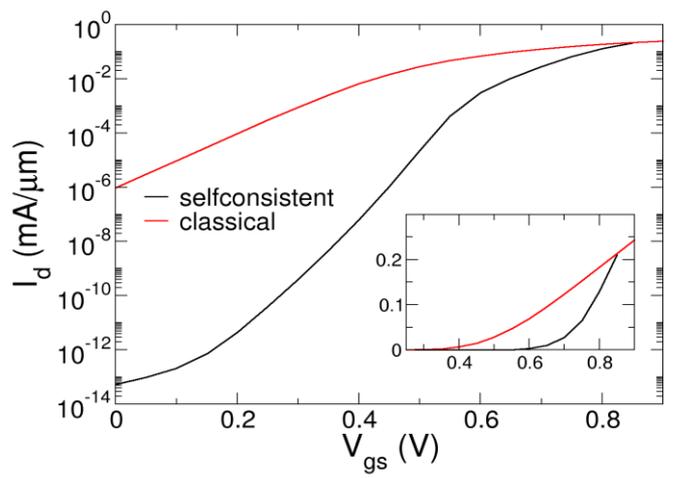
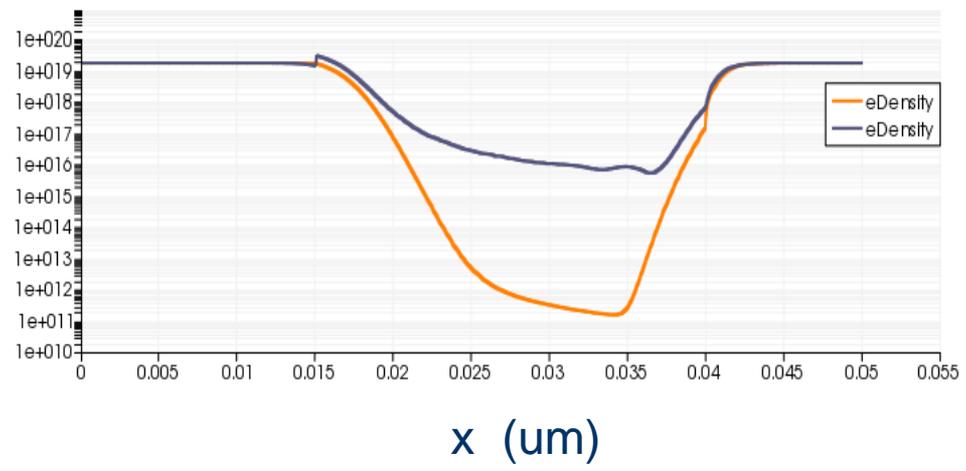
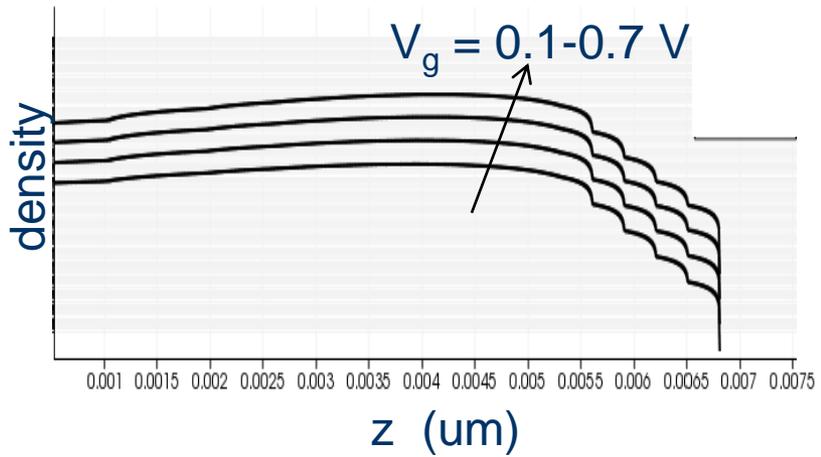
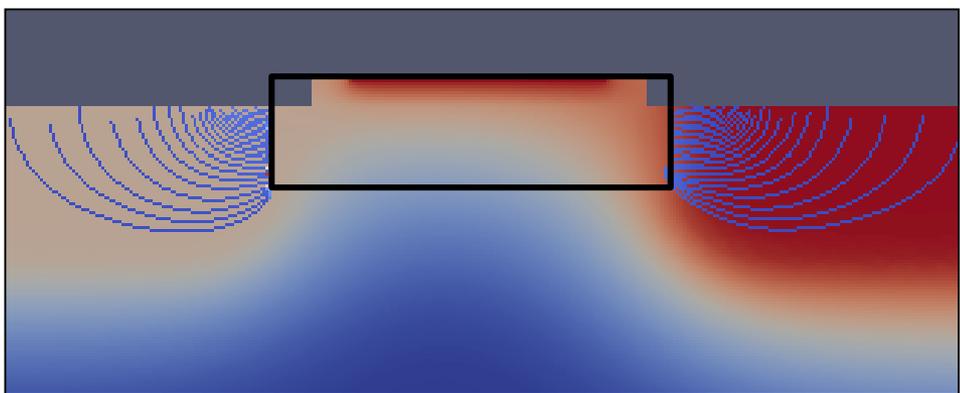
```
Module negf{
  regions = channel
  Physics{
    Hamiltonian efa {}
  }
}
```

In negf regions, solve only for electrostatic potential, (not for electron current)

```
Module selfconsistent
{
  solve = (negf, driftdiffusion)

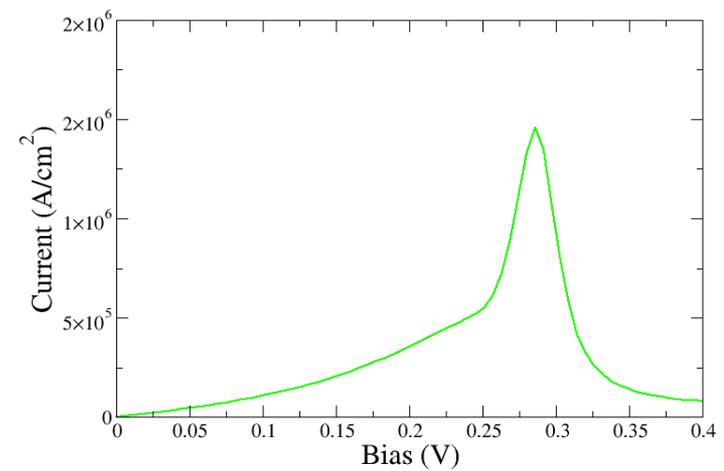
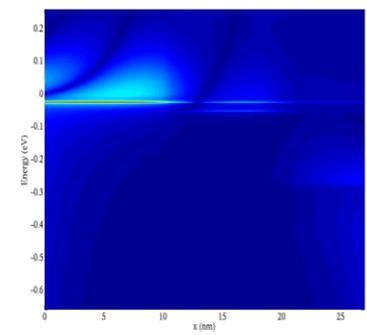
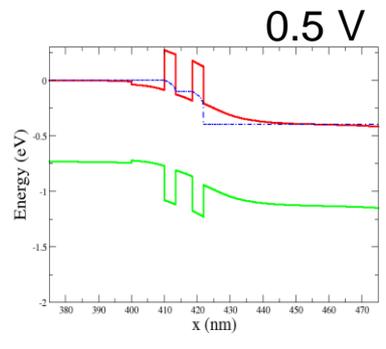
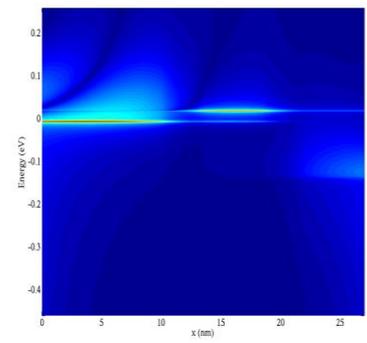
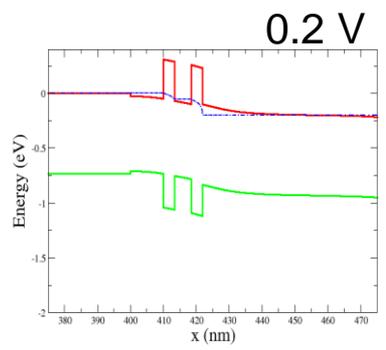
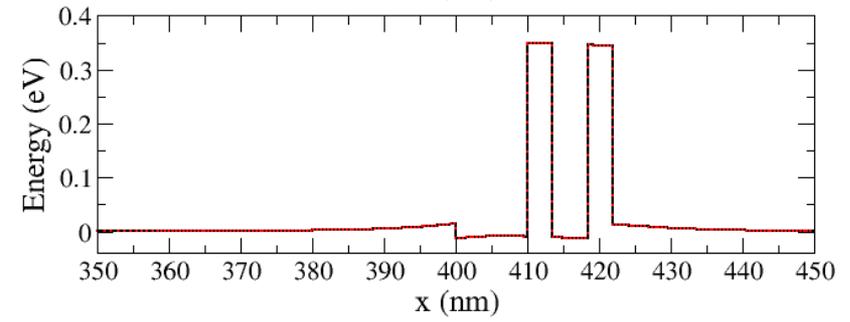
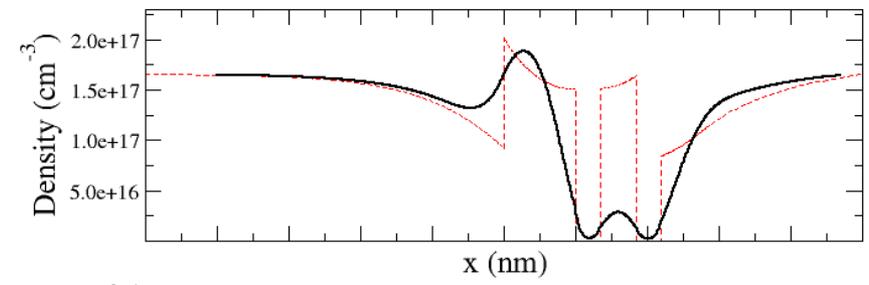
  Multiscale bridge {
    macromodel = driftdiffusion
    micromodel = negf
    restrict_variables = (fermi_e)
  }

  max_iterations = 10
  absolute_tolerance = 1e-3
  relative_tolerance = 1e-9
}
```

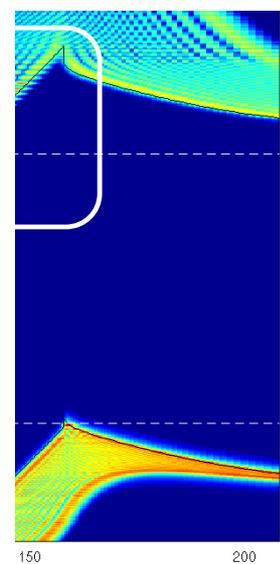
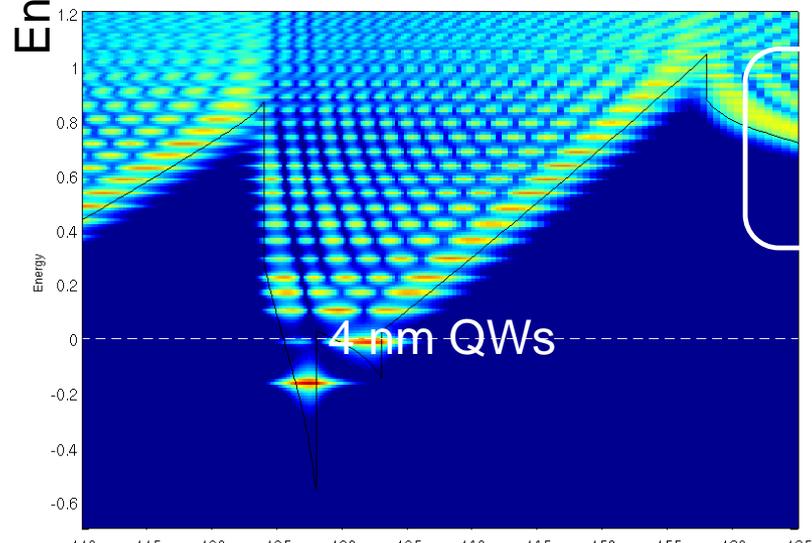
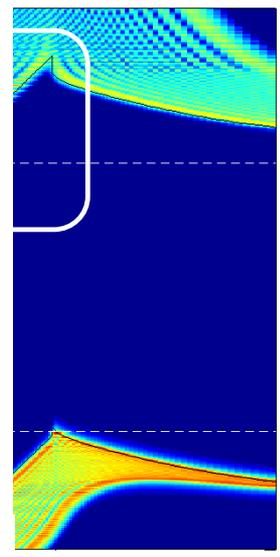
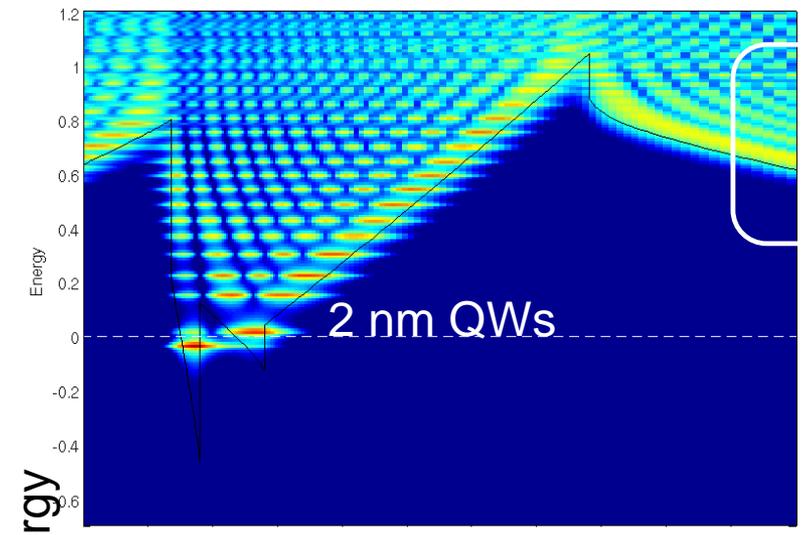


RTD structure

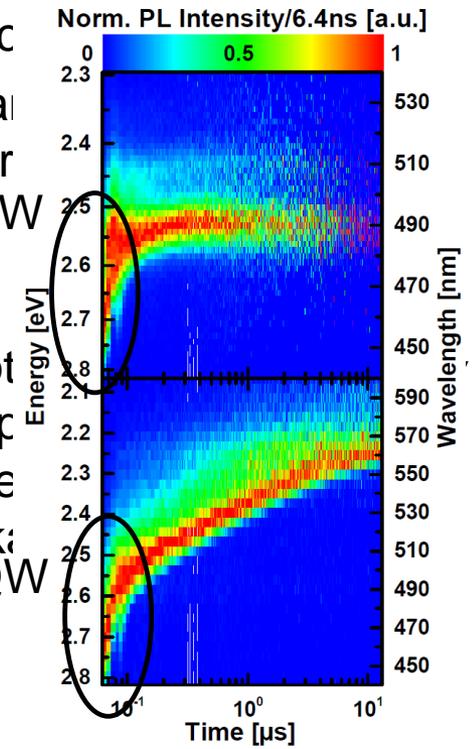
500A	n+	In _{0.53} Ga _{0.47} As	Contact
500A	n	In _{0.53} Ga _{0.47} As	Emitter
50A	i	In _{0.53} Ga _{0.47} As	Spacer
35A	i	In _{0.7} Ga _{0.3} P	Barrier
50A	i	In _{0.6} Ga _{0.4} As	Strained well
35A	i	In _{0.7} Ga _{0.3} P	Barrier
100A	i	In _{0.6} Ga _{0.4} As	Strained layer
1000A	i	In _{0.53} Ga _{0.47} As	Collector
3000A	n+	In _{0.53} Ga _{0.47} As	Contact
S.I.-InP substrate			



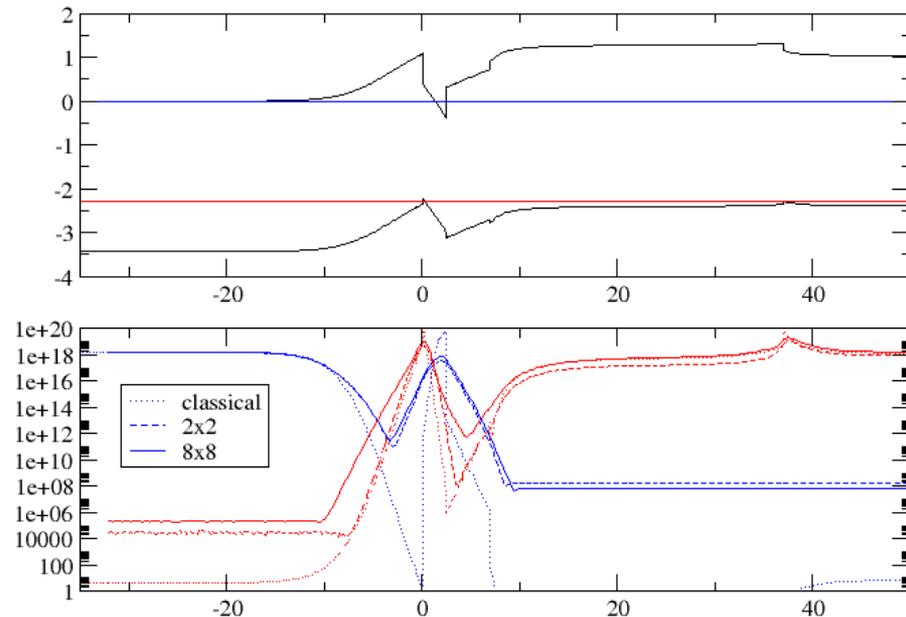
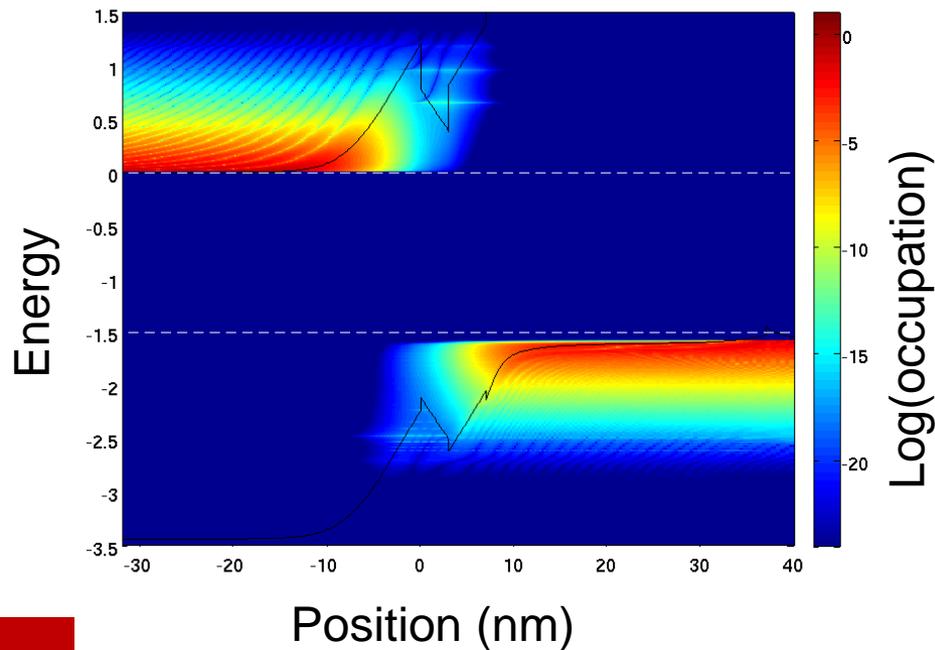
- Here we use (NE)GF to calculate the LDOS, on top of a DD simulation (no self-consistency)



- NEGF based LDOS give more insight into spatio-spec
- «sta
- appr
- 2 nm QW
- Future:
- Phot
- coup
- asse
- leak;
- 4 nm QW

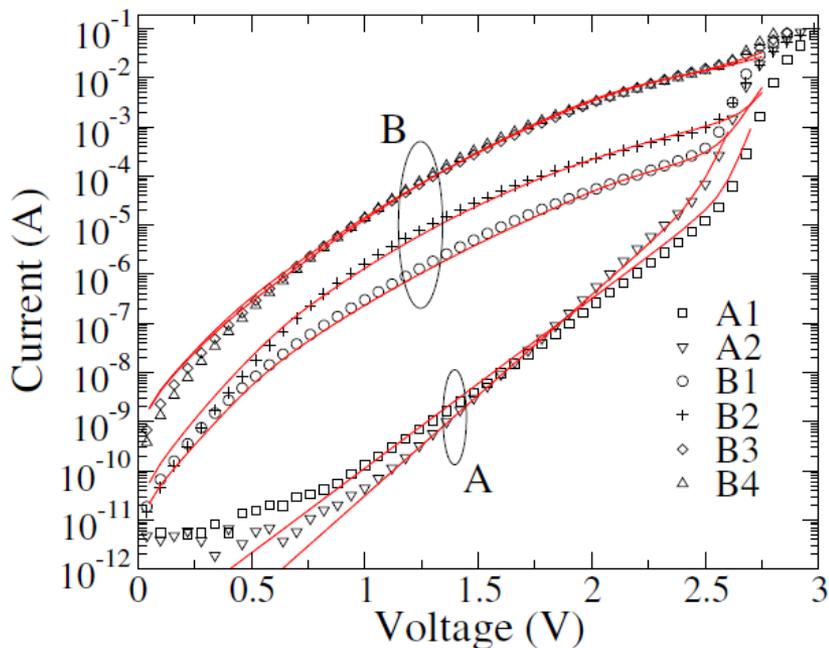


- Difficulties: separate n/p densities near equilibrium
- Below knee voltage the minority carrier densities become extremely low
- Reproduce non-radiative recombinations in NEGF (Auger, SRH)
- Introduce el- γ coupling in NEGF

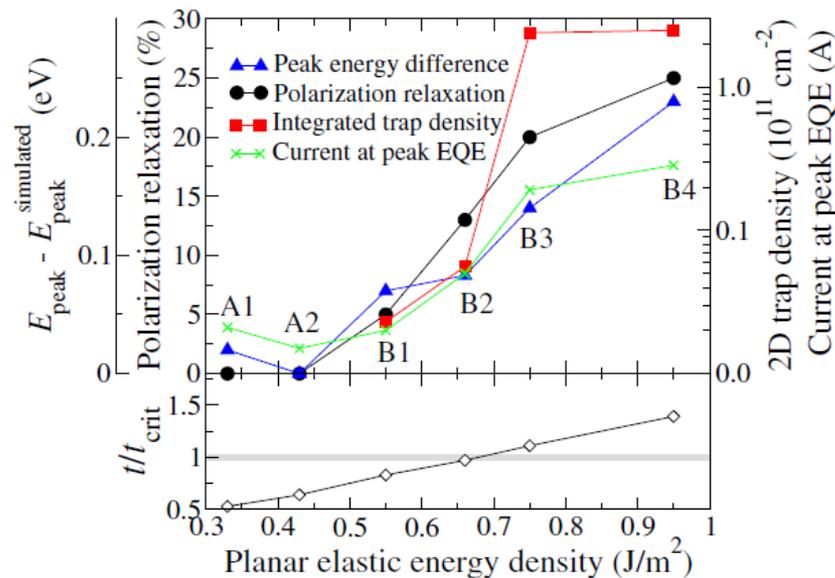
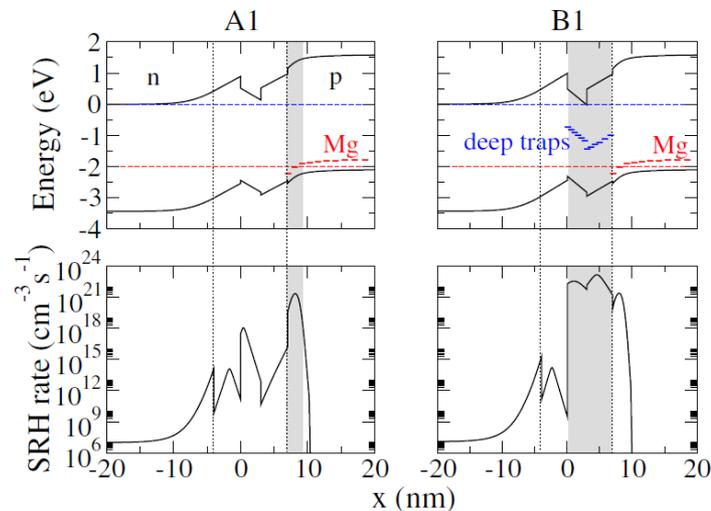


⇒ *work in progress*

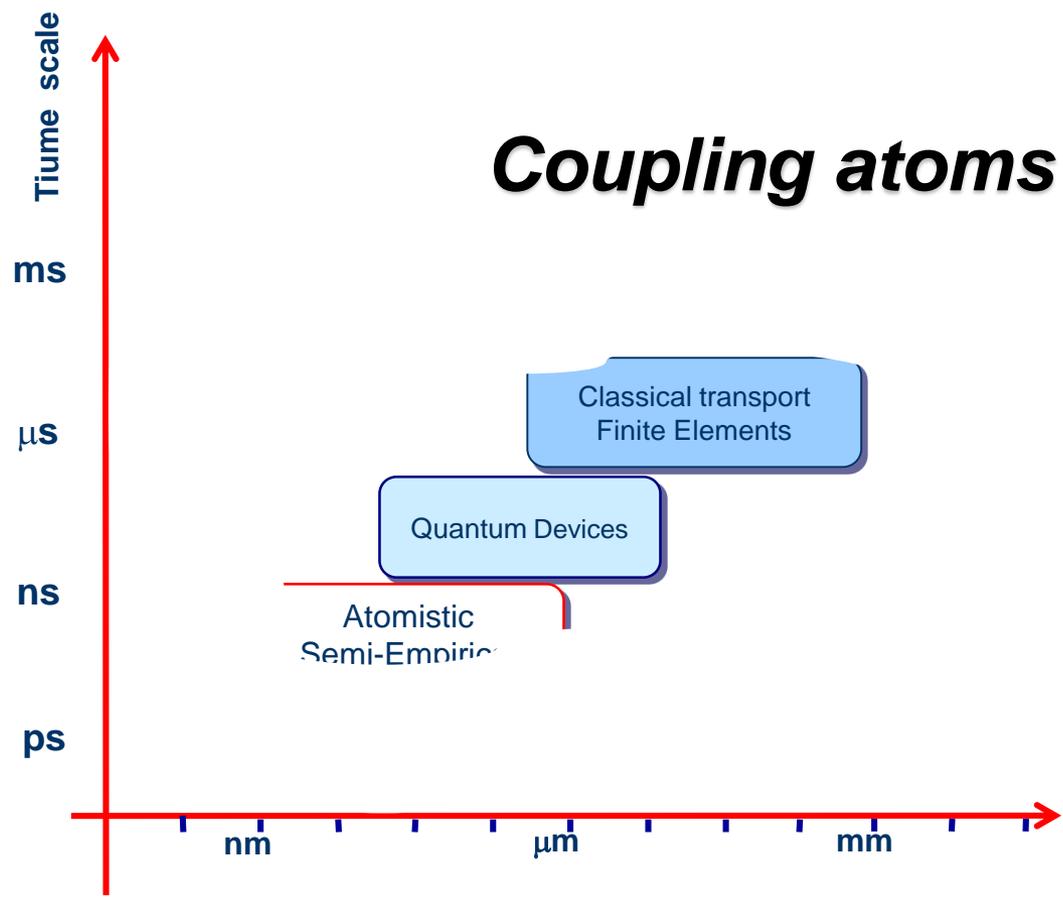
- Forward current at low injection, for different devices (different QW thickness, different In content)



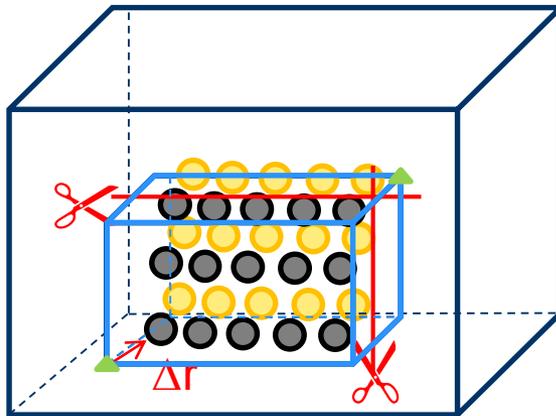
Correlation between fitting parameters and independent mechanical data



Coupling atoms with finite elements



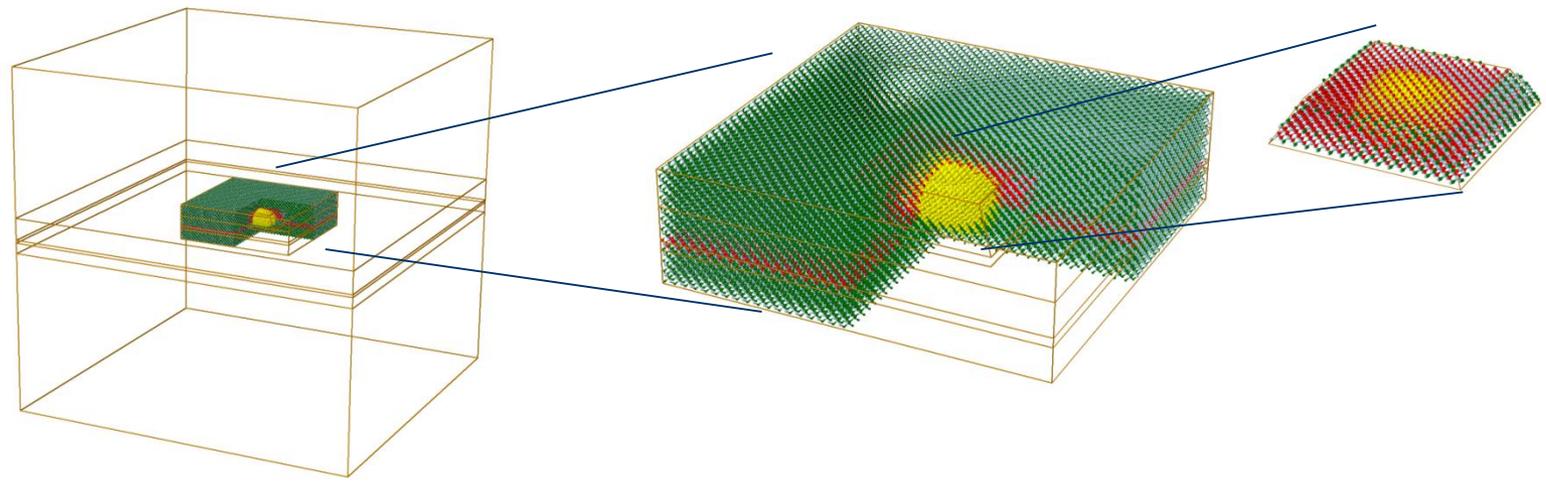
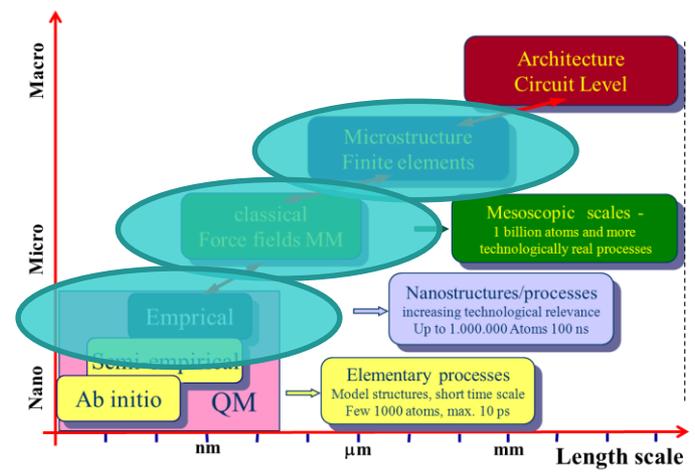
- We can assure a consistent atomistic structure using a top down approach:



1. Identify relevant volume
2. Shift origin slightly inside
3. Fill up with atoms using the crystal basis
4. Cut atoms outside of the structure

*It is important that all atoms are lying **inside** the simulation domain*

- we assume pseudomorphic structures with commensurate interfaces

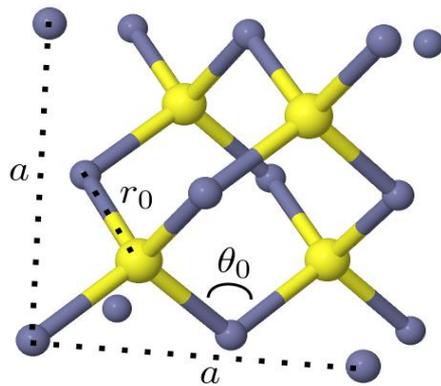


Drift-diffusion
Elasticity

Force Field

ETB

We included a Keating model to calculate strain at an atomistic level



$$U = \sum_i U_{i\alpha} + U_{i\beta}$$

$$U_{i\alpha} = \sum_j \frac{3\alpha_{ij}}{16r_{0ij}^2} \left(|\mathbf{r}_{ij}|^2 - r_{0ij} \right)^2$$

$$U_{i\beta} = \sum_j \sum_{k \neq j} \frac{3\beta_{ijk}}{8r_{0ij}r_{0ik}} \left(\mathbf{r}_{ij} \cdot \mathbf{r}_{ik} - r_{0ij}r_{0ik} \cos \theta_{0ijk} \right)^2$$

The equilibrium position is that one which minimizes U
 We use a nonlinear conjugate gradient minimization technique

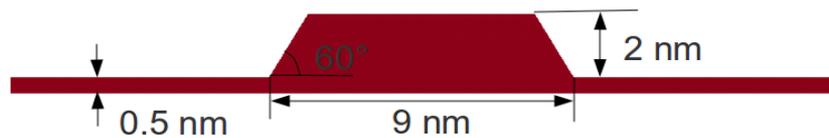
Keating (1966)

D. Camacho, Y. M. Niquet (2009)

Penazzi Gabriele, PhD. Thesis (2010)

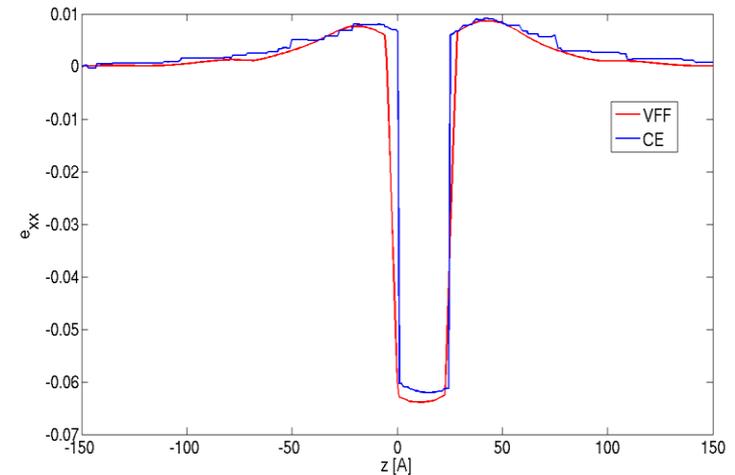
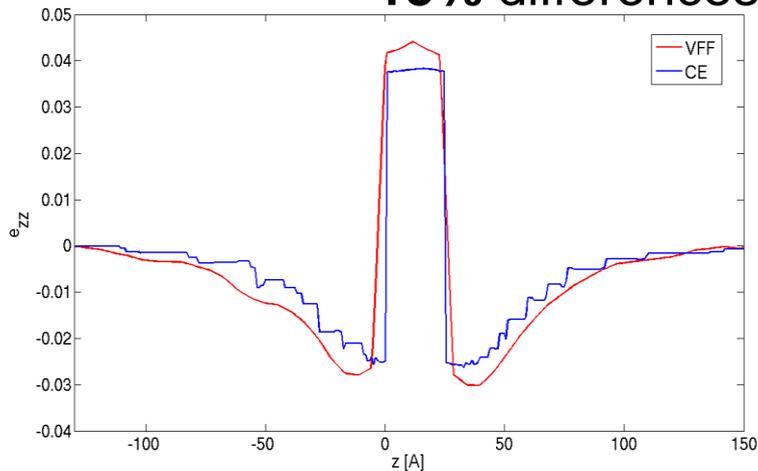
Evaluating when Continuum Elasticity failures is not trivial.
It depends on structure geometry. In general, it fails near interfaces

InAs quantum dot on GaAs
substrate

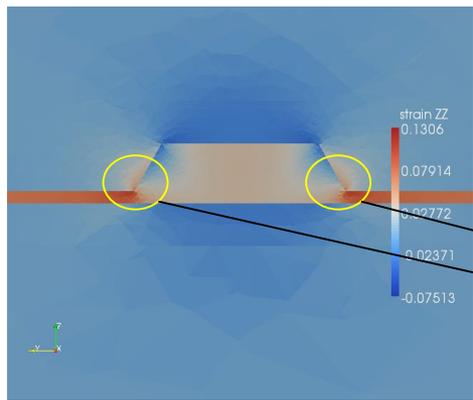


Self assembled by strain relaxation
High lattice mismatch (about 7%)

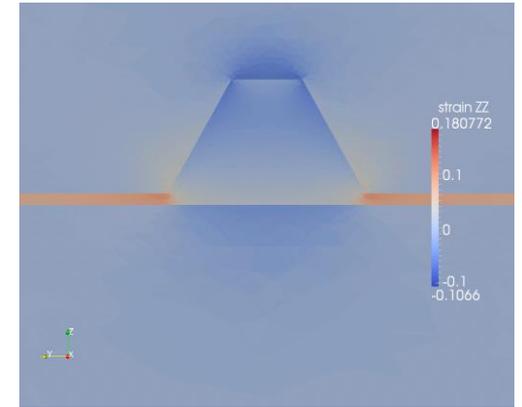
15% differences



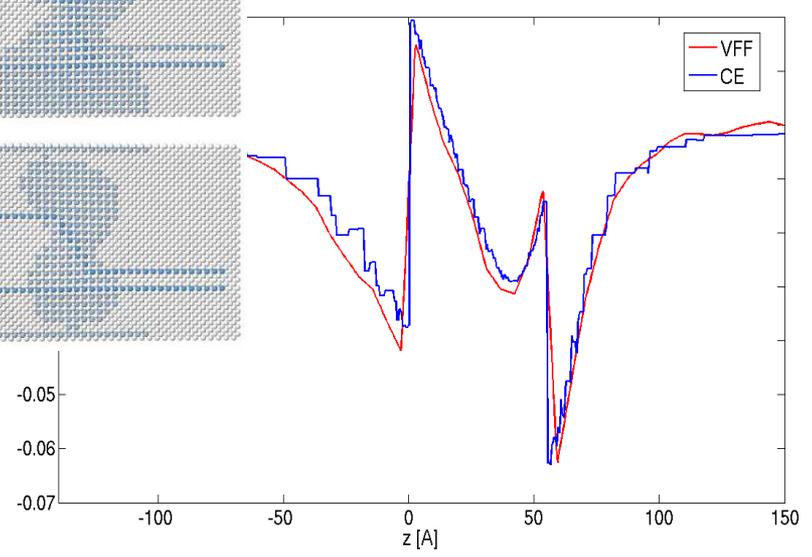
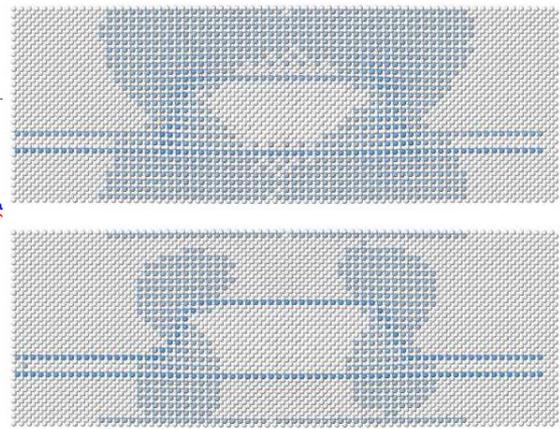
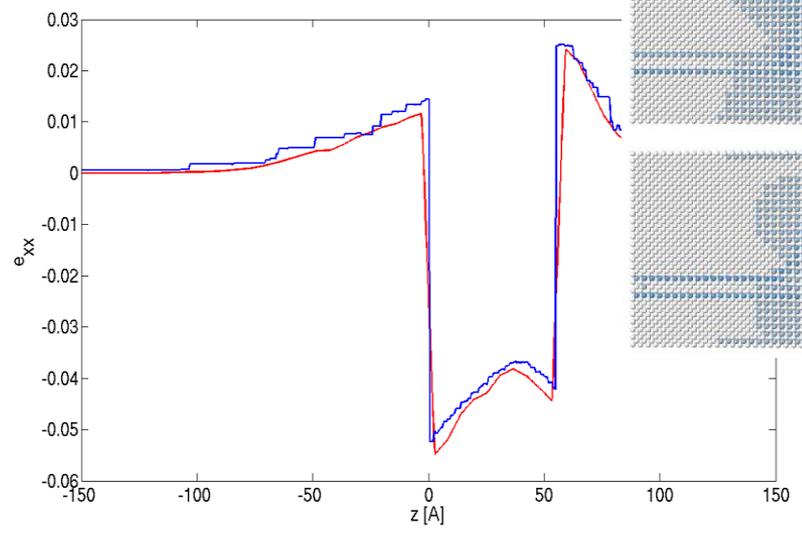
Smaller differences on low aspect/ratio structures

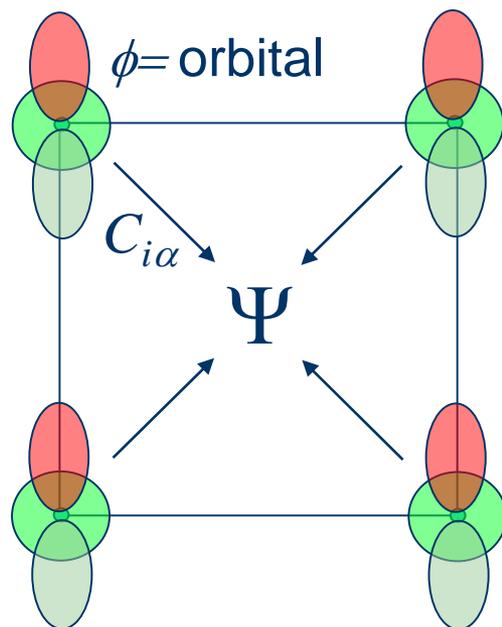


Increase height up to 5 nm



VFF is **fundamental** also to include **internal strain** here!





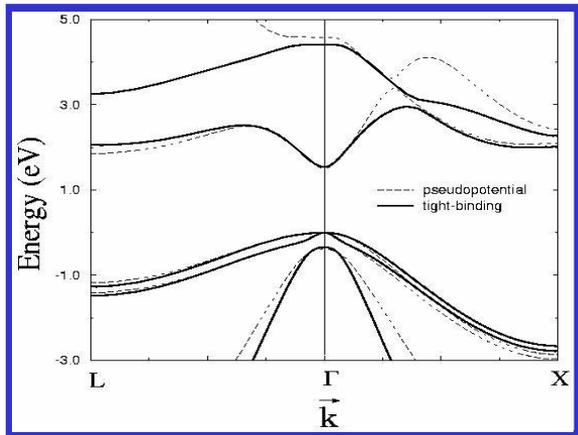
$$\psi(\mathbf{r}) = \sum_{\text{atomic site, } i} \sum_{\text{orbitals, } \alpha} C_{i\alpha} \phi_{i\alpha}(\mathbf{r} + \mathbf{R}_i)$$

$$\langle \phi_{i\alpha} | \phi_{j\beta} \rangle = S_{i\alpha, j\beta} = \delta_{ij} \delta_{\alpha\beta}$$

$$\sum_{\text{atomic site, } j} \sum_{\text{orbitals, } \beta} [H_{i\alpha, j\beta} - E_n] C_{j\beta} = 0$$

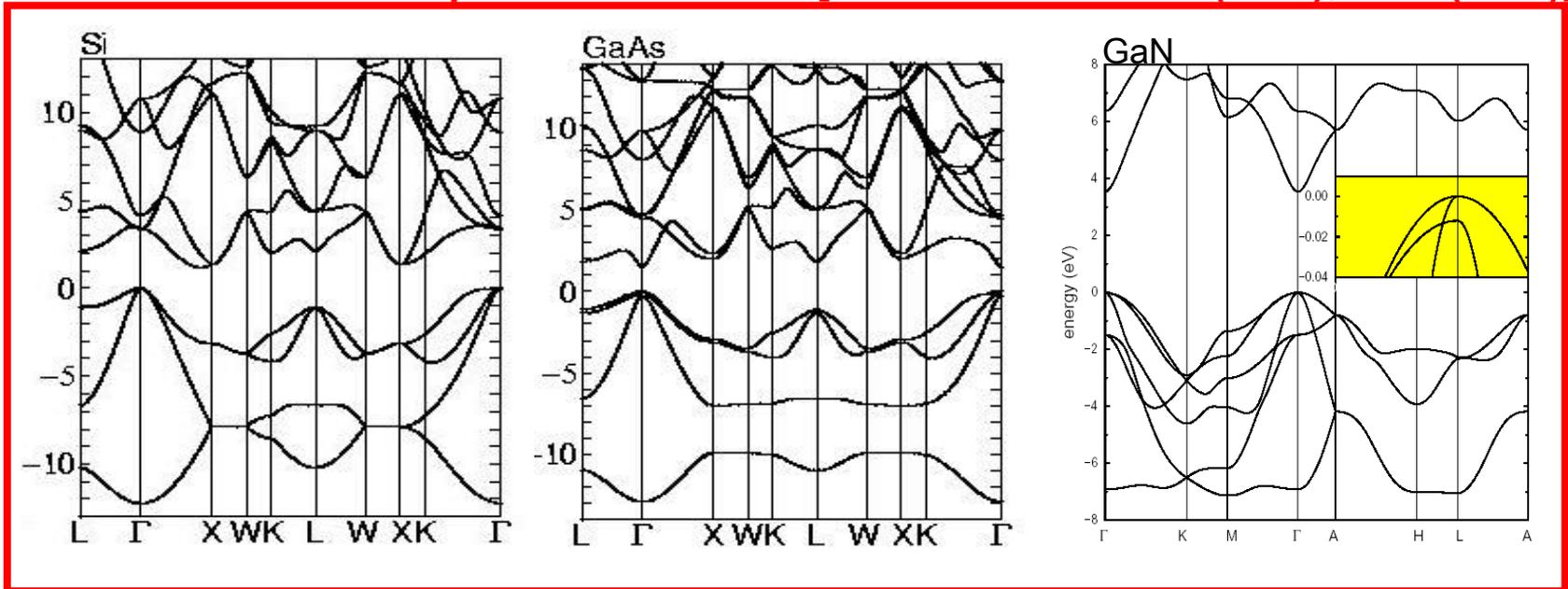
matrix notation:

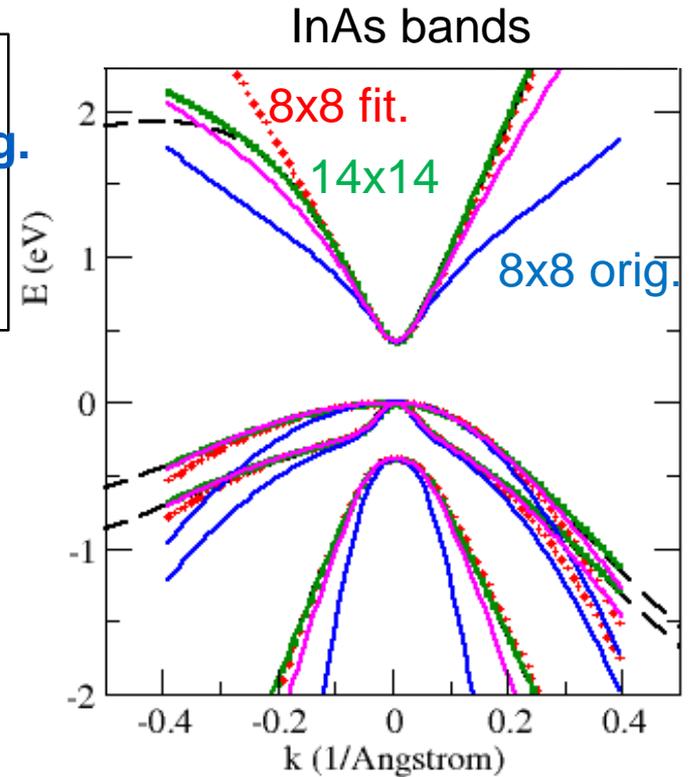
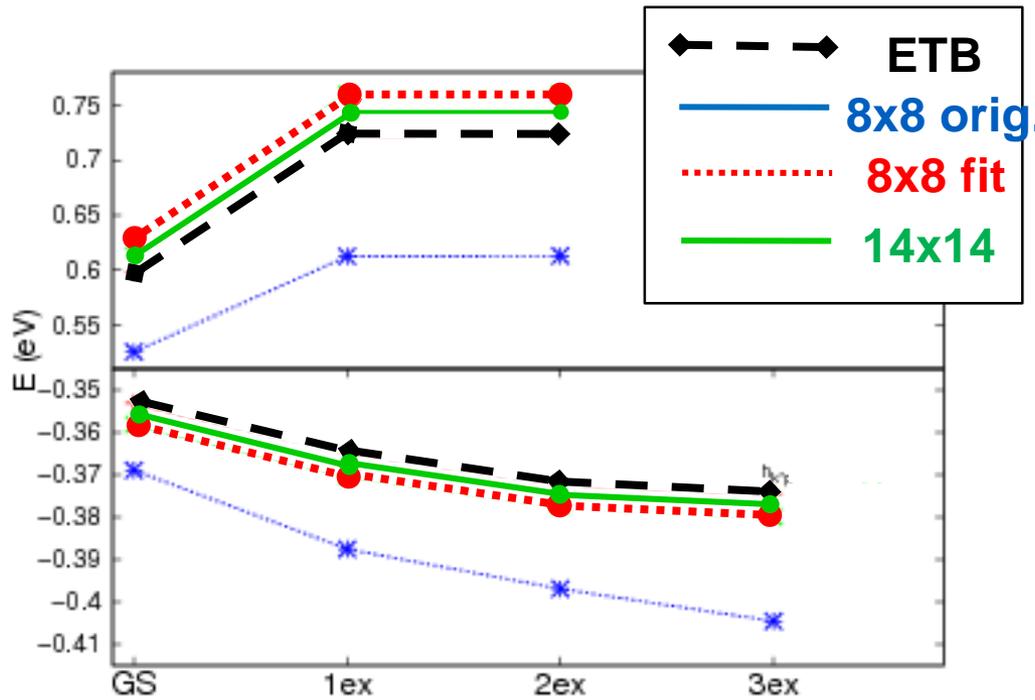
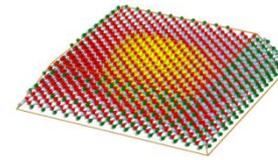
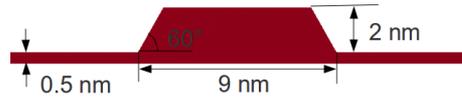
$$\mathbf{HC} = \mathbf{EC}$$



The sp^3s^* Hamiltonian
 [Vogl et al. J. Phys. Chem Sol. 44, 365 (1983)]

The $sp^3d^5s^*$ Hamiltonian [Jancu et al. PRB 57 (1998); PRB (2001)]





Residual difference can be due to **interface effects**

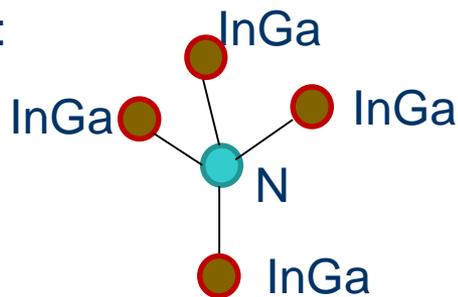
Alloys

Can treat alloys in two ways: VCA (virtual crystal approximation, effective material) or 'real' structure (e.g. random alloy)

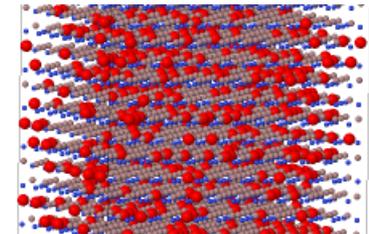
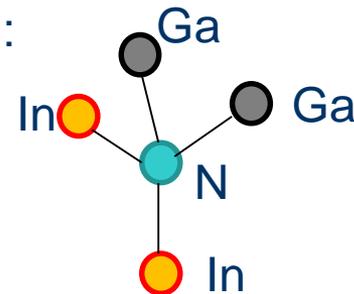
- In VCA matrix elements are taken as mean values:

$$\text{In}_x\text{Ga}_{1-x}\text{N} = x*(\text{InN}) + (1-x)*(\text{GaN})$$
- otherwise onsite elements according to the atom and hopping element according to the pair

VCA:



'real':



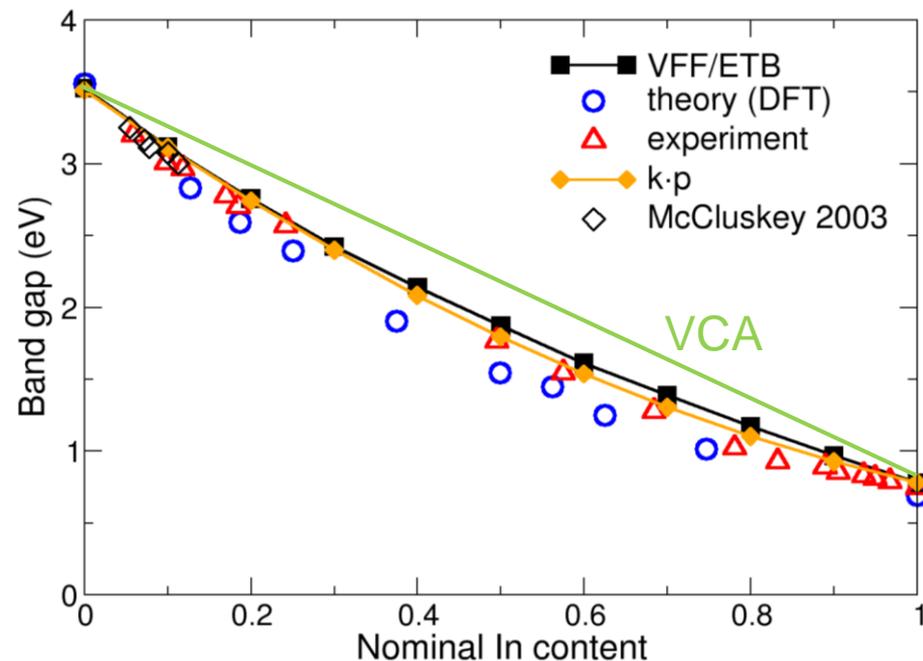
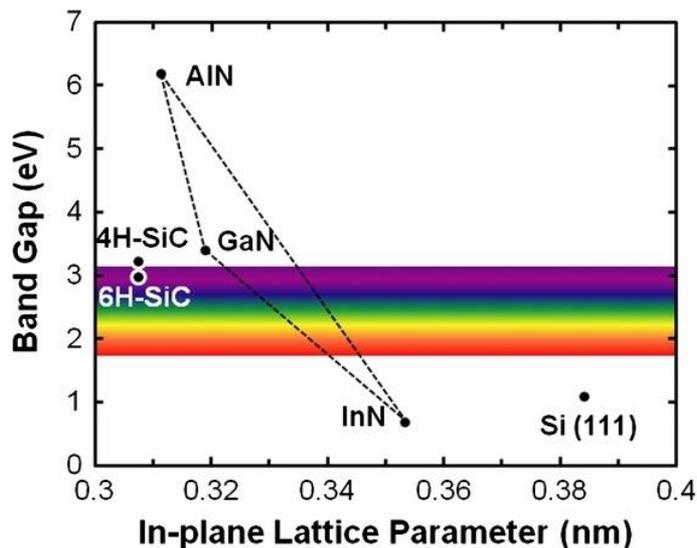
*requires supercell +
statistical ensemble*

Note: we like parameter sets where the common atom (N) is consistent between InN and GaN

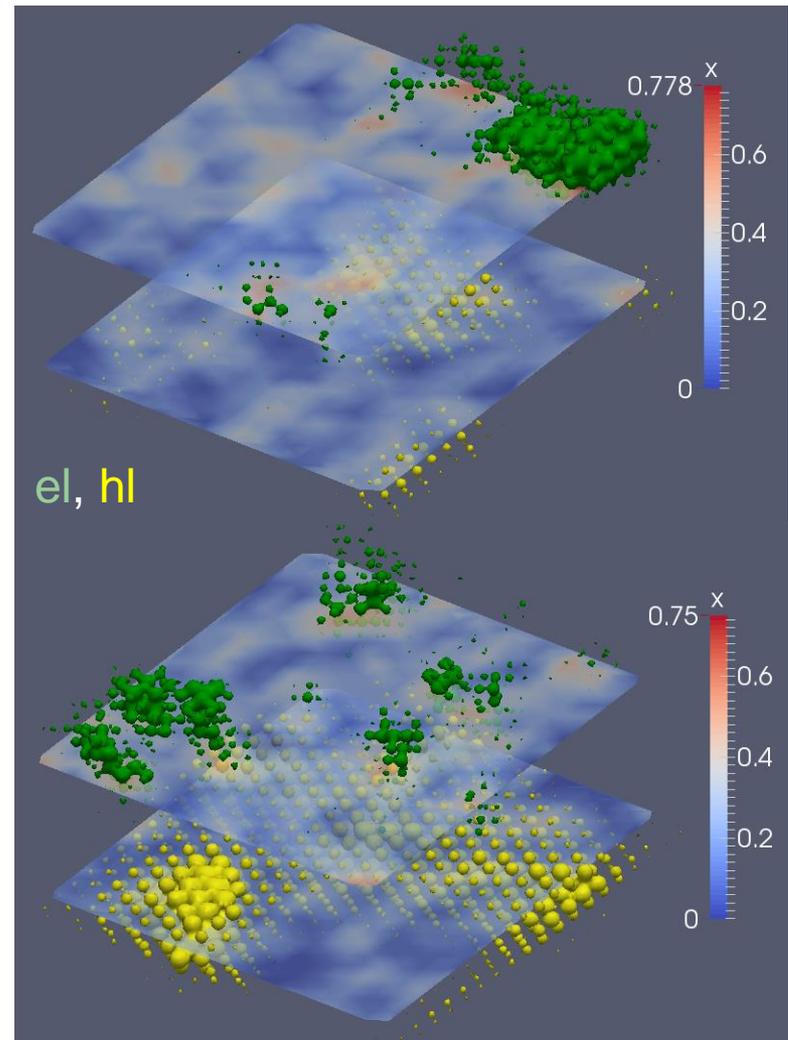
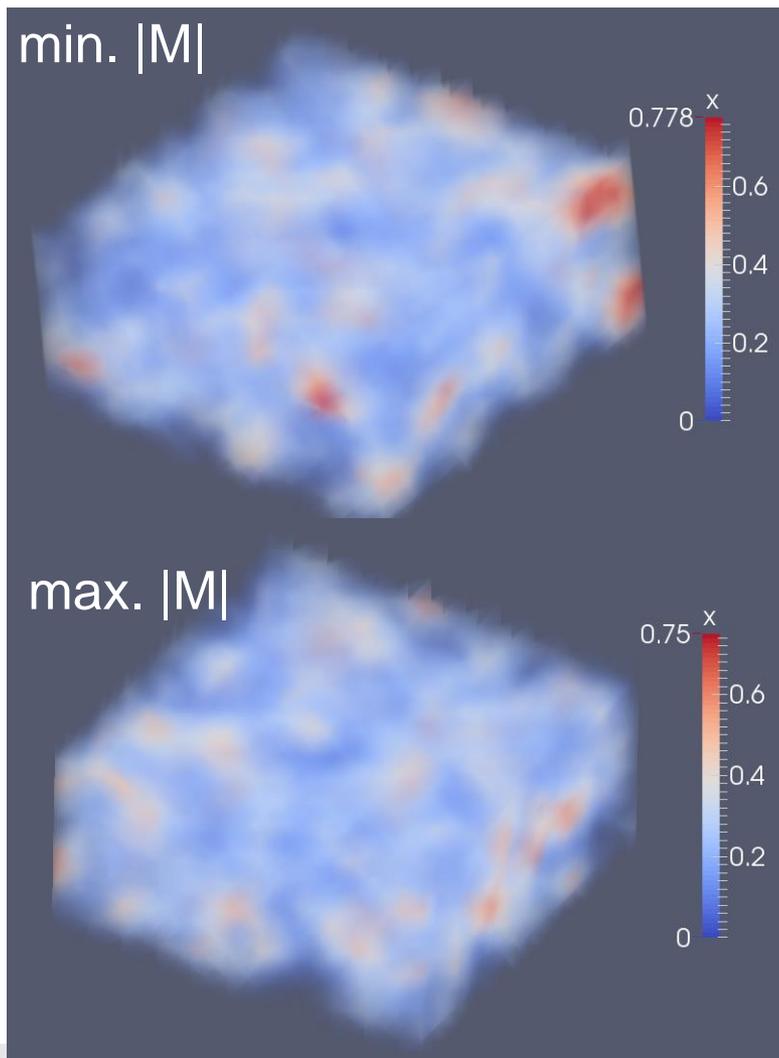
- Tunable gap across visible: high efficiency/efficacy LEDs
- Theoretically could allow for all-nitride phosphor-free white light
- Challenge: InN GaN are 10% lattice mismatched !

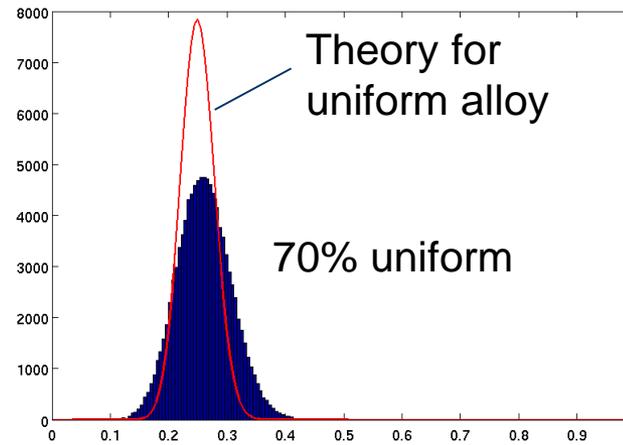
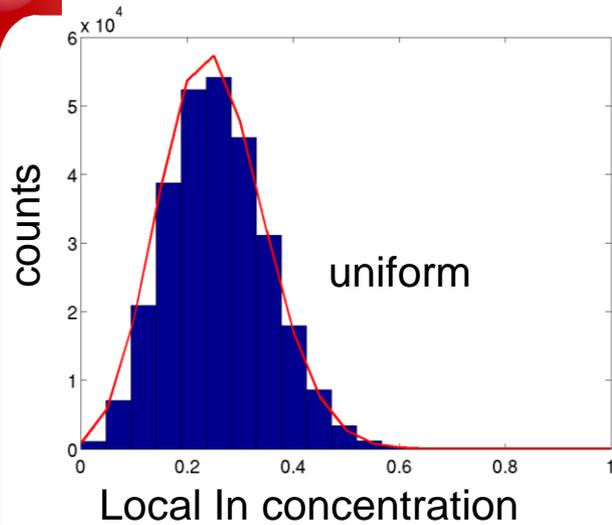
Bulk InGaN

Kaun et al, Semicond. Sci. Technol. 28 074001, 2013

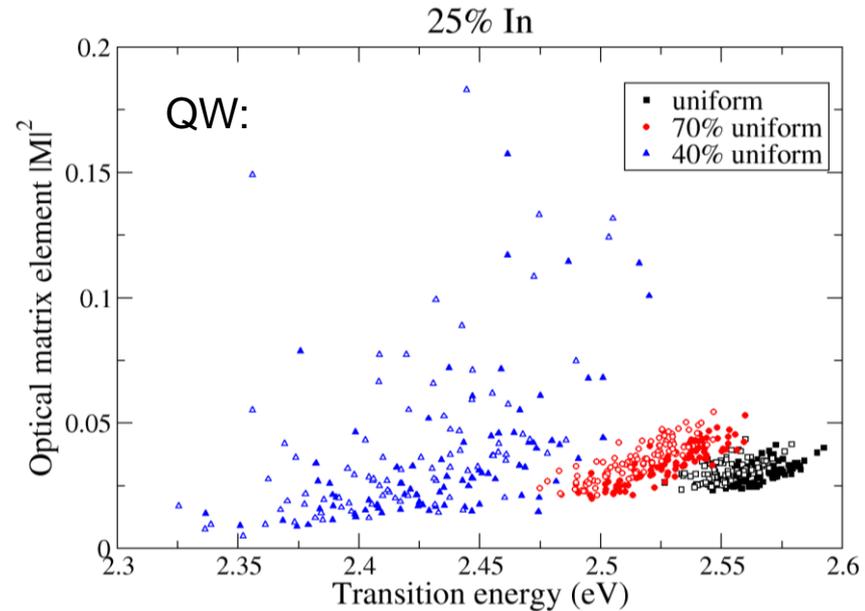
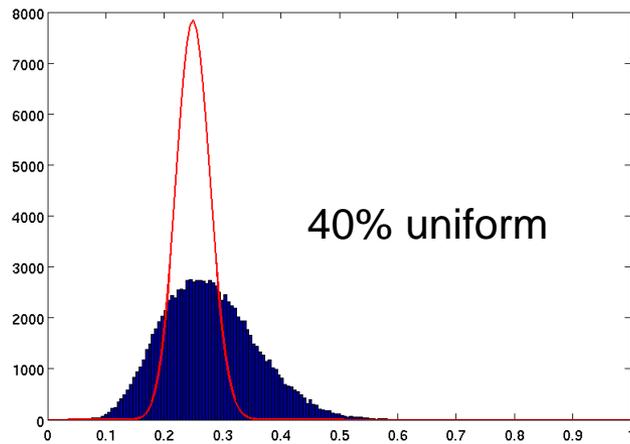


Correlation of local In concentration with wave function localization
Electrons and holes subject to different In fluctuations planes

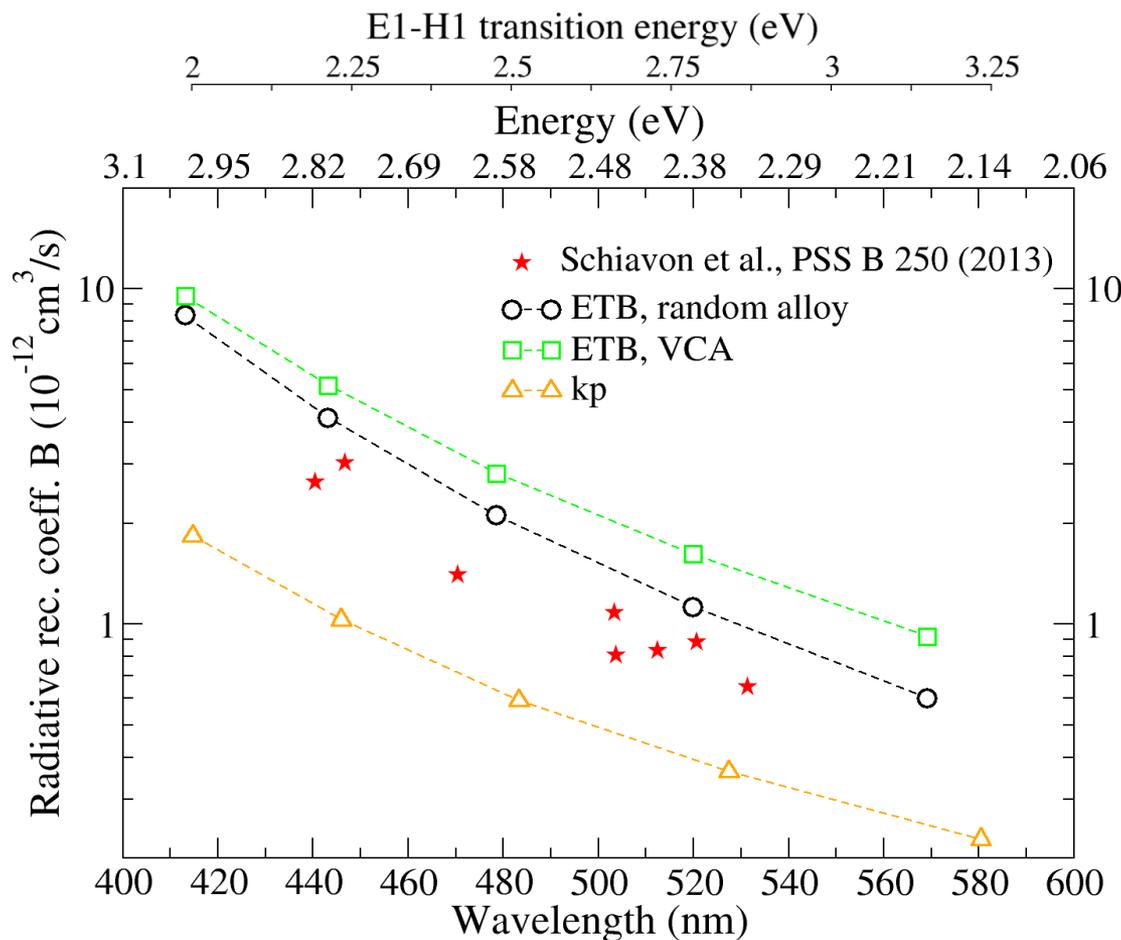




Environment dependent substitution probability



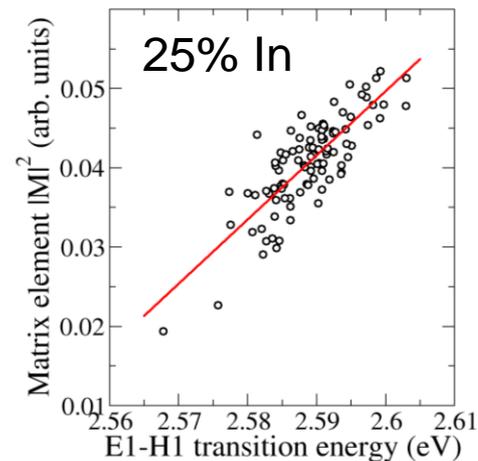
Lateral localization leads to strong fluctuations in optical matrix elements



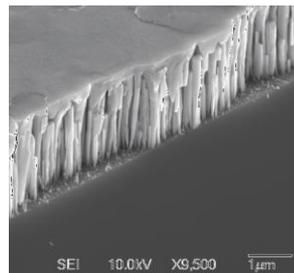
Fluctuation both in energy and M, increasing with In concentration

Correlation between E_g and MME

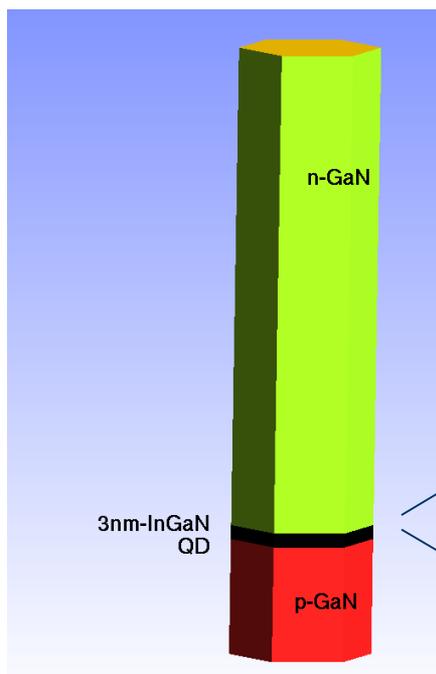
$$E_{ph} * |M|^2 \text{ (arb. units)}$$



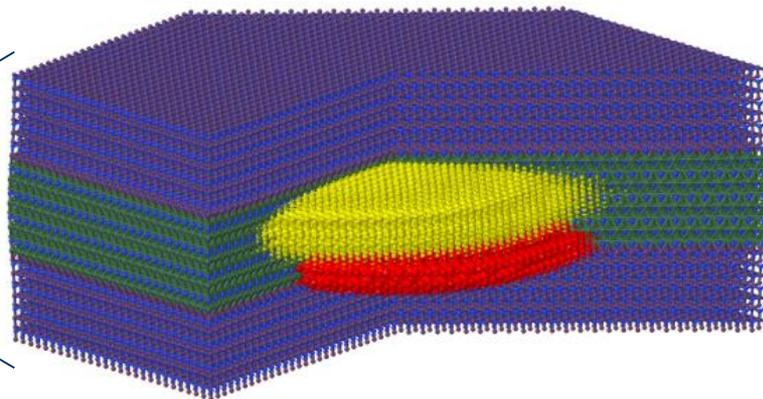
Increasing deviation from VCA values



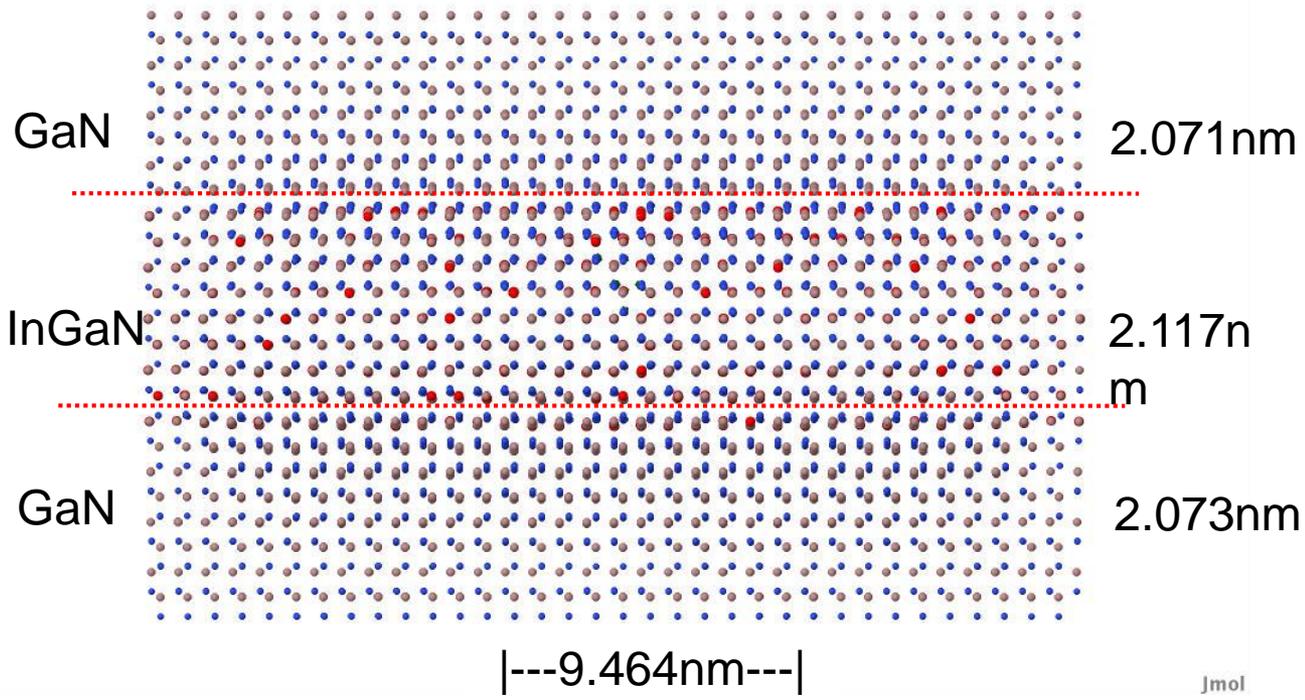
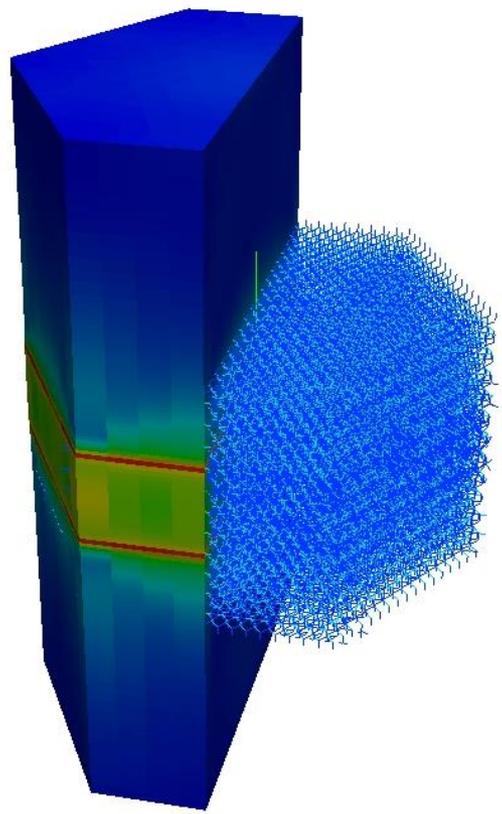
- small footprint on the substrate, allows:
- **defect-free** material
- growth on various substrates (Silicon)
- growth on large area substrates without lattice strain



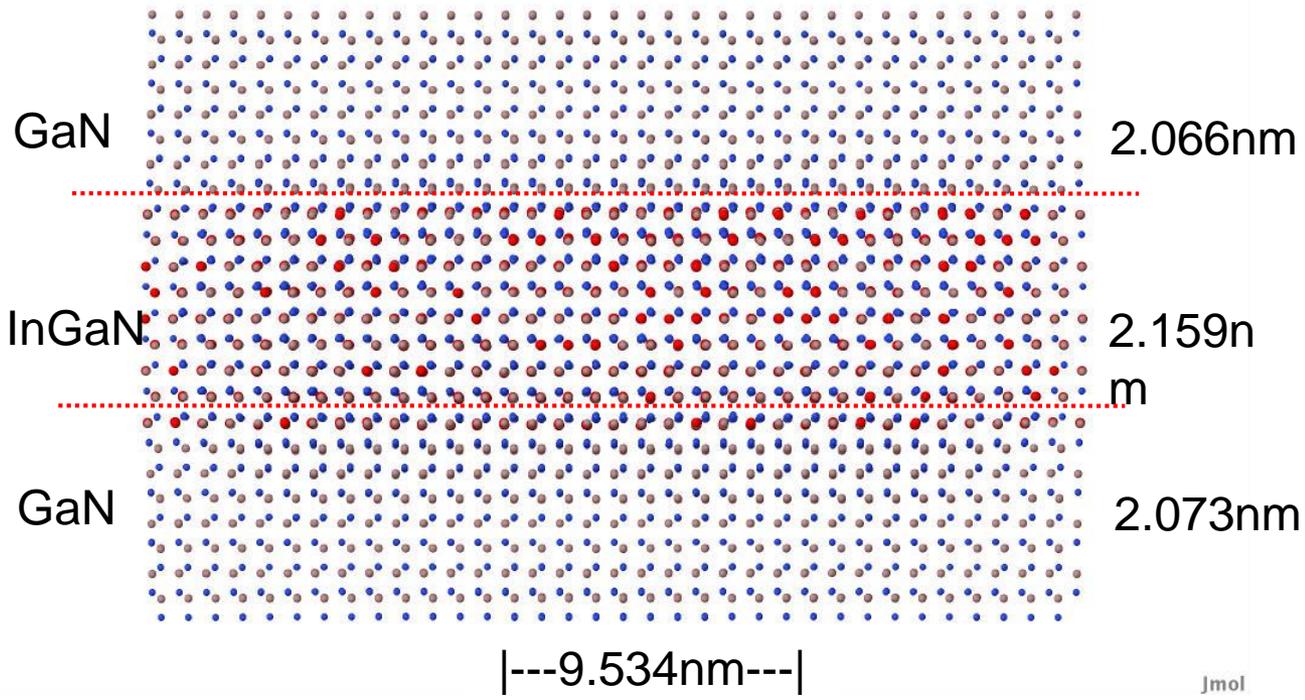
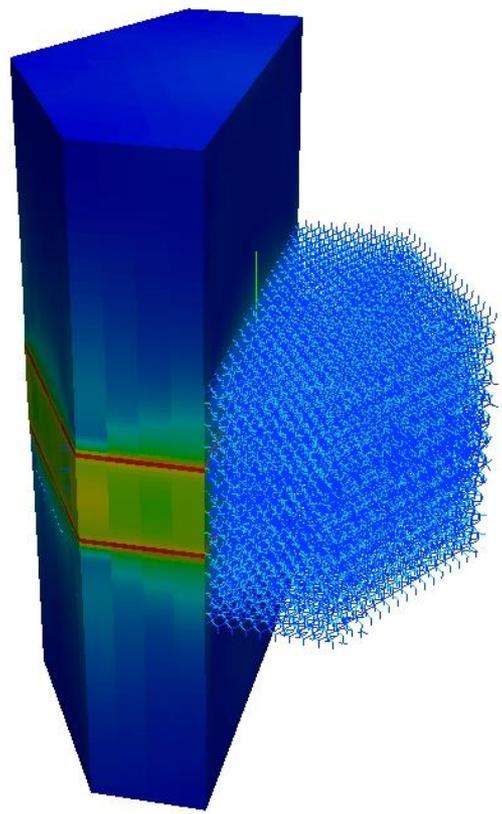
Empirical Tight binding model $sp^3d^5s^*+SO$
Solve few states using Lanczos



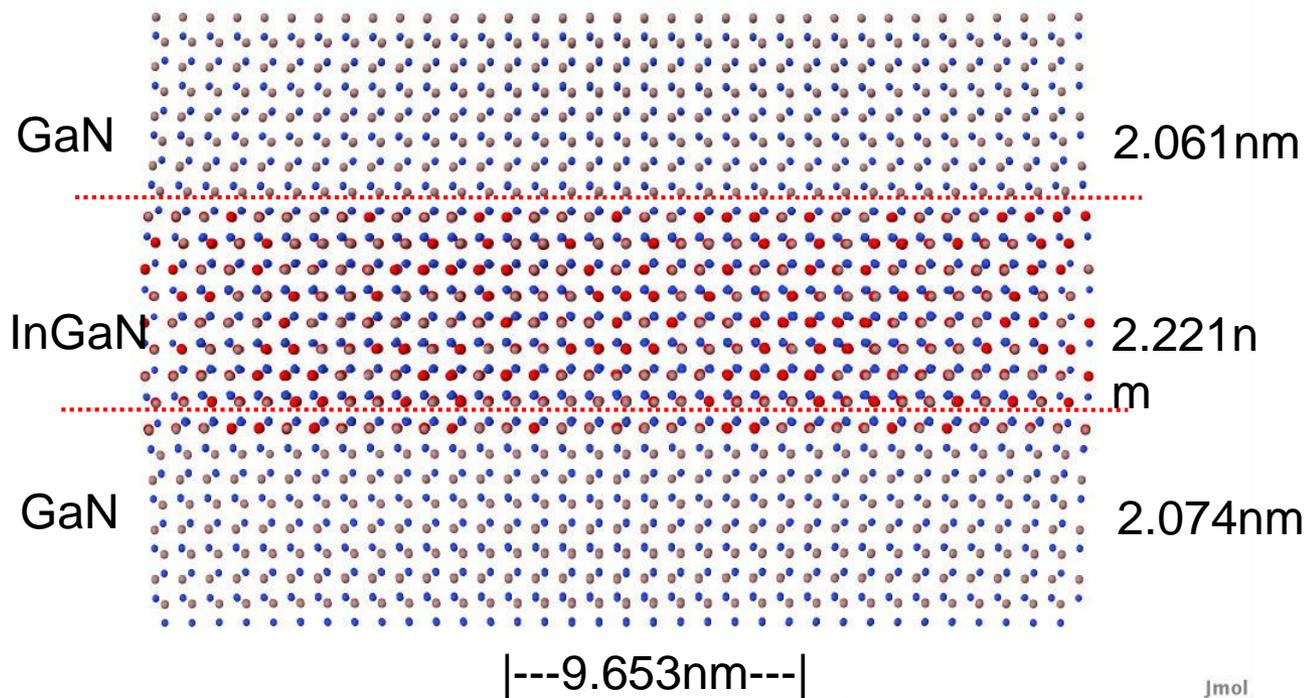
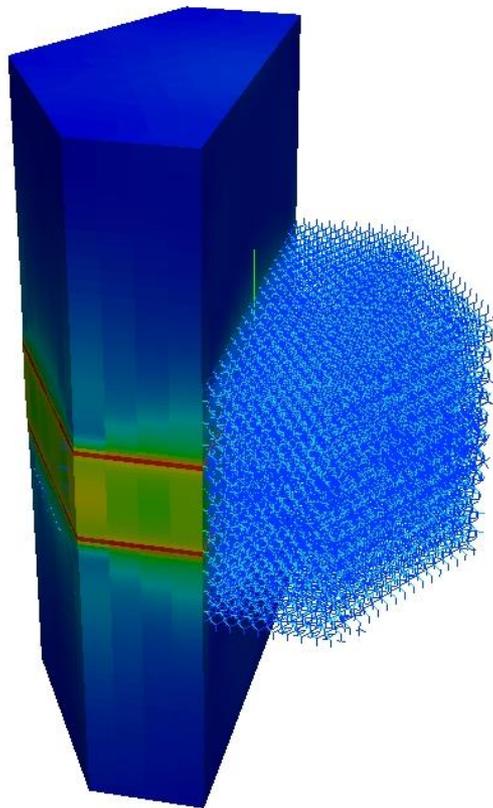
51714 Atoms Strained + VFF x(In=0.10).xyz

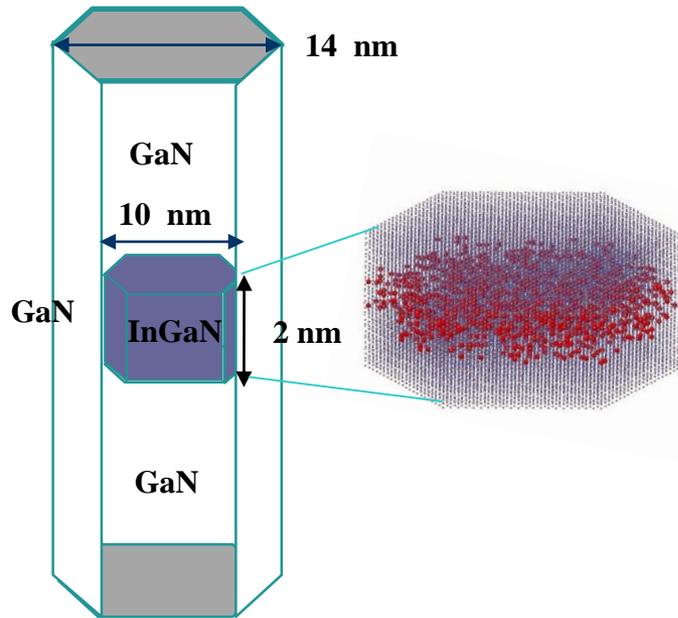


51714 Atoms Strained + VFF x(In=0.20).xyz



51714 Atoms Strained + VFF x(In=0.35).xyz



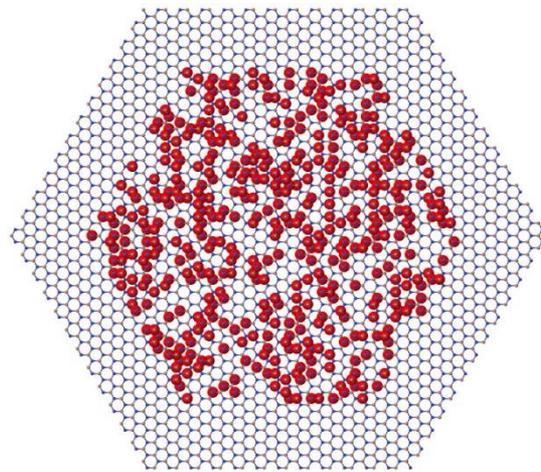
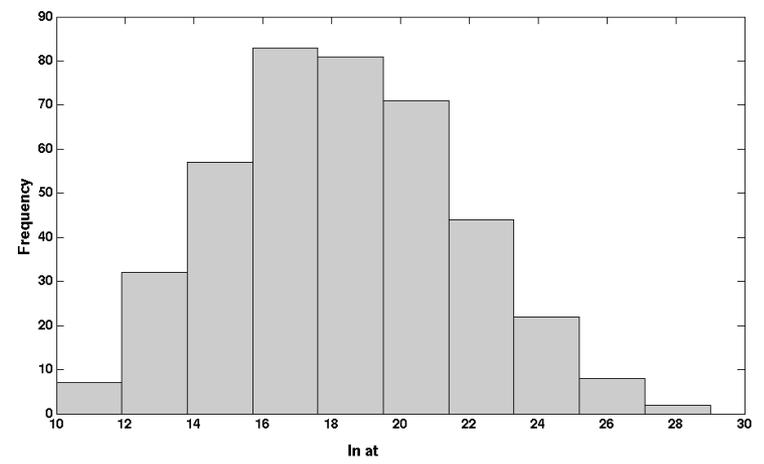


- VCA
- Random uniform
- Random with clustering

Uniform distribution is first applied to the structure (e.g. 70% uniform and 30% clustering)

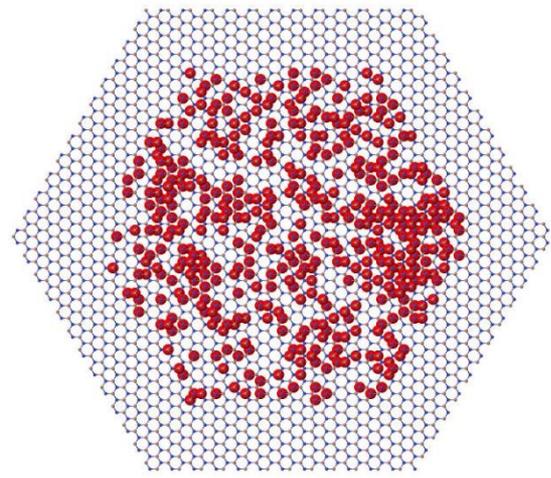
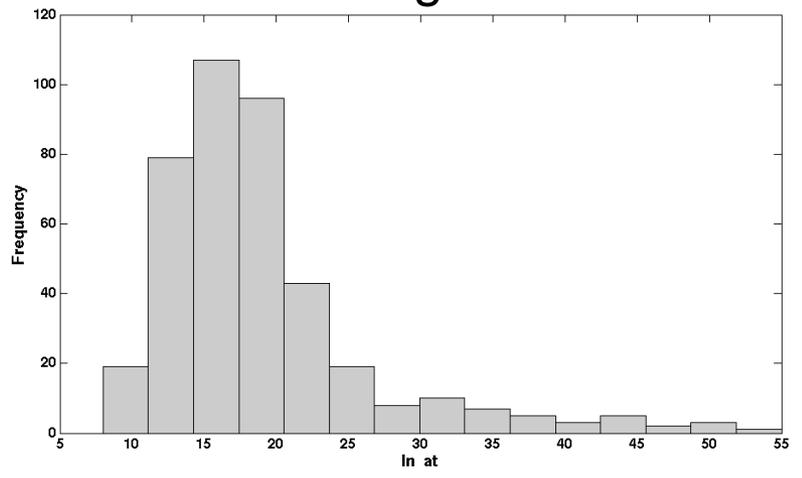
Probability of Substitution of a Ga atom in GaN with In is higher if other In atoms are already in a sphere of 1nm radius around the atom.

No clustering



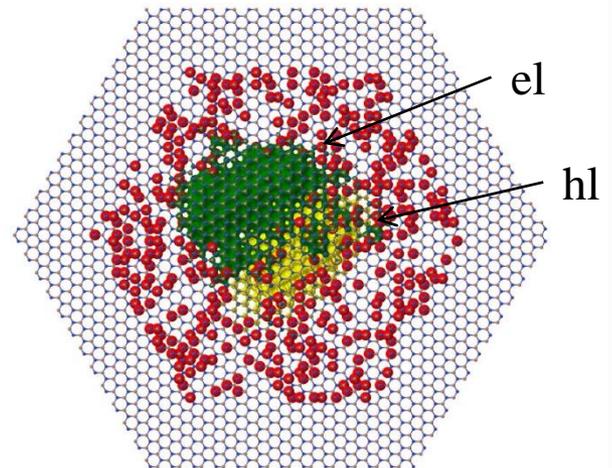
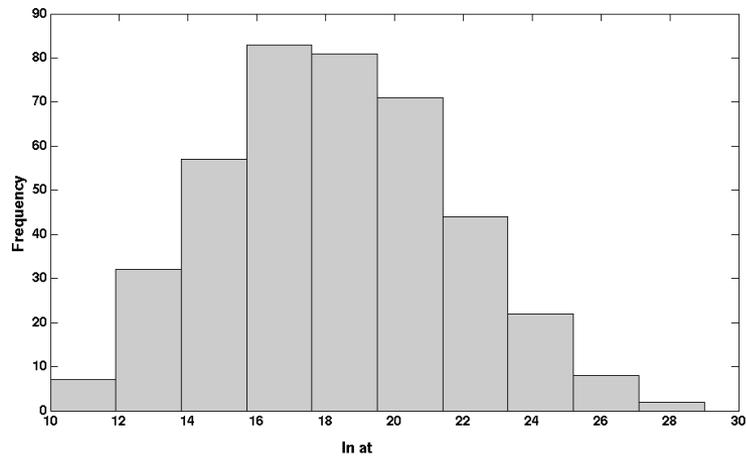
Jmol

30% clustering



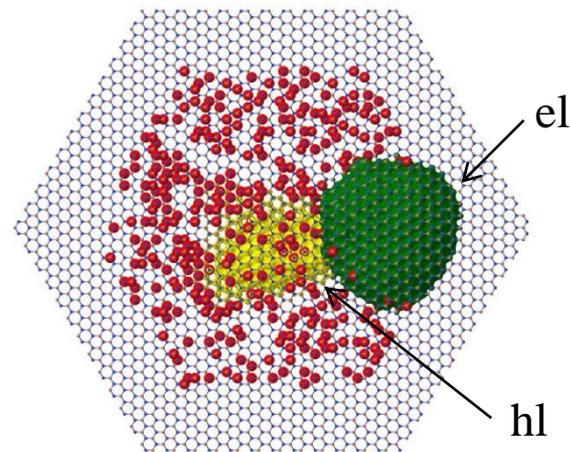
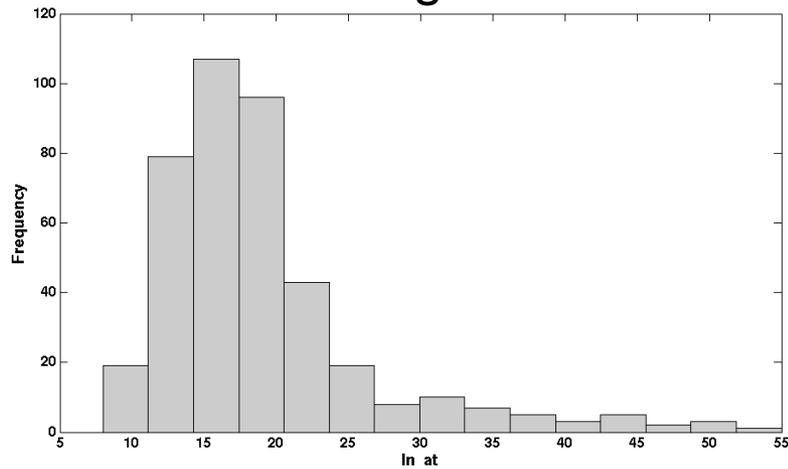
Jmol

No clustering

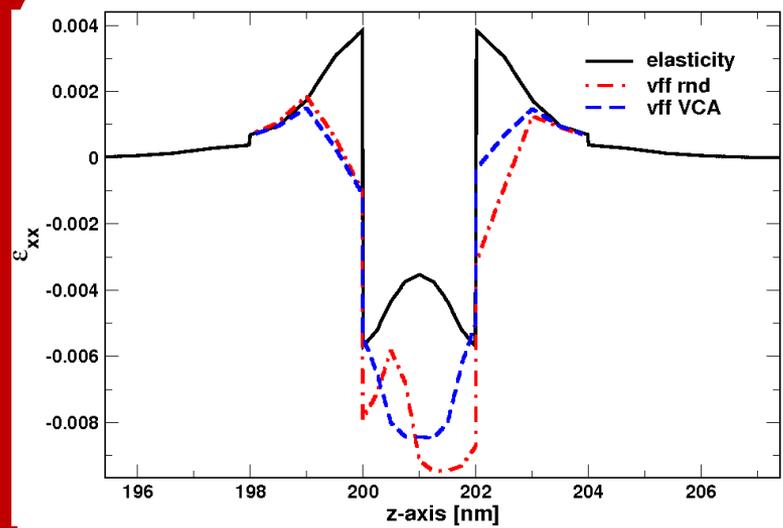


Jmol

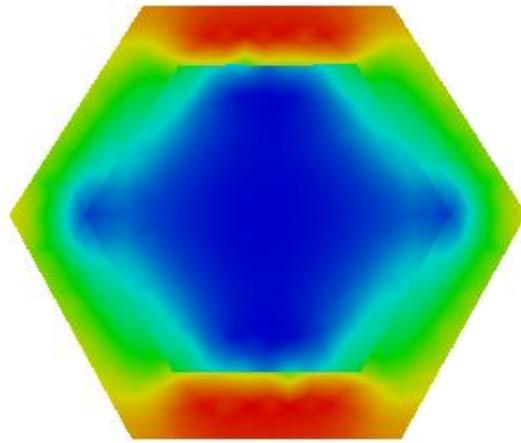
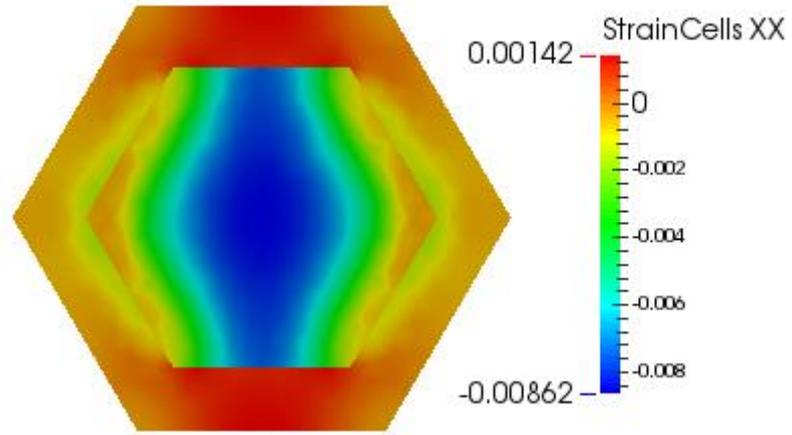
30% clustering



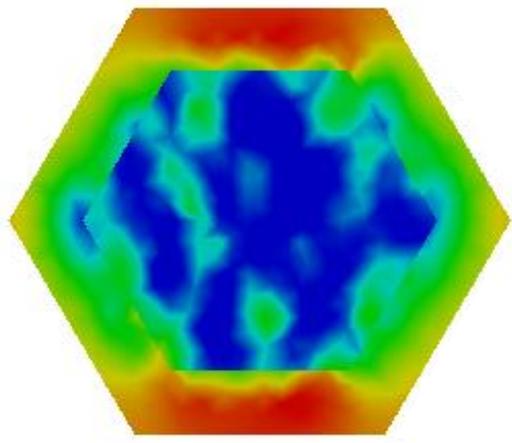
Jmol



ϵ_{xx} strain from elasticity macroscopic model (VCA)



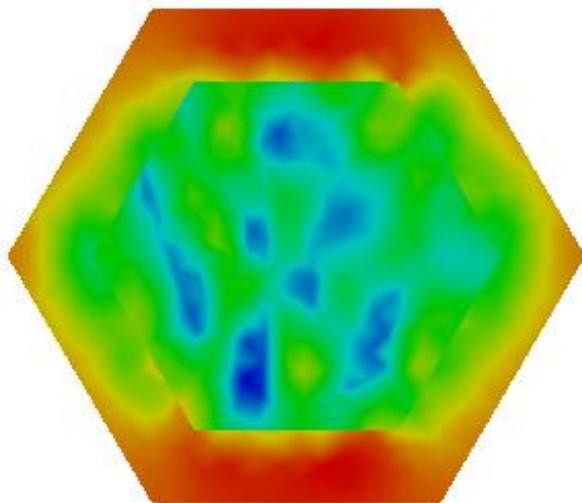
VFF on a VCA structure



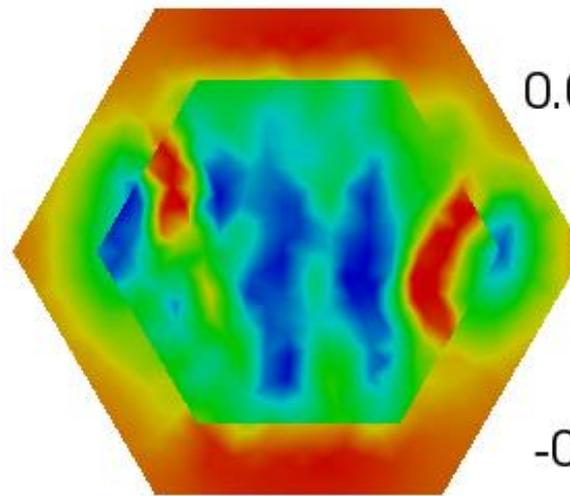
VFF on a random sample

xy plane in the InGaN region

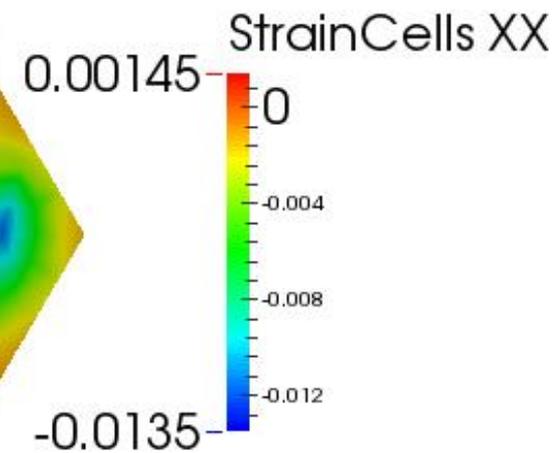
Strain from VFF on a random sample



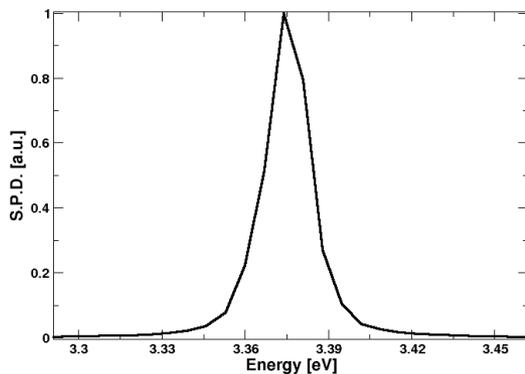
uniform distribution



clustering

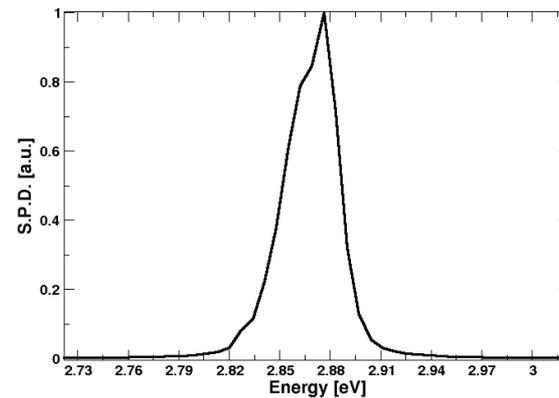


In 10%

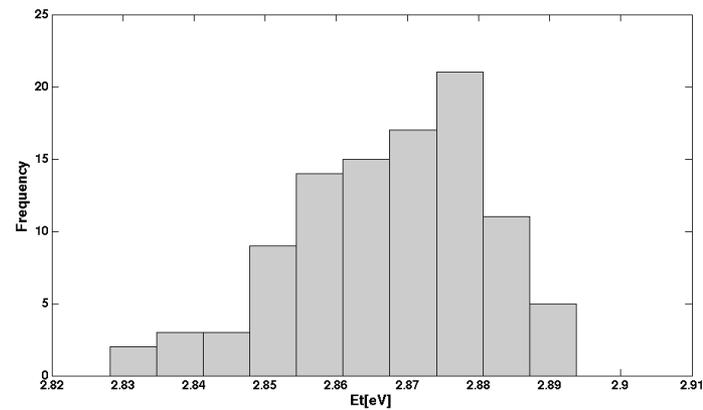
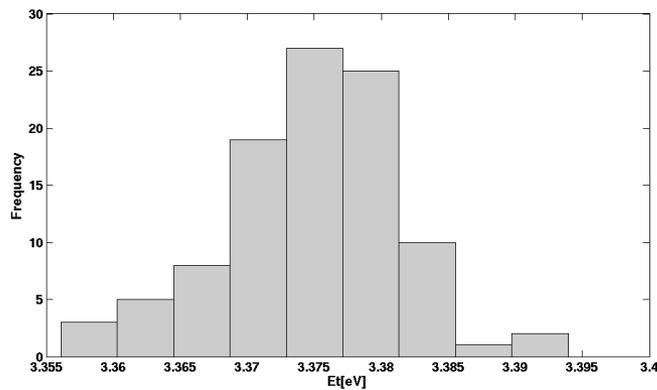


FWHM = 18 meV

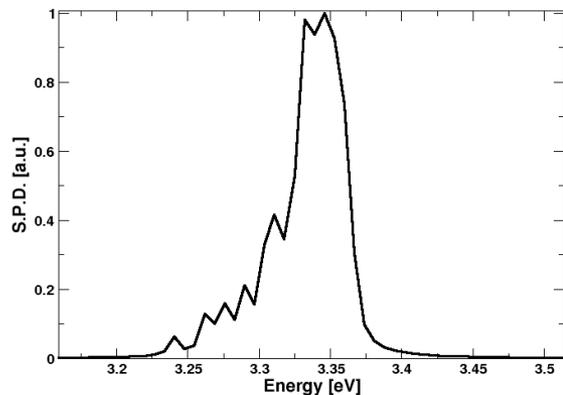
In 30%



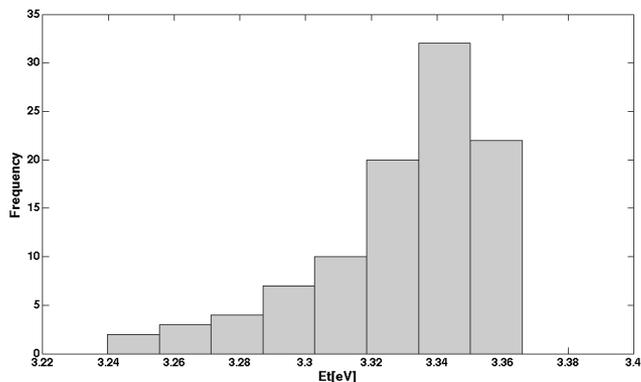
FWHM = 35 meV



In 10%



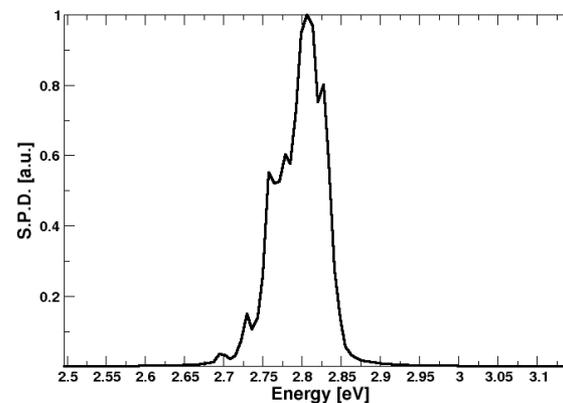
FWHM = 20 meV broadening



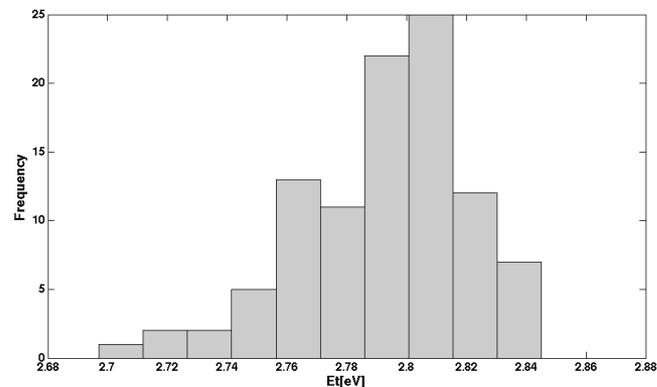
Distribution of energy gaps

Mean = 3.329
 Std = 0.0278
 skew = -1.242

In 30%

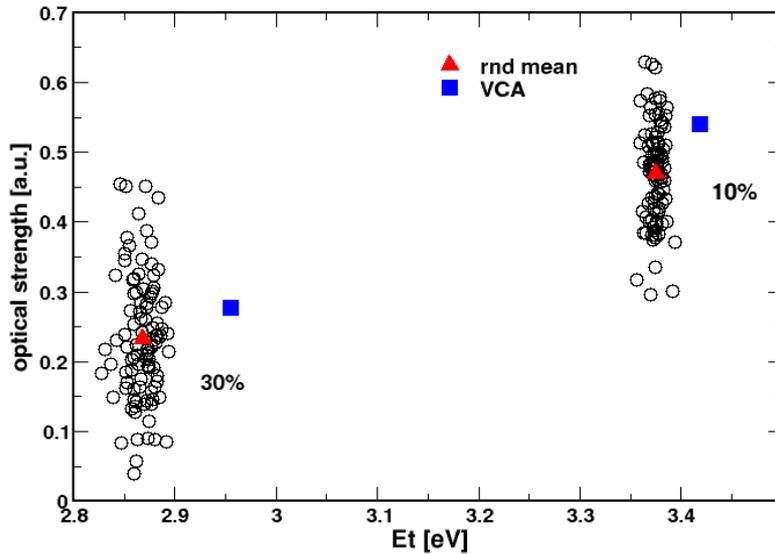


FWHM = 45 meV broadening



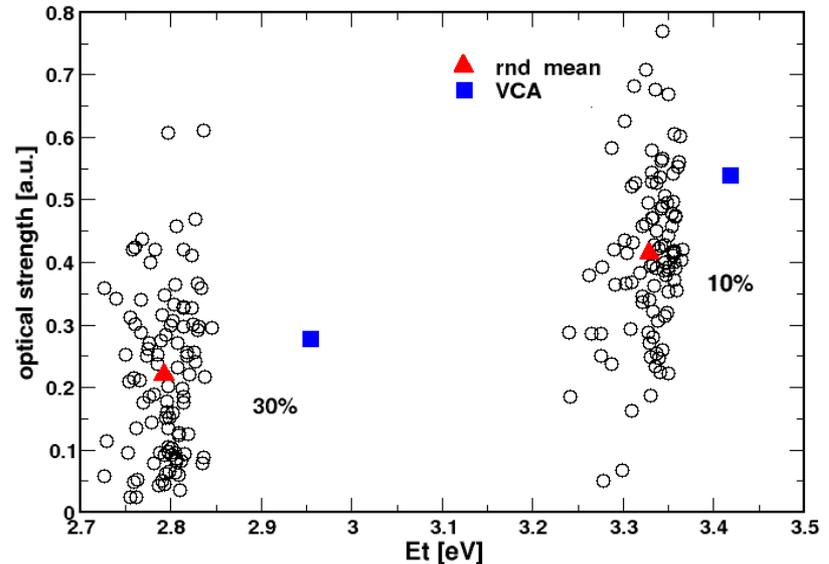
Distribution of energy gaps

Mean = 2.793
 Std = 0.028
 skew = -0.708

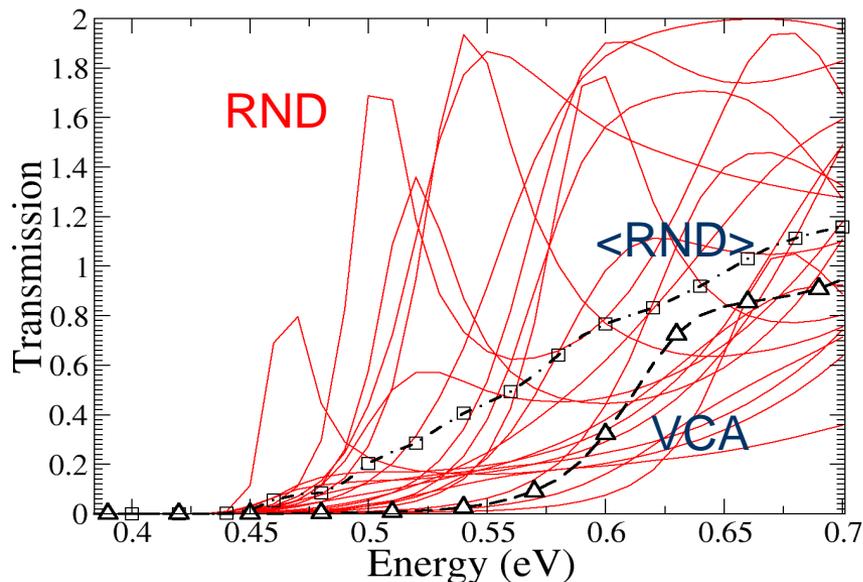
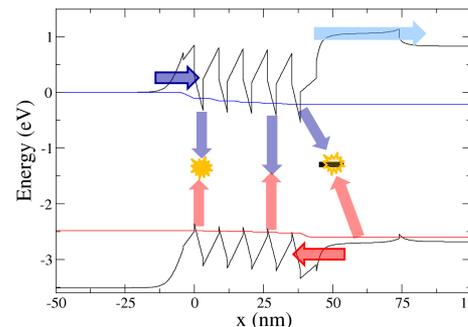
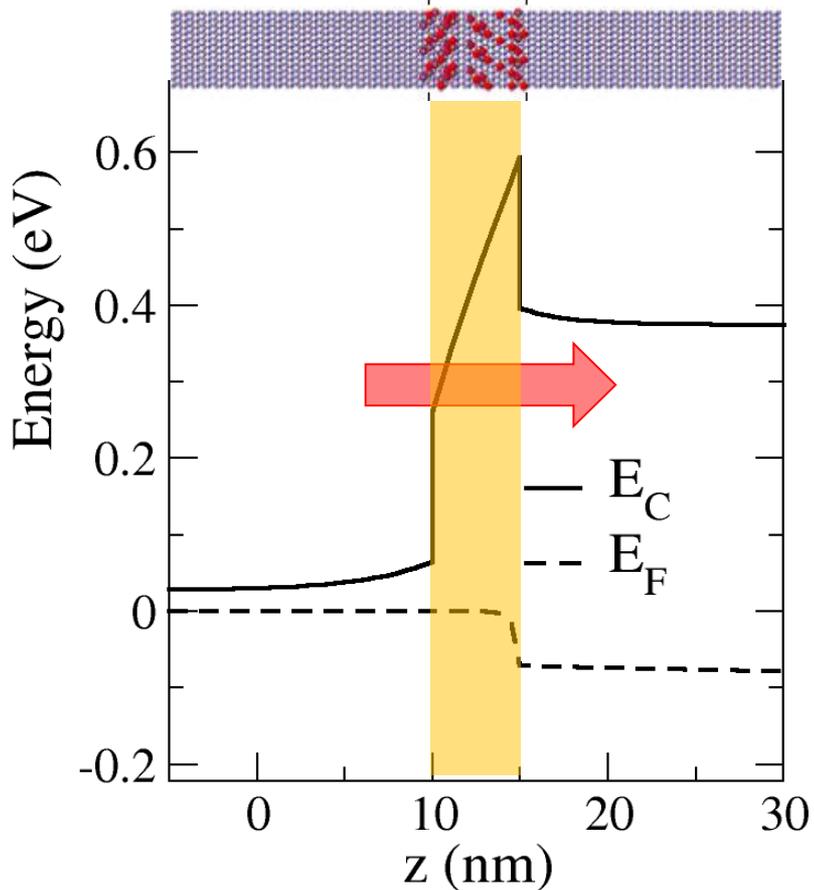


- ❑ Correlation between ground state transition energy and optical strength
- ❑ Increasing spread in random distribution with higher $x(\ln)$
- ❑ VCA overestimates E_t and Opt.strength

- ❑ Clustering effect:
- ❑ Larger spread in random distribution
- ❑ Lowering of mean E_t

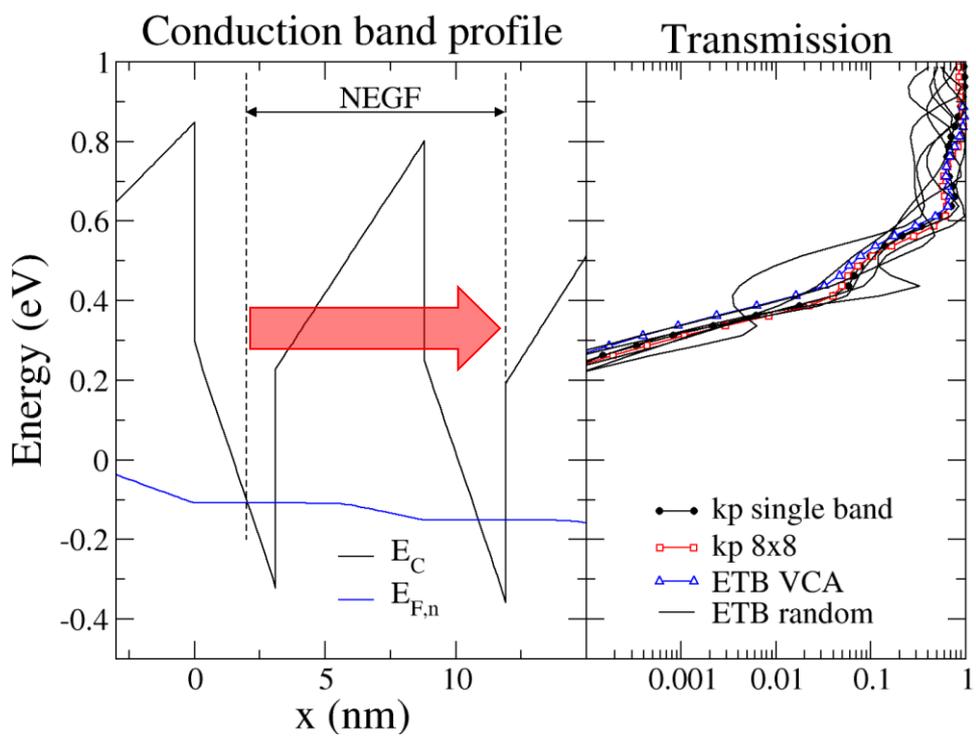


tunneling across $\text{Al}_{0.2}\text{Ga}_{0.8}\text{N}$ EBL:



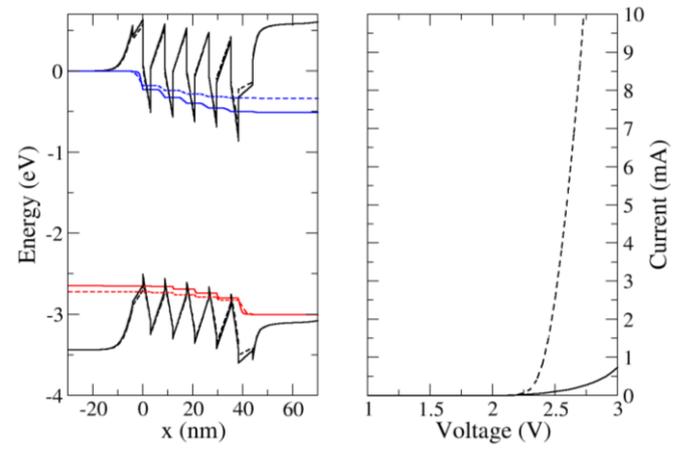
Considerable fluctuations due to random alloy: similar to defect assisted tunneling

tunneling across $\text{In}_{0.05}\text{Ga}_{0.95}\text{N}$ barrier:

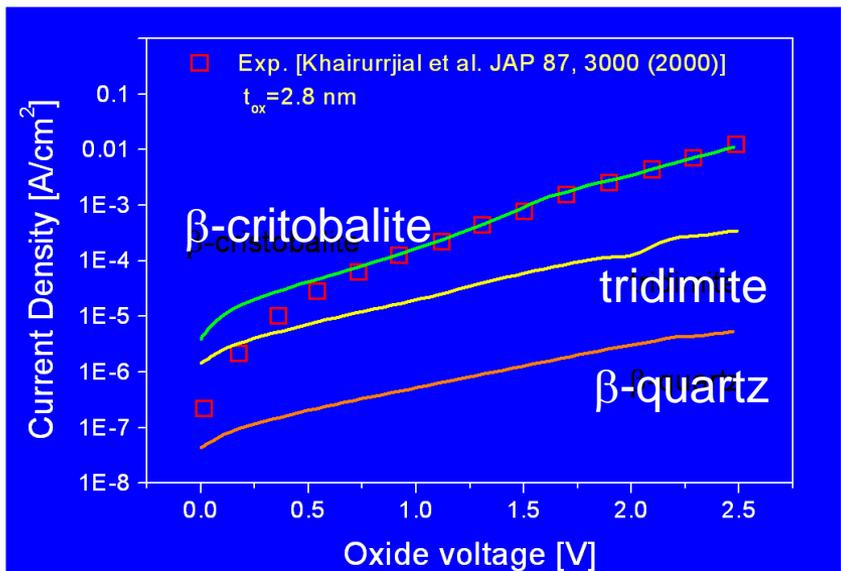
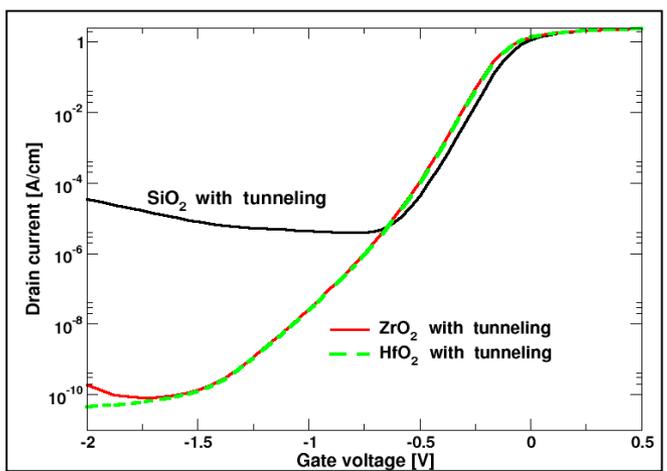
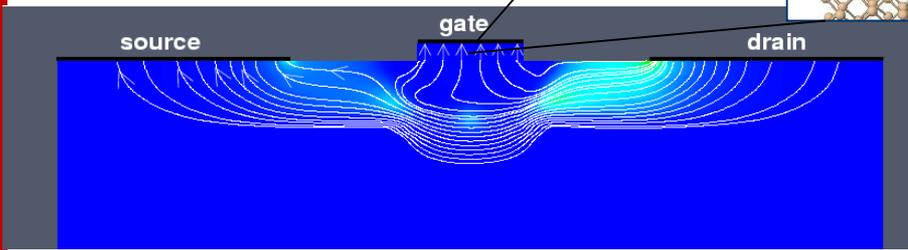
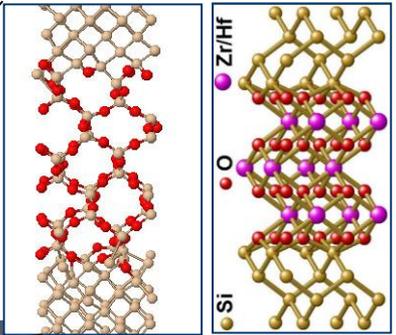


⇒ More realistic ON current:

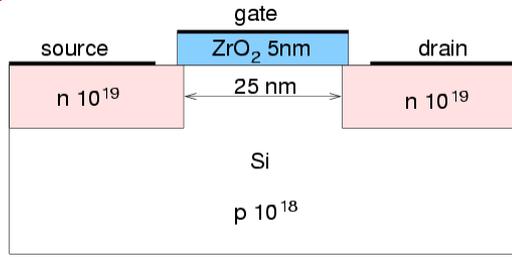
- Extracted barrier resistivity:
- Pure drift-diffusion: $15 \Omega\text{cm}^2$
- 8 band k·p: $1.33 \Omega\text{cm}^2$
- Random alloy: $0.28 - 1.26 \Omega\text{cm}^2$



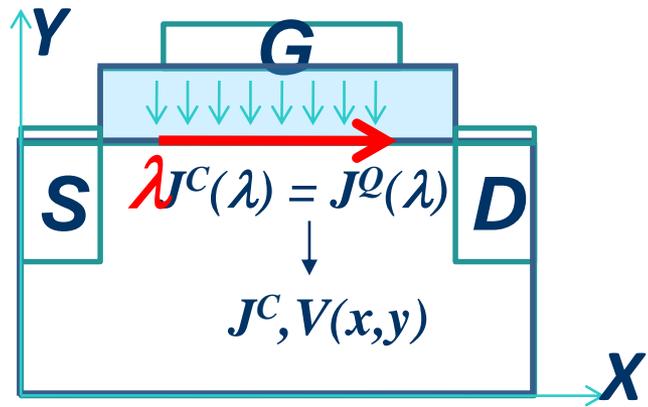
Coupling DD with ballistic tunneling, quantum density



Sacconi et al IEEE TED 2004 and 2007
 M. Auf der Maur et al. J. Comp. Elect., 7 398 (2008)



$$J_y^C(\lambda) = 0$$



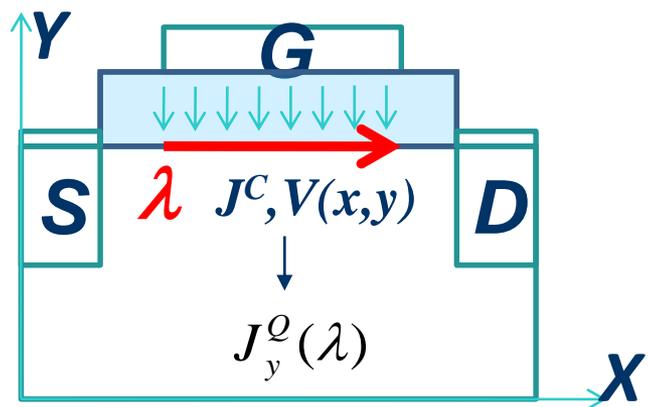
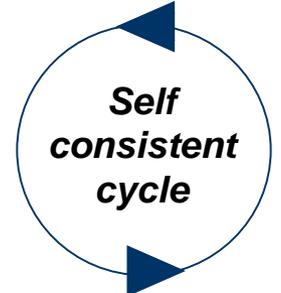
$$\mathbf{J}^C = \mu_n n \nabla \phi_n$$

$$\nabla \cdot \mathbf{J}^C = G - R$$

$$\nabla \cdot (\epsilon \nabla V) = -\rho$$

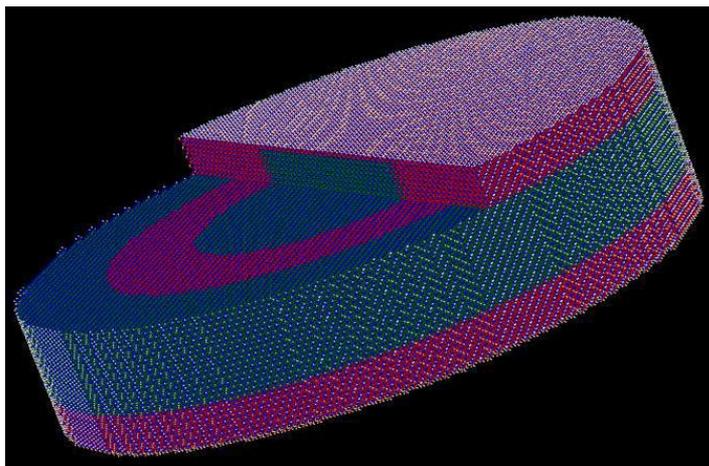
Poisson-Drift-Diffusion is solved in the whole device

$$J_y^C(\lambda) = J_y^Q(\lambda)$$



$$J_y^Q(\lambda) = f(V(\lambda) - V_G)$$

Tunneling current calculated with atomistic tight-binding model is taken as a boundary condition for electron continuity at Si/oxide interface



1,000,000 atoms on a WS!

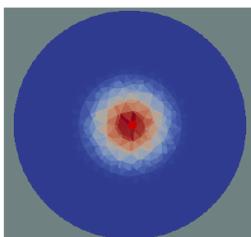


Fig 3: State 1 confined inside the Dot

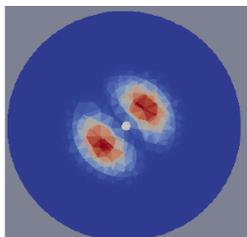


Fig 4: State 3 confined inside the Dot

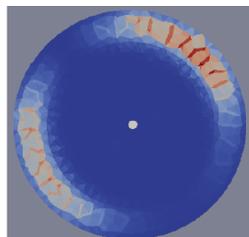
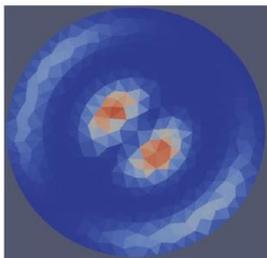
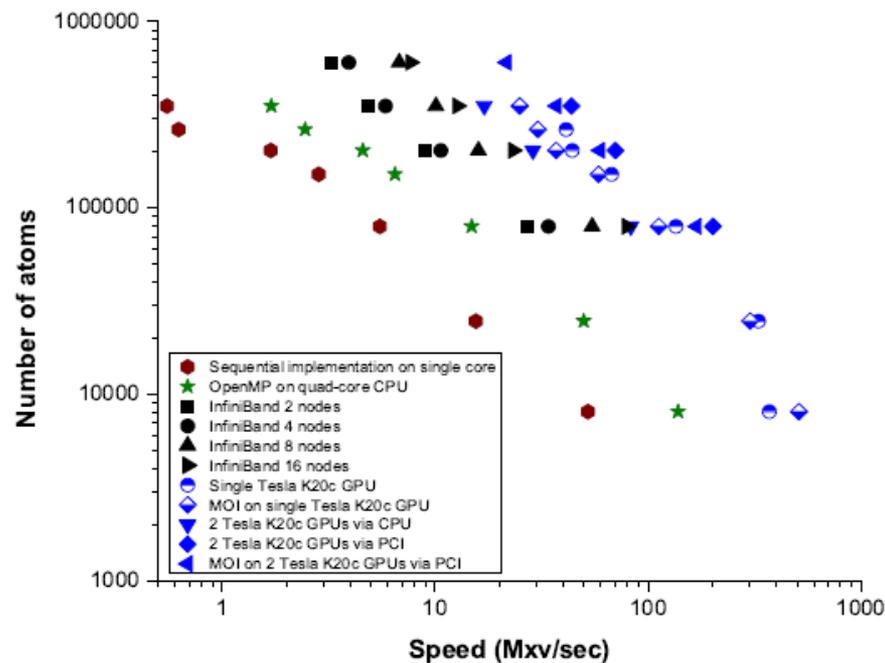


Fig 5: State 8 confined inside the Ring



Lambda state



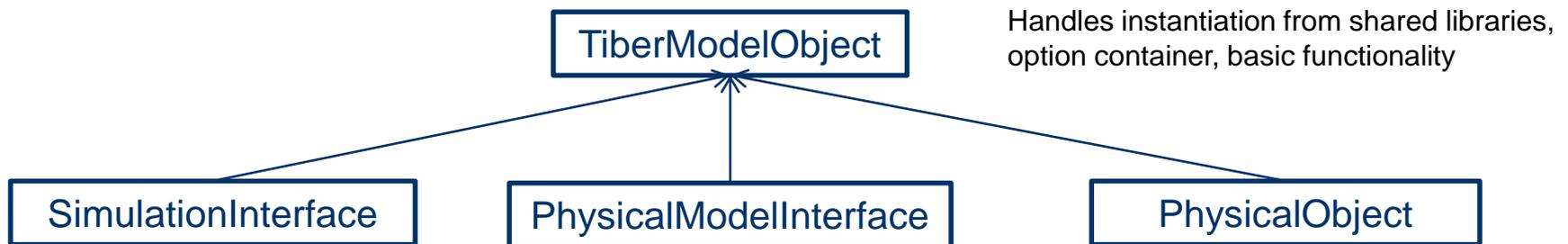
W. Rodrigues, A. Pecchia, A Di Carlo, *Comp. Phys. Comm.* (2014)

Software Development ToolKit

⇒ Allows to add new modules by user without relinking core

```
Module somename
{
  Physics {
    mobility constant { }
  }
}
```

 library name `somename.so`
 library name `mobility_constant.so`



```
Module driftdiffusion
{
}
```

```
Physics {
  mobility constant { }
}
```

Base class of all physical entities
bulk, interface, edge, node

```
#include "SimulationInterface.h"

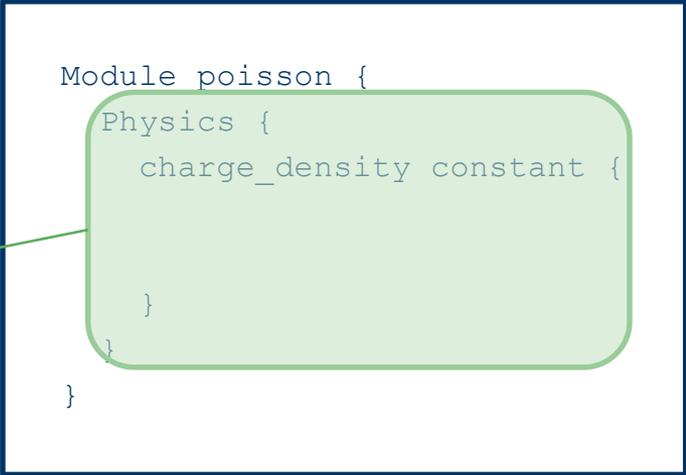
class Poisson : public SimulationInterface
{
public:
    static Poisson* create(options);

protected:
    virtual void do_init(void);
    virtual void parse_options(void);
    virtual void do_setup_solution_variables(void);
    virtual void do_solve(void);
    virtual PhysicalModel* create_bulk_model(options, material);
    virtual PhysicalModel* create_boundary_model(options, boundary);
    virtual void get_solution_secure(element, data, points);

private:

};
```

```
Module poisson {
    Physics {
        charge_density constant {
        }
    }
}
```



- Multiscale/multiphysics is requested for simulation of real modern electronic devices where electronics, optics, chemistry are linked together
- We have seen the most important physical models implemented in tiberCAD
- We have discussed the basics of how to couple atomistic and classical simulations
- Much effort is still needed to arrive at a true multiscale integration for transport simulations

*Additional info about **TiberCAD**:
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